[ExternalLocation=./]Consolas.ttf

Contents

1 Basic

1.1 vimrc

```
set number
syntax on
set showmode
set tabstop=2
set shiftwidth=2
set expandtab
set cursorline
set autoindent
set breakindent
filetype indent on
set smartcase
inoremap {<CR> {<CR>}<Esc>ko
```

1.2 Default code

```
#include <bits/stdc++.h>
using namespace std;
typedef long long l1;
typedef pair<int, int> pii;
typedef pair<ll, l1> pl1;
#define X first
#define Y second
#define SZ(a) ((int)a.size())
#define pb push_back
signed main() {
  ios::sync_with_stdio(0);
  cin.tie(0);
  return 0;
}
```

1.3 readchar

```
inline char readchar() {
  static const size_t bufsize = 65536;
  static char buf[bufsize];
  static char *p = buf, *end = buf;
  if (p == end)
    end = buf + fread_unlocked(buf, 1, bufsize, stdin),
        p = buf;
  return *p++;
}
```

1.4 Black Magic

```
#include <ext/pb_ds/assoc_container.hpp> //rb_tree
#include <ext/pb_ds/priority_queue.hpp>
                  _gnu_pbds;
using namespace
typedef __gnu_pbds::priority_queue<int> heap;
int main() {
  heap h1, h2;
  h1.push(1), h1.push(3);
  h2.push(2), h2.push(4);
  h1.join(h2);
  cout << h1.size() << h2.size() << h1.top() << endl;</pre>
  tree<11, null_type, less<11>, rb_tree_tag,
      tree_order_statistics_node_update>
      st;
  tree<11, 11, less<11>, rb_tree_tag,
      tree_order_statistics_node_update> mp;
  for (int x : {0, 2, 3, 4})
    st.insert(x);
  cout << *st.find_by_order(2) << st.order_of_key(1) <<</pre>
       endl; // 31
//__int128_t,__float128_t
```

2 Graph

2.1 BCC Vertex*

```
vector<int> G[N]; // 1-base
vector<int> nG[N], bcc[N];
int low[N], dfn[N], Time;
int bcc_id[N], bcc_cnt; // 1-base
bool is_cut[N]; // whether is av
bool cir[N];
int st[N], top;
```

```
} else if (dfn[v] < dfn[u] && v != pa)</pre>
      low[u] = min(low[u], dfn[v]);
  if (pa == -1 && child < 2)</pre>
    is_cut[u] = 0;
void bcc_init(int n) {
  Time = bcc_cnt = top = 0;
  for (int i = 1; i <= n; ++i)
    G[i].clear(), dfn[i] = bcc_id[i] = is_cut[i] = 0;
void bcc_solve(int n) {
 for (int i = 1; i <= n; ++i)
   if (!dfn[i])
     dfs(i);
  // circle-square tree
  for (int i = 1; i <= n; ++i)</pre>
    if (is_cut[i])
     bcc_id[i] = ++bcc_cnt, cir[bcc_cnt] = 1;
  for (int i = 1; i <= bcc_cnt && !cir[i]; ++i)
    for (int j : bcc[i])
      if (is_cut[j])
        nG[i].pb(bcc_id[j]), nG[bcc_id[j]].pb(i);
```

2.2 Bridge*

```
int low[N], dfn[N], Time; // 1-base
vector<pii> G[N], edge;
vector<bool> is_bridge;
void init(int n) {
  Time = 0;
  for (int i = 1; i <= n; ++i)</pre>
    G[i].clear(), low[i] = dfn[i] = 0;
void add_edge(int a, int b) {
  G[a].pb(pii(b, SZ(edge))), G[b].pb(pii(a, SZ(edge)));
  edge.pb(pii(a, b));
void dfs(int u, int f) {
  dfn[u] = low[u] = ++Time;
  for (auto i : G[u])
    if (!dfn[i.X])
    dfs(i.X, i.Y), low[u] = min(low[u], low[i.X]);
else if (i.Y != f)
       low[u] = min(low[u], dfn[i.X]);
  if (low[u] == dfn[u] && f != -1)
    is_bridge[f] = 1;
void solve(int n) {
  is_bridge.resize(SZ(edge));
  for (int i = 1; i <= n; ++i)
    if (!dfn[i])
      dfs(i, -1);
```

2.3 2SAT (SCC)*

```
struct SAT { // 0-base
  int low[N], dfn[N], bln[N], n, Time, nScc;
  bool instack[N], istrue[N];
  stack<int> st;
  vector<int> G[N], SCC[N];
  void init(int _n) {
    n = _n; // assert(n * 2 <= N);</pre>
    for (int i = 0; i < n + n; ++i)</pre>
      G[i].clear();
  void add_edge(int a, int b) { G[a].pb(b); }
  int rv(int a) {
    if (a > n)
      return a - n;
    return a + n;
  void add_clause(int a, int b) { add_edge(rv(a), b),
      add_edge(rv(b), a); }
  void dfs(int u) {
```

```
dfn[u] = low[u] = ++Time;
     instack[u] = 1, st.push(u);
for (int i : G[u])
       if (!dfn[i])
         dfs(i), low[u] = min(low[i], low[u]);
       else if (instack[i] && dfn[i] < dfn[u])</pre>
         low[u] = min(low[u], dfn[i]);
     if (low[u] == dfn[u]) {
       int tmp;
       do {
         tmp = st.top(), st.pop();
instack[tmp] = 0, bln[tmp] = nScc;
       } while (tmp != u);
       ++nScc;
    }
  bool solve() {
     Time = nScc = 0;
     for (int i = 0; i < n + n; ++i)
      SCC[i].clear(), low[i] = dfn[i] = bln[i] = 0;
     for (int i = 0; i < n + n; ++i)
       if (!dfn[i])
         dfs(i);
     for (int i = 0; i < n + n; ++i)
       SCC[bln[i]].pb(i);
     for (int i = 0; i < n; ++i) {
       if (bln[i] == bln[i + n])
        return false;
       istrue[i] = bln[i] < bln[i + n];
       istrue[i + n] = !istrue[i];
     return true;
  }
};
```

MinimumMeanCycle*

```
11 road[N][N]; // input here
struct MinimumMeanCycle {
  11 dp[N + 5][N], n;
  pll solve() {
    ll a = -1, b = -1, L = n + 1;
    for (int i = 2; i <= L; ++i)
      for (int k = 0; k < n; ++k)
        for (int j = 0; j < n; ++j)
          dp[i][j] = min(dp[i - 1][k] + road[k][j], dp[
               i][j]);
    for (int i = 0; i < n; ++i) {
      if (dp[L][i] >= INF)
        continue;
      11 ta = 0, tb = 1;
      for (int j = 1; j < n; ++j)
        if (dp[j][i] < INF && ta * (L - j) < (dp[L][i]</pre>
             - dp[j][i]) * tb)
          ta = dp[L][i] - dp[j][i], tb = L - j;
      if (ta == 0)
        continue;
      if (a == -1 || a * tb > ta * b)
        a = ta, b = tb;
    if (a != -1) {
      11 g = __gcd(a, b);
      return pll(a / g, b / g);
    return pll(-1LL, -1LL);
  }
  void init(int _n) {
    n = _n;
for (int i = 0; i < n; ++i)</pre>
      for (int j = 0; j < n; ++j)
        dp[i + 2][j] = INF;
};
```

Maximum Clique Dyn*

```
const int N = 150;
struct MaxClique { // Maximum Clique
 bitset<N> a[N], cs[N];
  int ans, sol[N], q, cur[N], d[N], n;
 void init(int _n) {
   n = _n;
```

```
for (int i = 0; i < n; i++)
       a[i].reset();
  void addEdge(int u, int v) { a[u][v] = a[v][u] = 1; }
  void csort(vector<int> &r, vector<int> &c) {
     int mx = 1, km = max(ans - q + 1, 1), t = 0, m = r.
         size();
     cs[1].reset(), cs[2].reset();
     for (int i = 0; i < m; i++) {</pre>
       int p = r[i], k = 1;
       while ((cs[k] & a[p]).count())
        k++;
       if (k > mx)
        mx++, cs[mx + 1].reset();
       cs[k][p] = 1;
       if (k < km)
         r[t++] = p;
    c.resize(m);
    if (t)
      c[t - 1] = 0;
     for (int k = km; k \le mx; k++)
       for (int p = cs[k]._Find_first(); p < N; p = cs[k]
           ]._Find_next(p))
         r[t] = p, c[t] = k, t++;
  void dfs(vector<int> &r, vector<int> &c, int 1,
       bitset<N> mask) {
     while (!r.empty()) {
       int p = r.back();
       r.pop_back(), mask[p] = 0;
       if (q + c.back() <= ans)</pre>
         return;
       cur[q++] = p;
       vector<int> nr, nc;
       bitset<N> nmask = mask & a[p];
       for (int i : r)
         if (a[p][i])
           nr.push_back(i);
       if (!nr.empty()) {
         if (1 < 4) {
           for (int i : nr)
             d[i] = (a[i] \& nmask).count();
           sort(nr.begin(), nr.end(), [&](int x, int y)
               { return d[x] > d[y]; });
         csort(nr, nc), dfs(nr, nc, l + 1, nmask);
       } else if (q > ans)
         ans = q, copy_n(cur, q, sol);
       c.pop_back(), q--;
  int solve(bitset<N> mask = bitset<N>(string(N, '1')))
        { // vertex mask
     vector<int> r, c;
     ans = q = 0;
     for (int i = 0; i < n; i++)
       if (mask[i])
         r.push_back(i);
     for (int i = 0; i < n; i++)</pre>
       d[i] = (a[i] & mask).count();
     sort(r.begin(), r.end(), [&](int i, int j) { return
    d[i] > d[j]; });
     csort(r, c), dfs(r, c, 1, mask);
    return ans; // sol[0 ~ ans-1]
  }
} graph;
2.6 Maximum Clique*
struct Maximum_Clique {
```

```
typedef bitset<MAXN> bst;
bst N[MAXN], empty;
int p[MAXN], n, ans;
void BronKerbosch2(bst R, bst P, bst X) {
  if (P == empty && X == empty)
    return ans = max(ans, (int)R.count()), void();
  bst tmp = P \mid X;
  int u;
  if ((R | P | X).count() <= ans)</pre>
    return;
  for (int uu = 0; uu < n; ++uu) {</pre>
```

```
u = p[uu];
      if (tmp[u] == 1)
    // if (double(clock())/CLOCKS_PER_SEC > .999)
    // return;
    bst now2 = P \& \sim N[u];
    for (int vv = 0; vv < n; ++vv) {
      int v = p[vv];
      if (now2[v] == 1) {
        R[v] = 1;
        BronKerbosch2(R, P & N[v], X & N[v]);
        R[v] = 0, P[v] = 0, X[v] = 1;
      }
    }
  }
  void init(int _n) {
    n = _n;
for (int i = 0; i < n; ++i)</pre>
      N[i].reset();
  void add_edge(int u, int v) { N[u][v] = N[v][u] = 1;
  int solve() { // remember srand
    bst R, P, X;
ans = 0, P.flip();
    for (int i = 0; i < n; ++i)</pre>
      p[i] = i;
    random_shuffle(p, p + n), BronKerbosch2(R, P, X);
    return ans;
 }
};
```

2.7 Minimum Steiner Tree*

```
// Minimum Steiner Tree
// O(V 3^T + V^2 2^T)
struct SteinerTree { // 0-base
  static const int T = 10, N = 105, INF = 1e9;
  int n, dst[N][N], dp[1 << T][N], tdst[N];
int vcost[N]; // the cost of vertexs</pre>
  void init(int _n) {
    n = _n;
for (int i = 0; i < n; ++i) {</pre>
       for (int j = 0; j < n; ++j)
         dst[i][j] = INF;
       dst[i][i] = vcost[i] = 0;
    }
  }
  void add_edge(int ui, int vi, int wi) { dst[ui][vi] =
        min(dst[ui][vi], wi); }
  void shortest_path() {
    for (int k = 0; k < n; ++k)
       for (int i = 0; i < n; ++i)</pre>
         for (int j = 0; j < n; ++j)
           dst[i][j] = min(dst[i][j], dst[i][k] + dst[k]
                1[i]);
  int solve(const vector<int> &ter) {
    shortest_path();
    int t = SZ(ter);
    for (int i = 0; i < (1 << t); ++i)
for (int j = 0; j < n; ++j)</pre>
         dp[i][j] = INF;
    for (int i = 0; i < n; ++i)
      dp[0][i] = vcost[i];
    for (int msk = 1; msk < (1 << t); ++msk) {</pre>
       if (!(msk & (msk - 1))) {
         int who = __lg(msk);
for (int i = 0; i < n; ++i)</pre>
           dp[msk][i] = vcost[ter[who]] + dst[ter[who]][
                i];
       for (int i = 0; i < n; ++i)
         for (int submsk = (msk - 1) & msk; submsk;
              submsk = (submsk - 1) \& msk)
           dp[msk][i] =
                min(dp[msk][i], dp[submsk][i] + dp[msk ^
    submsk][i] - vcost[i]);
       for (int i = 0; i < n; ++i) {
         tdst[i] = INF;
         for (int j = 0; j < n; ++j)
```

2.8 Minimum Arborescence*

```
struct zhu_liu { // O(VE)
  struct edge {
    int u, v;
    11 w;
  };
  vector<edge> E; // 0-base
  int pe[N], id[N], vis[N];
  ll in[N];
  void init() { E.clear(); }
  void add_edge(int u, int v, ll w) {
    if (u != v)
      E.pb(edge{u, v, w});
  11 build(int root, int n) {
    11 \text{ ans} = 0;
    for (;;) {
      fill_n(in, n, INF);
      for (int i = 0; i < SZ(E); ++i)
        if (E[i].u != E[i].v && E[i].w < in[E[i].v])</pre>
          pe[E[i].v] = i, in[E[i].v] = E[i].w;
      for (int u = 0; u < n; ++u) // no solution
        if (u != root && in[u] == INF)
          return -INF;
      int cntnode = 0;
      fill_n(id, n, -1), fill_n(vis, n, -1);
      for (int u = 0; u < n; ++u) {
        if (u != root)
          ans += in[u];
        int v = u:
        while (vis[v] != u && !~id[v] && v != root)
          vis[v] = u, v = E[pe[v]].u;
        if (v != root && !~id[v]) {
          for (int x = E[pe[v]].u; x != v; x = E[pe[x]]
               11.u)
            id[x] = cntnode;
          id[v] = cntnode++;
        }
      if (!cntnode)
        break; // no cycle
      for (int u = 0; u < n; ++u)
        if (!~id[u])
          id[u] = cntnode++;
      for (int i = 0; i < SZ(E); ++i) {
        int v = E[i].v;
        E[i].u = id[E[i].u], E[i].v = id[E[i].v];
        if (E[i].u != E[i].v)
          E[i].w -= in[v];
      n = cntnode, root = id[root];
    }
    return ans;
  }
};
```

2.9 Vizing's theorem

```
int X[kN] = {}, a;
  auto update = [&](int u) {
    for (X[u] = 1; C[u][X[u]]; X[u]++)
  auto color = [&](int u, int v, int c) {
    int p = G[u][v];
    G[u][v] = G[v][u] = c;
   C[u][c] = v, C[v][c] = u;
    C[u][p] = C[v][p] = 0;
    if (p)
      X[u] = X[v] = p;
      update(u), update(v);
    return p;
 auto flip = [&](int u, int c1, int c2) {
  int p = C[u][c1];
    swap(C[u][c1], C[u][c2]);
    if (p)
     G[u][p] = G[p][u] = c2;
    if (!C[u][c1])
      X[u] = c1;
    if (!C[u][c2])
     X[u] = c2:
    return p;
  for (int i = 1; i <= N; i++)
   X[i] = 1;
  for (int t = 0; t < E.size(); t++) {</pre>
    int u = E[t].first, v0 = E[t].second, v = v0, c0 =
        X[u], c = c0, d;
    vector<pair<int, int>> L;
    int vst[kN] = {};
    while (!G[u][v0]) {
      L.emplace_back(v, d = X[v]);
      if (!C[v][c])
        for (a = (int)L.size() - 1; a >= 0; a--)
          c = color(u, L[a].first, c);
      else if (!C[u][d])
        for (a = (int)L.size() - 1; a >= 0; a--)
          color(u, L[a].first, L[a].second);
      else if (vst[d])
        break;
      else
        vst[d] = 1, v = C[u][d];
    if (!G[u][v0]) {
      for (; v; v = flip(v, c, d), swap(c, d))
      if (C[u][c0]) {
        for (a = (int)L.size() - 2; a >= 0 && L[a].
            second != c; a--)
        for (; a >= 0; a--)
          color(u, L[a].first, L[a].second);
      } else
        t--;
 }
} // namespace vizing
```

2.10 Minimum Clique Cover*

```
struct Clique_Cover { // 0-base, 0(n2^n)
 int co[1 << N], n, E[N];</pre>
  int dp[1 << N];</pre>
  void init(int _n) {
    n = _n, fill_n(dp, 1 << n, 0);
    fill_n(E, n, 0), fill_n(co, 1 << n, 0);
  void add_edge(int u, int v) { E[u] |= 1 << v, E[v] |=</pre>
       1 << u; }
  int solve() {
    for (int i = 0; i < n; ++i)
      co[1 << i] = E[i] | (1 << i);
    co[0] = (1 << n) - 1;
    dp[0] = (n & 1) * 2 - 1;
    for (int i = 1; i < (1 << n); ++i) {
      int t = i & -i;
      dp[i] = -dp[i ^ t];
```

```
co[i] = co[i ^ t] & co[t];
}
for (int i = 0; i < (1 << n); ++i)
    co[i] = (co[i] & i) == i;
fwt(co, 1 << n);
for (int ans = 1; ans < n; ++ans) {
    int sum = 0;
    for (int i = 0; i < (1 << n); ++i)
        sum += (dp[i] *= co[i]);
    if (sum)
        return ans;
}
return n;
}
</pre>
```

2.11 NumberofMaximalClique*

```
struct BronKerbosch { // 1-base
  int n, a[N], g[N][N];
  int S, all[N][N], some[N][N], none[N][N];
  void init(int _n) {
    for (int i = 1; i <= n; ++i)
      for (int j = 1; j <= n; ++j)
        g[i][j] = 0;
  void add_edge(int u, int v) { g[u][v] = g[v][u] = 1;
  void dfs(int d, int an, int sn, int nn) {
    if (S > 1000)
      return; // pruning
    if (sn == 0 && nn == 0)
      ++S;
    int u = some[d][0];
    for (int i = 0; i < sn; ++i) {
      int v = some[d][i];
      if (g[u][v])
        continue;
      int tsn = 0, tnn = 0;
      copy_n(all[d], an, all[d + 1]);
      all[d + 1][an] = v;
      for (int j = 0; j < sn; ++j)
        if (g[v][some[d][j]])
          some[d + 1][tsn++] = some[d][j];
      for (int j = 0; j < nn; ++j)
        if (g[v][none[d][j]])
          none[d + 1][tnn++] = none[d][j];
      dfs(d + 1, an + 1, tsn, tnn);
      some[d][i] = 0, none[d][nn++] = v;
    }
  int solve() {
    iota(some[0], some[0] + n, 1);
    S = 0, dfs(0, 0, n, 0);
    return S;
  }
};
```

2.12 Theory

3 Data Structure

3.1 Leftist Tree

```
if (V(a->r) > V(a->l))
    swap(a->r, a->l);
a->v = V(a->r) + 1, a->sz = sz(a->l) + sz(a->r) + 1;
a->sum = sum(a->l) + sum(a->r) + a->data;
return a;
}
void pop(node *&o) {
    node *tmp = o;
    o = merge(o->l, o->r);
    delete tmp;
}
```

3.2 Heavy light Decomposition

```
struct Heavy light Decomposition { // 1-base
  int n, ulink[10005], deep[10005], mxson[10005], w
       [10005], pa[10005];
  int t, pl[10005], data[10005], dt[10005], bln[10005],
        edge[10005], et;
  vector<pii> G[10005];
  void init(int _n) {
    n = _n, t = 0, et = 1;
    for (int i = 1; i <= n; ++i)
      G[i].clear(), mxson[i] = 0;
  void add_edge(int a, int b, int w) {
    G[a].pb(pii(b, et)), G[b].pb(pii(a, et)), edge[et
         ++] = w;
  void dfs(int u, int f, int d) {
    w[u] = 1, pa[u] = f, deep[u] = d++;
    for (auto &i : G[u])
       if (i.X != f) {
         \mathsf{dfs}(\mathsf{i}.\mathsf{X},\;\mathsf{u},\;\mathsf{d}),\;\mathsf{w}[\mathsf{u}]\; +=\; \mathsf{w}[\mathsf{i}.\mathsf{X}];
         if (w[mxson[u]] < w[i.X])</pre>
           mxson[u] = i.X;
       } else
         bln[i.Y] = u, dt[u] = edge[i.Y];
  void cut(int u, int link) {
    data[pl[u] = t++] = dt[u], ulink[u] = link;
    if (!mxson[u])
       return;
    cut(mxson[u], link);
    for (auto i : G[u])
       if (i.X != pa[u] && i.X != mxson[u])
         cut(i.X, i.X);
  void build() { dfs(1, 1, 1), cut(1, 1), /*build*/; }
  int query(int a, int b) {
    int ta = ulink[a], tb = ulink[b], re = 0;
    while (ta != tb)
       if (deep[ta] < deep[tb])</pre>
         /*query*/, tb = ulink[b = pa[tb]];
       else /*query*/
         , ta = ulink[a = pa[ta]];
    if (a == b)
      return re;
    if (pl[a] > pl[b])
       swap(a, b);
    /*query*/
    return re;
  }
};
```

3.3 Centroid Decomposition*

```
void get_cent(int u, int f, int &mx, int &c, int num)
    int mxsz = 0;
    sz[u] = 1;
    for (pll e : G[u])
      if (!done[e.X] && e.X != f) {
         get_cent(e.X, u, mx, c, num);
         sz[u] += sz[e.X], mxsz = max(mxsz, sz[e.X]);
    if (mx > max(mxsz, num - sz[u]))
      mx = max(mxsz, num - sz[u]), c = u;
  void dfs(int u, int f, ll d, int org) {
    // if required, add self info or climbing info
    dis[layer[org]][u] = d;
     for (pll e : G[u])
      if (!done[e.X] && e.X != f)
         dfs(e.X, u, d + e.Y, org);
  int cut(int u, int f, int num) {
    int mx = 1e9, c = 0, lc;
    get_cent(u, f, mx, c, num);
    done[c] = 1, pa[c] = f, layer[c] = layer[f] + 1;
for (pll e : G[c])
      if (!done[e.X]) {
        if (sz[e.X] > sz[c])
          lc = cut(e.X, c, num - sz[c]);
           lc = cut(e.X, c, sz[e.X]);
        upinfo[lc] = pll(), dfs(e.X, c, e.Y, c);
    return done[c] = 0, c;
  void build() { cut(1, 0, n); }
  void modify(int u) {
    for (int a = u, ly = layer[a]; a; a = pa[a], --ly)
       info[a].X += dis[ly][u], ++info[a].Y;
      if (pa[a])
         upinfo[a].X += dis[ly - 1][u], ++upinfo[a].Y;
    }
  11 query(int u) {
    11 \text{ rt} = 0;
    for (int a = u, ly = layer[a]; a; a = pa[a], --ly)
       rt += info[a].X + info[a].Y * dis[ly][u];
       if (pa[a])
        rt -= upinfo[a].X + upinfo[a].Y * dis[ly - 1][u
             1;
    return rt;
};
```

3.4 Link cut tree*

```
struct Splay { // xor-sum
  static Splay nil;
  Splay *ch[2], *f;
  int val, sum, rev, size;
  f = ch[0] = ch[1] = &nil;
  bool isr() { return f->ch[0] != this && f->ch[1] !=
     this; }
  int dir() { return f->ch[0] == this ? 0 : 1; }
  void setCh(Splay *c, int d) {
   ch[d] = c;
   if (c != &nil)
     c->f = this;
   pull();
  void push() {
   if (!rev)
     return;
    swap(ch[0], ch[1]);
   if (ch[0] != &nil)
     ch[0]->rev ^= 1;
   if (ch[1] != &nil)
     ch[1]->rev ^= 1;
```

con

```
, x->pull(); }
    rev = 0:
                                                             int query(Splay *x, Splay *y) {
  void pull() {
                                                               split(x, y);
   // take care of the nil!
                                                               return v->sum;
    size = ch[0] -> size + ch[1] -> size + 1;
    sum = ch[0] \rightarrow sum \wedge ch[1] \rightarrow sum \wedge val;
                                                             3.5
                                                                    KDTree
    if (ch[0] != &nil)
      ch[0]->f = this;
    if (ch[1] != &nil)
                                                             namespace kdt {
      ch[1]->f = this;
                                                             int root, lc[maxn], rc[maxn], xl[maxn], xr[maxn], yl[
                                                                 maxn], vr[maxn];
} Splay::nil;
                                                             point p[maxn];
Splay *nil = &Splay::nil;
                                                             int build(int 1, int r, int dep = 0) {
void rotate(Splay *x) {
                                                               if (1 == r)
 Splay *p = x \rightarrow f;
                                                                 return -1;
  int d = x - 3 dir();
                                                               function<bool(const point &, const point &)> f = [dep
  if (!p->isr())
                                                                    ](const point &a,
   p->f->setCh(x, p->dir());
   x->f = p->f;
 p->setCh(x->ch[!d], d);
 x->setCh(p, !d);
 p->pull(), x->pull();
void splay(Splay *x) {
  vector<Splay *> splayVec;
  for (Splay *q = x;; q = q \rightarrow f) {
    splayVec.pb(q);
                                                                 if (dep & 1)
    if (q->isr())
                                                                   return a.x < b.x;</pre>
      break;
                                                                 else
                                                                   return a.y < b.y;</pre>
  reverse(ALL(splayVec));
  for (auto it : splayVec)
                                                               int m = (1 + r) >> 1;
   it->push();
                                                               nth_element(p + 1, p + m, p + r, f);
 while (!x->isr()) {
                                                               x1[m] = xr[m] = p[m].x;
   if (x->f->isr())
                                                               y1[m] = yr[m] = p[m].y;
      rotate(x);
                                                               lc[m] = build(1, m, dep + 1);
    else if (x->dir() == x->f->dir())
                                                               if (~lc[m]) {
     rotate(x->f), rotate(x);
                                                                 xl[m] = min(xl[m], xl[lc[m]]);
    else
                                                                 xr[m] = max(xr[m], xr[lc[m]]);
      rotate(x), rotate(x);
                                                                 yl[m] = min(yl[m], yl[lc[m]]);
 }
                                                                 yr[m] = max(yr[m], yr[lc[m]]);
Splay *access(Splay *x) {
                                                               rc[m] = build(m + 1, r, dep + 1);
  Splay *q = nil;
                                                               if (~rc[m]) {
  for (; x != nil; x = x->f)
                                                                 xl[m] = min(xl[m], xl[rc[m]]);
   splay(x), x \rightarrow setCh(q, 1), q = x;
                                                                 xr[m] = max(xr[m], xr[rc[m]]);
                                                                 yl[m] = min(yl[m], yl[rc[m]]);
                                                                 yr[m] = max(yr[m], yr[rc[m]]);
void root_path(Splay *x) { access(x), splay(x); }
void chroot(Splay *x) {
                                                               return m;
 root_path(x), x->rev ^= 1;
  x->push(), x->pull();
                                                             bool bound(const point &q, int o, long long d) {
                                                               double ds = sqrt(d + 1.0);
void split(Splay *x, Splay *y) { chroot(x), root_path(y
                                                               if (q.x < x1[o] - ds || q.x > xr[o] + ds || q.y < y1[
                                                                   o] - ds ||
void link(Splay *x, Splay *y) {
                                                                   q.v > vr[o] + ds)
                                                                 return false;
 root_path(x), chroot(y);
 x->setCh(y, 1);
                                                               return true;
void cut(Splay *x, Splay *y) {
                                                             long long dist(const point &a, const point &b) {
  split(x, y);
                                                               return (a.x - b.x) * 111 * (a.x - b.x) + (a.y - b.y)
  if (y->size != 5)
                                                                    * 111 * (a.y - b.y);
   return;
 y->push();
                                                             void dfs(const point &q, long long &d, int o, int dep =
 y - ch[0] = y - ch[0] - f = nil;
                                                                  0) {
                                                               if (!bound(q, o, d))
Splay *get_root(Splay *x) {
                                                                 return;
  for (root_path(x); x->ch[0] != nil; x = x->ch[0])
                                                               long long cd = dist(p[o], q);
   x->push();
                                                               if (cd != 0)
  splay(x);
                                                                 d = min(d, cd);
  return x;
                                                               if ((dep & 1) && q.x < p[o].x || !(dep & 1) && q.y <
                                                                   p[o].y) {
bool conn(Splay *x, Splay *y) { return get_root(x) ==
                                                                 if (~lc[o])
    get_root(y); }
                                                                   dfs(q, d, lc[o], dep + 1);
Splay *lca(Splay *x, Splay *y) {
                                                                 if (~rc[o])
  access(x), root_path(y);
                                                                   dfs(q, d, rc[o], dep + 1);
  if (y->f == nil)
                                                               } else {
                                                                 if (~rc[o])
   return v;
  return y->f;
                                                                   dfs(q, d, rc[o], dep + 1);
                                                                 if (~lc[o])
void change(Splay *x, int val) { splay(x), x \rightarrow val = val
                                                                   dfs(q, d, lc[o], dep + 1);
```

```
}

void init(const vector<point> &v) {
  for (int i = 0; i < v.size(); ++i)
    p[i] = v[i];
  root = build(0, v.size());
}
long long nearest(const point &q) {
  long long res = 1e18;
  dfs(q, res, root);
  return res;
}
} // namespace kdt</pre>
```

4 Flow/Matching

4.1 Kuhn Munkres

```
struct KM { // 0-base
  int w[MAXN][MAXN], h1[MAXN], hr[MAXN], s1k[MAXN], n;
  int fl[MAXN], fr[MAXN], pre[MAXN], qu[MAXN], ql, qr;
  bool v1[MAXN], vr[MAXN];
  void init(int _n) {
   n = _n;
for (int i = 0; i < n; ++i)
      for (int j = 0; j < n; ++j)
        w[i][j] = -INF;
  void add_edge(int a, int b, int wei) { w[a][b] = wei;
  bool Check(int x) {
    if (vl[x] = 1, \sim fl[x])
      return vr[qu[qr++] = fl[x]] = 1;
    while (~x)
      swap(x, fr[fl[x] = pre[x]]);
    return 0;
  void Bfs(int s) {
    fill(slk, slk + n, INF);
    fill(vl, vl + n, 0), fill(vr, vr + n, 0);
    ql = qr = 0, qu[qr++] = s, vr[s] = 1;
    while (1) {
      int d;
      while (ql < qr)</pre>
        for (int x = 0, y = qu[ql++]; x < n; ++x)
          if (!vl[x] \&\& slk[x] >= (d = hl[x] + hr[y] -
               w[x][y])
            if (pre[x] = y, d)
              slk[x] = d;
            else if (!Check(x))
              return;
      d = INF;
      for (int x = 0; x < n; ++x)
        if (!vl[x] && d > slk[x])
          d = slk[x];
      for (int x = 0; x < n; ++x) {
        if (v1[x])
          hl[x] += d;
        else
          slk[x] -= d;
        if (vr[x])
          hr[x] -= d;
      for (int x = 0; x < n; ++x)
        if (!v1[x] && !slk[x] && !Check(x))
          return;
    }
  int Solve() {
    fill(fl, fl + n, -1), fill(fr, fr + n, -1), fill(hr
        , hr + n, 0);
    for (int i = 0; i < n; ++i)
      hl[i] = *max_element(w[i], w[i] + n);
    for (int i = 0; i < n; ++i)
      Bfs(i);
    int res = 0;
    for (int i = 0; i < n; ++i)
      res += w[i][fl[i]];
    return res;
};
```

4.2 MincostMaxflow

```
struct MCMF { // 0-base
  struct edge {
     ll from, to, cap, flow, cost, rev;
  } *past[MAXN];
  vector<edge> G[MAXN];
  bitset<MAXN> inq;
  11 dis[MAXN], up[MAXN], s, t, mx, n;
bool BellmanFord(ll &flow, ll &cost) {
     fill(dis, dis + n, INF);
     queue<ll> q;
     q.push(s), inq.reset(), inq[s] = 1;
up[s] = mx - flow, past[s] = 0, dis[s] = 0;
     while (!q.empty()) {
       11 u = q.front();
q.pop(), inq[u] = 0;
       if (!up[u])
         continue;
       for (auto &e : G[u])
         if (e.flow != e.cap && dis[e.to] > dis[u] + e.
              cost) {
            dis[e.to] = dis[u] + e.cost, past[e.to] = &e;
            up[e.to] = min(up[u], e.cap - e.flow);
            if (!inq[e.to])
              inq[e.to] = 1, q.push(e.to);
         }
     if (dis[t] == INF)
       return 0:
     flow += up[t], cost += up[t] * dis[t];
     for (11 i = t; past[i]; i = past[i]->from) {
       auto &e = *past[i];
       e.flow += up[t], G[e.to][e.rev].flow -= up[t];
     }
     return 1;
  11 MinCostMaxFlow(ll _s, ll _t, ll &cost) {
     s = _s, t = _t, cost = 0;
     11 \text{ flow} = 0;
     while (BellmanFord(flow, cost))
     return flow;
  void init(ll _n, ll _mx) {
     n = _n, mx = _mx;
for (int i = 0; i < n; ++i)</pre>
       G[i].clear();
  void add_edge(ll a, ll b, ll cap, ll cost) {
     G[a].pb(edge{a, b, cap, 0, cost, G[b].size()});
     G[b].pb(edge{b, a, 0, 0, -cost, G[a].size() - 1});
};
```

4.3 Minimum Weight Matching (Clique version)*

```
struct Graph { // 0-base (Perfect Match), n is even
  int n, match[N], onstk[N], stk[N], tp;
  11 edge[N][N], dis[N];
  void init(int _n) {
   n = _n, tp = 0;
    for (int i = 0; i < n; ++i)
      fill_n(edge[i], n, 0);
  void add_edge(int u, int v, ll w) { edge[u][v] = edge
      [v][u] = w; }
  bool SPFA(int u) {
    stk[tp++] = u, onstk[u] = 1;
    for (int v = 0; v < n; ++v)
      if (!onstk[v] && match[u] != v) {
         int m = match[v];
         if (dis[m] > dis[u] - edge[v][m] + edge[u][v])
           dis[m] = dis[u] - edge[v][m] + edge[u][v];
           onstk[v] = 1, stk[tp++] = v;
if (onstk[m] || SPFA(m))
             return 1:
           --tp, onstk[v] = 0;
        }
      }
```

```
onstk[u] = 0, --tp;
    return 0;
  ll solve() { // find a match
    for (int i = 0; i < n; ++i)
      match[i] = i ^ 1;
    while (1) {
      int found = 0;
      fill_n(dis, n, 0);
      fill_n(onstk, n, 0);
for (int i = 0; i < n; ++i)
        if (tp = 0, !onstk[i] && SPFA(i))
           for (found = 1; tp >= 2;) {
             int u = stk[--tp];
             int v = stk[--tp];
             match[u] = v, match[v] = u;
      if (!found)
        break:
    ll ret = 0;
    for (int i = 0; i < n; ++i)
      ret += edge[i][match[i]];
    return ret >> 1;
  }
};
```

4.4 SW-mincut

```
// global min cut
struct SW { // O(V^3)
  static const int MXN = 514;
  int n, vst[MXN], del[MXN];
  int edge[MXN][MXN], wei[MXN];
  void init(int _n) { n = _n, MEM(edge, 0), MEM(del, 0)
      ; }
  void addEdge(int u, int v, int w) { edge[u][v] += w,
      edge[v][u] += w; }
  void search(int &s, int &t) {
    MEM(vst, 0), MEM(wei, 0), s = t = -1;
    while (1) {
      int mx = -1, cur = 0;
      for (int i = 0; i < n; ++i)
        if (!del[i] && !vst[i] && mx < wei[i])</pre>
          cur = i, mx = wei[i];
      if (mx == -1)
       break;
      vst[cur] = 1, s = t, t = cur;
      for (int i = 0; i < n; ++i)
        if (!vst[i] && !del[i])
          wei[i] += edge[cur][i];
   }
  int solve() {
   int res = INF;
    for (int i = 0, x, y; i < n - 1; ++i) {
      search(x, y), res = min(res, wei[y]), del[y] = 1;
      for (int j = 0; j < n; ++j)
        edge[x][j] = (edge[j][x] += edge[y][j]);
    return res;
};
```

4.5 BoundedFlow(Dinic*)

```
struct BoundedFlow { // 0-base
 struct edge {
    int to, cap, flow, rev;
  vector<edge> G[N];
 int n, s, t, dis[N], cur[N], cnt[N];
 void init(int _n) {
   n = _n;
for (int i = 0; i < n + 2; ++i)</pre>
      G[i].clear(), cnt[i] = 0;
 void add_edge(int u, int v, int lcap, int rcap) {
   cnt[u] -= lcap, cnt[v] += lcap;
    G[u].pb(edge{v, rcap, lcap, SZ(G[v])});
    G[v].pb(edge{u, 0, 0, SZ(G[u]) - 1});
```

```
void add_edge(int u, int v, int cap) {
     G[u].pb(edge{v, cap, 0, SZ(G[v])})
     G[v].pb(edge{u, 0, 0, SZ(G[u]) - 1});
   int dfs(int u, int cap) {
     if (u == t || !cap)
       return cap;
     for (int &i = cur[u]; i < SZ(G[u]); ++i) {</pre>
       edge &e = G[u][i];
       if (dis[e.to] == dis[u] + 1 && e.cap != e.flow) {
         int df = dfs(e.to, min(e.cap - e.flow, cap));
         if (df) {
           e.flow += df, G[e.to][e.rev].flow -= df;
           return df;
         }
      }
     dis[u] = -1;
     return 0:
   bool bfs() {
     fill_n(dis, n + 3, -1);
     queue<int> q;
     q.push(s), dis[s] = 0;
     while (!q.empty()) {
       int u = q.front();
       q.pop();
       for (edge &e : G[u])
         if (!~dis[e.to] && e.flow != e.cap)
           q.push(e.to), dis[e.to] = dis[u] + 1;
     return dis[t] != -1;
   int maxflow(int _s, int _t) {
     s = _s, t = _t;
     int \overline{flow} = 0, df;
     while (bfs()) {
       fill_n(cur, n + 3, 0);
       while ((df = dfs(s, INF)))
         flow += df;
     }
     return flow;
   bool solve() {
     int sum = 0;
     for (int i = 0; i < n; ++i)
       if (cnt[i] > 0)
         add_edge(n + 1, i, cnt[i]), sum += cnt[i];
       else if (cnt[i] < 0)</pre>
         add_edge(i, n + 2, -cnt[i]);
     if (sum != maxflow(n + 1, n + 2))
       sum = -1;
     for (int i = 0; i < n; ++i)
       if (cnt[i] > 0)
       G[n + 1].pop_back(), G[i].pop_back();
else if (cnt[i] < 0)</pre>
         G[i].pop_back(), G[n + 2].pop_back();
     return sum != -1;
   int solve(int _s, int
     add_edge(_t, _s, INF);
     if (!solve())
      return -1; // invalid flow
     int x = G[_t].back().flow;
     return G[_t].pop_back(), G[_s].pop_back(), x;
};
```

4.6 Flow Models

•Maximum/Minimum flow with lower bound / Circulation problem

1.Construct super source \boldsymbol{S} and sink T.

2.For each edge (x,y,l,u), connect x o y with capacity u-l. 3.For each vertex \boldsymbol{v} , denote by $in(\boldsymbol{v})$ the difference between the sum of

incoming lower bounds and the sum of outgoing lower bounds. 4.If in(v)>0, connect $S\to v$ with capacity in(v), otherwise, connect $v \to T$ with capacity -in(v).

–To maximize, connect $t \to s$ with capacity ∞ (skip this in circulation problem), and let f be the maximum flow from S to T. If $f
eq \sum_{v \in V, in(v) > 0} in(v)$, there's no solution. Otherwise, the maximum

flow from s to t is the answer. -To minimize, let f be the maximum flow from S to T. Connect $t \to s$ with capacity ∞ and let the flow from S to T be f'. If $f+f' \ne \sum_{v \in V, in(v)>0} in(v)$, there's no solution. Otherwise, f' is the answer.

```
5.The solution of each edge e is l_e+f_e, where f_e corresponds to the flow 	extstyle 5.3 Manacher*
  of edge e on the graph.
                                                                                  int z[MAXN];
 int Manacher(string tmp) {
  graph(X,Y)
1. Redirect every edge: y \to x if (x,y) \in M, x \to y otherwise.
                                                                                      string s = "%";
2.DFS from unmatched vertices in X. 
 3.x \in X is chosen iff x is unvisited. 
 4.y \in Y is chosen iff y is visited.
                                                                                      int 1 = 0, r = 0, x, ans;
                                                                                      for (char c : tmp)
                                                                                       s.pb(c), s.pb('%');
 •Minimum cost cyclic flow
                                                                                      ans = 0, x = 0;
                                                                                      for (int i = 1; i < SZ(s); ++i) {
  z[i] = r > i ? min(z[2 * l - i], r - i) : 1;
1.Consruct super source {\cal S} and sink {\cal T}
2.For each edge (x,y,c), connect x \to y with (cost,cap)=(c,1) if c>0, otherwise connect y \to x with (cost,cap)=(-c,1)
3.For each edge with c<0, sum these cost as K, then increase d(y) by
                                                                                        while (s[i + z[i]] == s[i - z[i]])
1, decrease d(x) by 1 4. For each vertex v with d(v)>0, connect S\to v with (cost,cap)=(0,d(v)) 5. For each vertex v with d(v)<0, connect v\to T with (cost,cap)=(0,d(v))
                                                                                           ++z[i];
                                                                                         if(z[i] + i > r)
                                                                                           r = z[i] + i, l = i;
6.Flow from S to T, the answer is the cost of the flow C+\bar{K}
                                                                                      for (int i = 1; i < SZ(s); ++i)
  if (s[i] == '%')</pre>
 •Maximum density induced subgraph
1.Binary search on answer, suppose we're checking answer {\cal T}
2. Construct a max flow model, let K be the sum of all weights 3. Connect source s \to v, v \in G with capacity K 4. For each edge (u,v,w) in G, connect u \to v and v \to u with capacity w 5. For v \in G, connect it with sink v \to t with capacity K + 2T - (\sum_{e \in E(v)} w(e)) - 2w(v) 6. T is a valid answer if the maximum flow f < K^{\dagger}V^{\dagger}
                                                                                           x = max(x, z[i]);
                                                                                     ans = x / 2 * 2, x = 0;
for (int i = 1; i < SZ(s); ++i)
if (s[i] != '%')
                                                                                           x = max(x, z[i]);
6.T is a valid answer if the maximum flow f < K|V|
                                                                                      return max(ans, (x - 1) / 2 * 2 + 1);
-Minimum weight edge cover 1.For each v \in V create a copy v' , and connect u' \to v' with weight
                                                                                  5.4 SAIS*
2.Connect v 	o v' with weight 2\mu(v), where \mu(v) is the cost of the cheapest
  edge incident to \boldsymbol{v}.
3. Find the minimum weight perfect matching on G^{\prime} .
                                                                                   class SAIS {
                                                                                   public:

    Project selection problem

1.If p_v>0, create edge (s,v) with capacity p_v; otherwise, create edge (v,t) with capacity -p_v.
2.Create edge (u,v) with capacity w with w being the cost of choosing u
                                                                                      int *SA, *H;
                                                                                      // zero based, string content MUST > 0
                                                                                      // result height H[i] is LCP(SA[i - 1], SA[i])
  without choosing v.
3. The mincut is equivalent to the maximum profit of a subset of projects.
                                                                                      // string, length, |sigma|
                                                                                      void build(int *s, int n, int m = 128) {
 •0/1 quadratic programming
            \sum_{x} c_{x} x + \sum_{y} c_{y} \bar{y} + \sum_{xy} c_{xy} x \bar{y} + \sum_{xyx'y'} c_{xyx'y'} (x\bar{y} + x'\bar{y'})
                                                                                        copy_n(s, n, _s);
                                                                                         h[0] = s[n++] = 0;
                                                                                        sais(_s, _sa, _p, _q, _t, _c, n, m);
                                                                                        mkhei(n);
  can be minimized by the mincut of the following graph:
                                                                                        SA = _sa + 1;
H = _h + 1;
1.Create edge (x,t) with capacity c_x and create edge (s,y) with capacity
. Create edge (x,y) with capacity c_{xy}. 
 3.Create edge (x,y) and edge (x',y') with capacity c_{xyx'y'}.
                                                                                   private:
                                                                                      bool _t[N * 2];
         String
                                                                                      5.1 KMP
                                                                                      void mkhei(int n) {
                                                                                        for (int i = 0; i < n; i++)
  int F[MAXN];
                                                                                          r[_sa[i]] = i;
  vector<int> match(string A, string B) {
                                                                                         for (int i = 0; i < n; i++)
     vector<int> ans;
     F[0] = -1, F[1] = 0;
                                                                                           if (r[i]) {
                                                                                              int ans = i > 0? max([r[i - 1]] - 1, 0) : 0;
     for (int i = 1, j = 0; i < SZ(B); F[++i] = ++j) {
                                                                                              while (_s[i + ans] == _s[_sa[r[i] - 1] + ans])
        if (B[i] == B[j])
                                                                                                ans++:
          F[i] = F[j]; // optimize
                                                                                              _h[r[i]] = ans;
        while (j != -1 && B[i] != B[j])
          j = F[j];
                                                                                      void sais(int *s, int *sa, int *p, int *q, bool *t,
     for (int i = 0, j = 0; i < SZ(A); ++i) {
                                                                                           int *c, int n, int z) {
        while (j != -1 && A[i] != B[j])
                                                                                        bool uniq = t[n - 1] = 1, neq;
          j = F[j];
                                                                                        int nn = 0, nmxz = -1, *nsa = sa + n, *ns = s + n,
        if (++j == SZ(B))
                                                                                              1st = -1:
          ans.pb(i + 1 - j), j = F[j];
                                                                                   #define MAGIC(XD)
     return ans;
                                                                                      fill_n(sa, n, 0);
  5.2 Z-value
  const int MAXn = 1e5 + 5;
                                                                                      copy_n(c, z, x);
  int z[MAXn];
  void make_z(string s) {
     int 1 = 0, r = 0;
                                                                                      XD:
     for (int i = 1; i < s.size(); i++) {
        for (z[i] = max(0, min(r - i + 1, z[i - 1]));
               i + z[i] < s.size() && s[i + z[i]] == s[z[i]];
                                                                                      copy_n(c, z - 1, x + 1);
                      z[i]++)
        if(i + z[i] - 1 > r)
          l = i, r = i + z[i] - 1;
                                                                                      for (int i = 0; i < n; i++)
```

} }

```
if (sa[i] && !t[sa[i] - 1])
                                                                 for (char c : s) {
                                                                   while (X && !~nx[X][c - 'a'])
                                                                     X = fl[X];
      sa[x[s[sa[i] - 1]]++] = sa[i] - 1;
                                                                   X = X ? nx[X][c - 'a'] : 1, ++cnt[X];
  copy n(c, z, x);
                                                                 for (int i = top - 2; i > 0; --i)
                                                                   cnt[fl[pri[i]]] += cnt[pri[i]];
  for (int i = n - 1; i >= 0; i - -)
                                                            };
                                                                    Smallest Rotation
    if (sa[i] && t[sa[i] - 1])
                                                             5.6
                                                             string mcp(string s) {
      sa[--x[s[sa[i] - 1]]] = sa[i] - 1;
                                                               int n = SZ(s), i = 0, j = 1;
                                                               s += s;
    fill_n(c, z, 0);
                                                               while (i < n && j < n) {
    for (int i = 0; i < n; i++)
                                                                 int k = 0;
                                                                 while (k < n \&\& s[i + k] == s[j + k])
      uniq \&= ++c[s[i]] < 2;
    partial_sum(c, c + z, c);
    if (uniq) {
                                                                 if (s[i + k] \leftarrow s[j + k])
      for (int i = 0; i < n; i++)</pre>
                                                                   j += k + 1;
        sa[--c[s[i]]] = i;
                                                                 else
                                                                   i += k + 1;
      return;
                                                                 if (i == j)
    for (int i = n - 2; i >= 0; i--)
                                                                   ++j;
      t[i] = (s[i] == s[i + 1] ? t[i + 1] : s[i] < s[i]
          + 1]);
                                                               int ans = i < n ? i : j;</pre>
    MAGIC(for (int i = 1; i <= n - 1; i++) if (t[i] &&
                                                               return s.substr(ans, n);
        !t[i - 1])
              sa[--x[s[i]]] = p[q[i] = nn++] = i);
    for (int i = 0; i < n; i++)</pre>
                                                                    De Bruijn sequence*
                                                             5.7
      if (sa[i] && t[sa[i]] && !t[sa[i] - 1]) {
                                                             constexpr int MAXC = 10, MAXN = 1e5 + 10;
        neq = (1st < 0) ||
              !equal(s + lst, s + lst + p[q[sa[i]] + 1]
                                                             struct DBSeq {
                    - sa[i], s + sa[i]);
                                                               int C, N, K, L, buf[MAXC * MAXN]; // K <= C^N</pre>
                                                               void dfs(int *out, int t, int p, int &ptr) {
        ns[q[lst = sa[i]]] = nmxz += neq;
                                                                 if (ptr >= L)
    sais(ns, nsa, p + nn, q + n, t + n, c + z, nn, nmxz
                                                                   return;
                                                                 if (t > N) {
         + 1);
    MAGIC(for (int i = nn - 1; i \ge 0; i--) sa[--x[s[p[
                                                                   if (N % p)
        nsa[i]]]] = p[nsa[i]]);
                                                                     return:
  }
                                                                   for (int i = 1; i <= p && ptr < L; ++i)</pre>
} sa;
                                                                      out[ptr++] = buf[i];
                                                                 } else {
      Aho-Corasick Automatan
                                                                   buf[t] = buf[t - p], dfs(out, t + 1, p, ptr);
                                                                   for (int j = buf[t - p] + 1; j < C; ++j)
const int len = 400000, sigma = 26;
                                                                     buf[t] = j, dfs(out, t + 1, t, ptr);
struct AC_Automatan {
  int nx[len][sigma], fl[len], cnt[len], pri[len], top;
  int newnode() {
                                                               void solve(int _c, int _n, int _k, int *out) {
    fill(nx[top], nx[top] + sigma, -1);
                                                                 int p = 0;
                                                                 C = _c, N = _n, K = _k, L = N + K - 1;
dfs(out, 1, 1, p);
    return top++;
  void init() { top = 1, newnode(); }
                                                                 if (p < L)
                                                                   fill(out + p, out + L, 0);
 int input(string &s) { // return the end_node of
      string
                                                             } dbs;
    int X = 1;
    for (char c : s) {
  if (!~nx[X][c - 'a'])
    nx[X][c - 'a'] = newnode();
  X = nx[X][c - 'a'];
                                                             5.8 SAM
                                                             const int MAXM = 1000010;
    }
                                                             struct SAM {
                                                               int tot, root, lst, mom[MAXM], mx[MAXM];
    return X;
                                                               int acc[MAXM], nxt[MAXM][33];
  void make_fl() {
                                                               int newNode() {
    queue<int> q;
                                                                 int res = ++tot;
    q.push(1), fl[1] = 0;
                                                                 fill(nxt[res], nxt[res] + 33, 0);
    for (int t = 0; !q.empty();) {
                                                                 mom[res] = mx[res] = acc[res] = 0;
      int R = q.front();
                                                                 return res;
      q.pop(), pri[t++] = R;
      for (int i = 0; i < sigma; ++i)</pre>
                                                               void init() {
        if (~nx[R][i]) {
                                                                 tot = 0;
          int X = nx[R][i], Z = fl[R];
                                                                 root = newNode();
          for (; Z && !~nx[Z][i];)
                                                                 mom[root] = 0, mx[root] = 0;
            Z = f1[Z];
                                                                 lst = root;
          fl[X] = Z ? nx[Z][i] : 1, q.push(X);
                                                               void push(int c) {
```

int p = lst;

int np = newNode();

mx[np] = mx[p] + 1;

nxt[p][c] = np;

for (; p && nxt[p][c] == 0; p = mom[p])

}

void get_v(string &s) {

fill(cnt, cnt + top, 0);

int X = 1;

}

```
if (p == 0)
                                                             #define LU 1
      mom[np] = root;
                                                             #define U 2
                                                             const int mov[3][2] = \{0, -1, -1, -1, -1, 0\};
      int q = nxt[p][c];
                                                             int al, bl;
                                                             char a[MAXL * 2], b[MAXL * 2]; // 0-indexed
      if (mx[p] + 1 == mx[q])
        mom[np] = q;
                                                             int dp[MAXL * 2][MAXL];
      else {
                                                             char pred[MAXL * 2][MAXL];
                                                             inline int lcs_length(int r) {
        int nq = newNode();
                                                               int i = r + al, j = bl, l = 0;
        mx[nq] = mx[p] + 1;
        for (int i = 0; i < 33; i++)
                                                               while (i > r) {
          nxt[nq][i] = nxt[q][i];
                                                                 char dir = pred[i][j];
                                                                 if (dir == LU)
        mom[nq] = mom[q];
        mom[q] = nq;
                                                                   1++;
        mom[np] = nq;
for (; p && nxt[p][c] == q; p = mom[p])
                                                                 i += mov[dir][0];
                                                                 j += mov[dir][1];
          nxt[p][c] = nq;
      }
                                                               return 1:
                                                             inline void reroot(int r) { // r = new base row
    lst = np;
  }
                                                               int i = r, j = 1;
  void push(char *str) {
                                                               while (j \le bl \&\& pred[i][j] != LU)
    for (int i = 0; str[i]; i++)
                                                                 j++;
      push(str[i] - 'a' + 1);
                                                               if (j > b1)
  }
                                                                 return;
                                                               pred[i][j] = L;
} sam;
                                                               while (i < 2 * al && j <= bl) {
5.9 PalTree
                                                                 if (pred[i + 1][j] == U) {
struct palindromic_tree { // Check by APIO 2014
                                                                   pred[i][j] = L;
                                                                 } else if (j < bl && pred[i + 1][j + 1] == LU) {
                           // palindrome
  struct node {
                                                                   i++;
    int next[26], fail, len;
                                                                    j++;
    int cnt, num; // cnt: appear times, num: number of
                                                                   pred[i][j] = L;
                   // pal. suf.
                                                                 } else {
    node(int 1 = 0) : fail(0), len(1), cnt(0), num(0) {
                                                                   j++;
      for (int i = 0; i < 26; ++i)
        next[i] = 0;
                                                               }
    }
  };
                                                             int cyclic_lcs() {
                                                               // a, b, al, bl should be properly filled
  vector<node> St;
  vector<char> s;
                                                               // note: a WILL be altered in process
  int last, n;
                                                                          -- concatenated after itself
  palindromic_tree() : St(2), last(1), n(0) {
                                                               char tmp[MAXL];
    St[0].fail = 1, St[1].len = -1, s.pb(-1);
                                                               if (al > bl) {
                                                                 swap(al, bl);
  inline void clear() {
                                                                 strcpy(tmp, a);
    St.clear(), s.clear(), last = 1, n = 0;
                                                                 strcpy(a, b);
    St.pb(0), St.pb(-1);
                                                                 strcpy(b, tmp);
    St[0].fail = 1, s.pb(-1);
                                                               strcpy(tmp, a);
  inline int get_fail(int x) {
                                                               strcat(a, tmp);
    while (s[n - St[x].len - 1] != s[n])
                                                               // basic lcs
      x = St[x].fail;
                                                               for (int i = 0; i <= 2 * al; i++) {
                                                                 dp[i][0] = 0;
    return x;
                                                                 pred[i][0] = U;
  inline void add(int c) {
   s.push_back(c -= 'a'), ++n;
                                                               for (int j = 0; j <= bl; j++) {</pre>
    int cur = get_fail(last);
                                                                 dp[0][j] = 0;
                                                                 pred[0][j] = L;
    if (!St[cur].next[c]) {
      int now = SZ(St);
      St.pb(St[cur].len + 2);
                                                               for (int i = 1; i <= 2 * al; i++) {
                                                                 for (int j = 1; j <= bl; j++) {
  if (a[i - 1] == b[j - 1])</pre>
      St[now].fail = St[get_fail(St[cur].fail)].next[c
                                                                      dp[i][j] = dp[i - 1][j - 1] + 1;
      St[cur].next[c] = now;
      St[now].num = St[St[now].fail].num + 1;
                                                                    else
                                                                     dp[i][j] = max(dp[i - 1][j], dp[i][j - 1]);
    last = St[cur].next[c], ++St[last].cnt;
                                                                    if (dp[i][j - 1] == dp[i][j])
                                                                   pred[i][j] = L;
else if (a[i - 1] == b[j - 1])
  inline void count() { // counting cnt
    auto i = St.rbegin();
                                                                     pred[i][j] = LU;
    for (; i != St.rend(); ++i) {
                                                                   else
      St[i->fail].cnt += i->cnt;
                                                                     pred[i][j] = U;
                                                                 }
                                                               // do cyclic lcs
  inline int size() { // The number of diff. pal.
    return SZ(St) - 2;
                                                               int clcs = 0;
                                                               for (int i = 0; i < al; i++) {
};
                                                                 clcs = max(clcs, lcs_length(i));
                                                                 reroot(i + 1);
       cyclicLCS
5.10
                                                               // recover a
```

a[al] = '\0';

|#define L 0

```
while (size() && !back())
  return clcs:
                                                                    pop_back();
                                                                  if (empty())
                                                                    negative = 0;
    Math
6
6.1 ax+by=gcd*
                                                                void carry(int _base = base) {
                                                                  for (size_t i = 0; i < size(); ++i) {</pre>
                                                                    if (at(i) >= 0 && at(i) < _base)</pre>
pll exgcd(ll a, ll b) {
                                                                      continue;
  if (b == 0)
    return pll(1, 0);
                                                                    if (i + 1u == size())
                                                                      push_back(0);
  else {
                                                                    int r = at(i) % _base;
    11 p = a / b;
                                                                    if (r < 0)
    pll q = exgcd(b, a % b);
    return pll(q.Y, q.X - q.Y * p);
                                                                      r += _base;
                                                                    at(i + \overline{1}) + \overline{at(i)} - r) / \underline{base}, at(i) = r;
}
                                                                int abscmp(const bigN &b) const {
6.2 floor and ceil
                                                                  if (size() > b.size())
                                                                    return 1;
int floor(int a, int b) { return a / b - (a % b && a <</pre>
    0 ^ b < 0); }
                                                                  if (size() < b.size())</pre>
int ceil(int a, int b) { return a / b + (a % b && a<0 ^</pre>
                                                                    return -1;
                                                                  for (int i = int(size()) - 1; i >= 0; --i) {
     b> 0); }
                                                                    if (at(i) > b[i])
6.3 Miller Rabin*
                                                                      return 1:
                                                                    if (at(i) < b[i])</pre>
// n < 4,759,123,141 3 : 2, 7, 61
// n < 1,122,004,669,633 4 : 2, 13, 23, 1662803
                                                                      return -1;
                                                                  }
// n < 3,474,749,660,383 6 : pirmes <= 13
                                                                  return 0;
// n < 2^64
// 2, 325, 9375, 28178, 450775, 9780504, 1795265022
                                                                int cmp(const bigN &b) const {
                                                                  if (negative != b.negative)
bool Miller_Rabin(ll a, ll n) {
  if ((a = a \% n) == 0)
                                                                    return negative ? -1 : 1;
                                                                  return negative ? -abscmp(b) : abscmp(b);
    return 1;
  if ((n & 1) ^ 1)
                                                                bool operator<(const bigN &b) const { return cmp(b) <</pre>
    return n == 2;
  11 \text{ tmp} = (n - 1) / ((n - 1) & (1 - n));
  11 t =
          _{lg}(((n - 1) & (1 - n))), x = 1;
                                                                bool operator>(const bigN &b) const { return cmp(b) >
                                                                     0; }
  for (; tmp; tmp >>= 1, a = mul(a, a, n))
    if (tmp & 1)
                                                                bool operator<=(const bigN &b) const { return cmp(b)</pre>
                                                                     <= 0; }
      x = mul(x, a, n);
  if (x == 1 || x == n - 1)
                                                                bool operator>=(const bigN &b) const { return cmp(b)
    return 1;
                                                                bool operator==(const bigN &b) const { return !cmp(b)
  while (--t)
    if ((x = mul(x, x, n)) == n - 1)
                                                                    ; }
                                                                bool operator!=(const bigN &b) const { return cmp(b)
      return 1:
                                                                    != 0; }
  return 0;
                                                                bigN abs() const {
                                                                  bigN res = *this;
6.4 Big number
                                                                  return res.negative = 0, res;
                                                                bigN operator-() const {
template <typename T> inline string to_string(const T &
                                                                  bigN res = *this;
    x) {
  stringstream ss;
                                                                  return res.negative = !negative, res.trim(), res;
  return ss << x, ss.str();</pre>
                                                                bigN operator+(const bigN &b) const {
                                                                  if (negative)
struct bigN : vector<ll> {
  const static int base = 1000000000, width = log10(
                                                                    return -(-(*this) + (-b));
                                                                  if (b.negative)
      base);
                                                                    return *this - (-b);
  bool negative;
  bigN(const_iterator a, const_iterator b) : vector<ll</pre>
                                                                  bigN res = *this;
       >(a, b) {}
                                                                  if (b.size() > size())
                                                                    res.resize(b.size());
  bigN(string s) {
                                                                  for (size_t i = 0; i < b.size(); ++i)</pre>
    if (s.empty())
      return;
                                                                    res[i] += b[i];
    if (s[0] == '-')
                                                                  return res.carry(), res.trim(), res;
      negative = 1, s = s.substr(1);
                                                                bigN operator-(const bigN &b) const {
    else
                                                                  if (negative)
      negative = 0;
    for (int i = int(s.size()) - 1; i >= 0; i -= width)
                                                                    return -(-(*this) - (-b));
                                                                  if (b.negative)
      11 t = 0;
                                                                    return *this + (-b);
      for (int j = max(0, i - width + 1); j <= i; ++j)
  t = t * 10 + s[j] - '0';</pre>
                                                                  if (abscmp(b) < 0)
                                                                    return -(b - (*this));
                                                                  bigN res = *this;
      push_back(t);
                                                                  if (b.size() > size())
                                                                    res.resize(b.size());
    trim();
                                                                  for (size_t i = 0; i < b.size(); ++i)</pre>
                                                                    res[i] -= b[i];
  template <typename T> bigN(const T &x) : bigN(
      to_string(x)) {}
                                                                  return res.carry(), res.trim(), res;
```

bigN operator*(const bigN &b) const {

bigN() : negative(0) {}

void trim() {

```
bigN res;
    res.negative = negative != b.negative;
    res.resize(size() + b.size());
    for (size_t i = 0; i < size(); ++i)</pre>
      for (size_t j = 0; j < b.size(); ++j)</pre>
        if ((res[i + j] += at(i) * b[j]) >= base) {
          res[i + j + 1] += res[i + j] / base;
           res[i + j] %= base;
        } // \Box \frac{1}{4}^{a} k  carry \cdot | \Box \cdot \cdot |
    return res.trim(), res;
  bigN operator/(const bigN &b) const {
    int norm = base / (b.back() + 1);
    bigN x = abs() * norm;
    bigN y = b.abs() * norm;
    bigN q, r;
    q.resize(x.size());
    for (int i = int(x.size()) - 1; i >= 0; --i) {
      r = r * base + x[i];
      int s1 = r.size() <= y.size() ? 0 : r[y.size()];</pre>
      int s2 = r.size() < y.size() ? 0 : r[y.size() -</pre>
          1];
      int d = (ll(base) * s1 + s2) / y.back();
      r = r - y * d;
      while (r.negative)
        r = r + y, --d;
      q[i] = d;
    }
    q.negative = negative != b.negative;
    return q.trim(), q;
  bigN operator%(const bigN &b) const { return *this -
      (*this / b) * b; }
  friend istream &operator>>(istream &ss, bigN &b) {
    string s;
    return ss >> s, b = s, ss;
  friend ostream &operator<<(ostream &ss, const bigN &b</pre>
      ) {
    if (b.negative)
      ss << '-';
    ss << (b.empty() ? 0 : b.back());</pre>
    for (int i = int(b.size()) - 2; i >= 0; --i)
      ss << setw(width) << setfill('0') << b[i];</pre>
    return ss;
  template <typename T> operator T() {
    stringstream ss;
    ss << *this;
    T res;
    return ss >> res, res;
  }
};
6.5 Fraction
```

```
struct fraction {
  11 n, d;
  fraction(const 11 \& n = 0, const 11 \& d = 1): n(n),
       d(_d) {
    11 t = __gcd(n, d);
n /= t, d /= t;
if (d < 0)</pre>
      n = -n, d = -d;
  fraction operator-() const { return fraction(-n, d);
  fraction operator+(const fraction &b) const {
    return fraction(n * b.d + b.n * d, d * b.d);
  fraction operator-(const fraction &b) const {
   return fraction(n * b.d - b.n * d, d * b.d);
  fraction operator*(const fraction &b) const {
    return fraction(n * b.n, d * b.d);
  fraction operator/(const fraction &b) const {
    return fraction(n * b.d, d * b.n);
  void print() {
    cout << n;
    if (d != 1)
```

```
cout << "/" << d;
};
```

6.6 Simultaneous Equations

```
struct matrix { // m variables, n equations
  int n, m;
  fraction M[MAXN][MAXN + 1], sol[MAXN];
  int solve() { //-1: inconsistent, >= 0: rank
    for (int i = 0; i < n; ++i) {</pre>
      int piv = 0;
      while (piv < m && !M[i][piv].n)
        ++piv;
      if (piv == m)
        continue;
      for (int j = 0; j < n; ++j) {
        if (i == j)
          continue;
        fraction tmp = -M[j][piv] / M[i][piv];
        for (int k = 0; k <= m; ++k)
          M[j][k] = tmp * M[i][k] + M[j][k];
      }
    int rank = 0;
    for (int i = 0; i < n; ++i) {
      int piv = 0;
      while (piv < m && !M[i][piv].n)</pre>
        ++piv;
      if (piv == m && M[i][m].n)
        return -1;
      else if (piv < m)</pre>
        ++rank, sol[piv] = M[i][m] / M[i][piv];
    return rank;
  }
};
```

6.7 Pollard Rho

6.8 Simplex Algorithm

```
const int MAXN = 111;
const int MAXM = 111;
const double eps = 1E-10;
double a[MAXN][MAXM], b[MAXN], c[MAXM], d[MAXN][MAXM];
double x[MAXM];
int ix[MAXN + MAXM]; // !!! array all indexed from 0
// max{cx} subject to {Ax<=b,x>=0}
// n: constraints, m: vars !!!
// x[] is the optimal solution vector
// usage :
// value = simplex(a, b, c, N, M);
double simplex(double a[MAXN][MAXM], double b[MAXN],
    double c[MAXM], int n,
  ++m;
  int r = n, s = m - 1;
  memset(d, 0, sizeof(d));
  for (int i = 0; i < n + m; ++i)</pre>
    ix[i] = i;
  for (int i = 0; i < n; ++i) {
    for (int j = 0; j < m - 1; ++j)
      d[i][j] = -a[i][j];
    d[i][m - 1] = 1;
    d[i][m] = b[i];
```

```
if (d[r][m] > d[i][m])
                                                                            for (int i = 0; i < SZ(a); ++i)
         r = i;
                                                                              res[i] = b[a[i]];
                                                                            return res:
    for (int j = 0; j < m - 1; ++j)
                                                                         }
       d[n][j] = c[j];
                                                                         vector<int> inv(const vector<int> &a) {
    d[n + 1][m - 1] = -1;
                                                                            vector<int> res(SZ(a));
    for (double dd;;) {
                                                                            for (int i = 0; i < SZ(a); ++i)
       if (r < n) {
                                                                              res[a[i]] = i;
         int t = ix[s];
                                                                            return res:
         ix[s] = ix[r + m];
         ix[r + m] = t;
                                                                          int filter(const vector<int> &g, bool add = true) {
         d[r][s] = 1.0 / d[r][s];
                                                                            n = SZ(bkts);
         for (int j = 0; j <= m; ++j)
                                                                            vector<int> p = g;
           if (j != s)
                                                                            for (int i = 0; i < n; ++i) {
                                                                              assert(p[i] >= 0 && p[i] < SZ(lk[i]));
              d[r][j] *= -d[r][s];
         for (int i = 0; i <= n + 1; ++i)
                                                                               if (lk[i][p[i]] == -1) {
           if (i != r) {
                                                                                 if (add) {
              for (int j = 0; j <= m; ++j)
                                                                                    bkts[i].pb(p);
                 if (j != s)
                                                                                    binv[i].pb(inv(p));
                   d[i][j] += d[r][j] * d[i][s];
                                                                                   lk[i][p[i]] = SZ(bkts[i]) - 1;
              d[i][s] *= d[r][s];
                                                                                 return i;
       }
       r = -1;
                                                                              p = p * binv[i][lk[i][p[i]]];
       s = -1;
       for (int j = 0; j < m; ++j)</pre>
                                                                            return -1;
         if (s < 0 \mid | ix[s] > ix[j]) {
           if (d[n + 1][j] > eps || (d[n + 1][j] > -eps &&
                                                                          bool inside(const vector<int> &g) { return filter(g,
                  d[n][j] > eps))
                                                                               false) == -1; }
                                                                          void solve(const vector<vector<int>> &gen, int _n) {
       if (s < 0)
                                                                            bkts.clear(), bkts.resize(n);
                                                                            binv.clear(), binv.resize(n);
lk.clear(), lk.resize(n);
         break;
       for (int i = 0; i < n; ++i)
         if (d[i][s] < -eps) {</pre>
                                                                            vector<int> iden(n);
           if (r < 0 \mid | (dd = d[r][m] / d[r][s] - d[i][m]
                                                                            iota(iden.begin(), iden.end(), 0);
                 / d[i][s]) < -eps ||
                                                                            for (int i = 0; i < n; ++i) {
                 (dd < eps && ix[r + m] > ix[i + m]))
                                                                               lk[i].resize(n, -1);
                                                                               bkts[i].pb(iden);
                                                                               binv[i].pb(iden);
       if(r < 0)
                                                                               lk[i][i] = 0;
         return -1; // not bounded
                                                                            for (int i = 0; i < SZ(gen); ++i)</pre>
    if (d[n + 1][m] < -eps)</pre>
                                                                              filter(gen[i]);
       return -1; // not executable
                                                                            queue<pair<pii, pii>> upd;
    double ans = 0;
                                                                            for (int i = 0; i < n; ++i)
                                                                               for (int j = i; j < n; ++j)
    for (int i = 0; i < m; i++)</pre>
      x[i] = 0;
                                                                                 for (int k = 0; k < SZ(bkts[i]); ++k)</pre>
                                                                                    for (int 1 = 0; 1 < SZ(bkts[j]); ++1)</pre>
    for (int i = m; i < n + m; ++i) { // the missing
         enumerated x[i] = 0
                                                                                      upd.emplace(pii(i, k), pii(j, l));
                                                                            while (!upd.empty()) {
       if (ix[i] < m - 1) {</pre>
         ans += d[i - m][m] * c[ix[i]];
                                                                              auto a = upd.front().X;
                                                                               auto b = upd.front().Y;
         x[ix[i]] = d[i - m][m];
      }
                                                                               upd.pop();
    }
                                                                               int res = filter(bkts[a.X][a.Y] * bkts[b.X][b.Y]);
                                                                               if (res == -1)
    return ans;
 }
                                                                                 continue;
                                                                               pii pr = pii(res, SZ(bkts[res]) - 1);
 6.8.1 Construction
                                                                               for (int i = 0; i < n; ++i)
 Standard form: maximize \mathbf{c}^T\mathbf{x} subject to A\mathbf{x} \leq \mathbf{b} and \mathbf{x} \geq 0. Dual LP: minimize \mathbf{b}^T\mathbf{y} subject to A^T\mathbf{y} \geq \mathbf{c} and \mathbf{y} \geq 0. \bar{\mathbf{x}} and \bar{\mathbf{y}} are optimal if and only if for all i \in [1,n], either \bar{x}_i = 0 and \bar{\mathbf{x}}_i = 0.
                                                                                 for (int j = 0; j < SZ(bkts[i]); ++j) {</pre>
                                                                                    if (i <= res)
                                                                                      upd.emplace(pii(i, j), pr);
        \sum_{i=1}^{n}A_{ji}ar{y}_{j}=c_{i} holds and for all i\in[1,m] either ar{y}_{i}=0 or
                                                                                    if (res <= i)
 \sum_{j=1}^{n} A_{ij} \bar{x}_j = b_j holds.
                                                                                      upd.emplace(pr, pii(i, j));
                                                                                 }
1.In case of minimization, let c_i^\prime = -c_i
                                                                            }
2.\sum_{1\leq i\leq n} A_{ji}x_i \geq b_j \rightarrow \sum_{1\leq i\leq n} -A_{ji}x_i \leq -b_j
3. \sum_{1 \leq i \leq n} A_{ji} x_i = b_j
                                                                          long long size() {
 \begin{array}{l} \bullet \sum_{1 \leq i \leq n} A_{ji} x_i \leq b_j \\ \bullet \sum_{1 \leq i \leq n} A_{ji} x_i \geq b_j \end{array}
                                                                            long long res = 1;
                                                                            for (int i = 0; i < n; ++i)
                                                                              res = res * SZ(bkts[i]);
4.If x_i has no lower bound, replace x_i with x_i - x_i'
                                                                            return res;
  6.9 Schreier-Sims Algorithm*
                                                                         } // namespace schreier
                                                                          6.10 chineseRemainder
  namespace schreier {
  vector<vector<int>>> bkts, binv;
                                                                         LL solve(LL x1, LL m1, LL x2, LL m2) {
```

LL g = $_gcd(m1, m2)$;

return -1; // no sol

if ((x2 - x1) % g)

m1 /= g;

vector<vector<int>> lk;

vector<int> &b) {

vector<int> res(SZ(a));

vector<int> operator*(const vector<int> &a, const

```
m2 /= g;
pair<LL, LL> p = gcd(m1, m2);
LL lcm = m1 * m2 * g;
LL res = p.first * (x2 - x1) * m1 + x1;
return (res % lcm + lcm) % lcm;
}
```

6.11 QuadraticResidue

```
int Jacobi(int a, int m) {
  int s = 1;
  for (; m > 1;) {
    a %= m;
    if (a == 0)
     return 0;
    const int r = __builtin_ctz(a);
    if ((r & 1) && ((m + 2) & 4))
     s = -s;
    a >>= r;
   if (a & m & 2)
     s = -s;
    swap(a, m);
  }
  return s;
}
int QuadraticResidue(int a, int p) {
 if (p == 2)
   return a & 1;
  const int jc = Jacobi(a, p);
 if (jc == 0)
    return 0;
  if (jc == -1)
   return -1;
  int b, d;
  for (;;) {
   b = rand() % p;
    d = (1LL * b * b + p - a) \% p;
    if (Jacobi(d, p) == -1)
      break;
  }
  int f0 = b, f1 = 1, g0 = 1, g1 = 0, tmp;
  for (int e = (1LL + p) >> 1; e; e >>= 1) {
    if (e & 1) {
      tmp = (1LL * g0 * f0 + 1LL * d * (1LL * g1 * f1 %
          p)) % p;
      g1 = (1LL * g0 * f1 + 1LL * g1 * f0) % p;
      g0 = tmp;
    tmp = (1LL * f0 * f0 + 1LL * d * (1LL * f1 * f1 % p
       )) % p;
    f1 = (2LL * f0 * f1) % p;
    f0 = tmp;
  return g0;
```

6.12 Discrete Log

```
int DiscreteLog(int s, int x, int y, int m) {
  constexpr int kStep = 32000;
  unordered_map<int, int> p;
  int b = 1;
  for (int i = 0; i < kStep; ++i) {</pre>
   p[y] = i;
y = 1LL * y * x % m;
    b = 1LL * b * x % m;
  for (int i = 0; i < m + 10; i += kStep) {
   s = 1LL * s * b % m;</pre>
    if (p.find(s) != p.end())
      return i + kStep - p[s];
 }
  return -1;
int DiscreteLog(int x, int y, int m) {
  if (m == 1)
    return 0;
  int s = 1;
  for (int i = 0; i < 100; ++i) {
    if (s == y)
      return i;
```

```
s = 1LL * s * x % m;
}
if (s == y)
    return 100;
int p = 100 + DiscreteLog(s, x, y, m);
if (fpow(x, p, m) != y)
    return -1;
return p;
}
```

6.13 PiCount

```
int64_t PrimeCount(int64_t n) {
 if (n <= 1)
   return 0;
  const int v = sqrt(n);
  vector<int> smalls(v + 1);
  for (int i = 2; i <= v; ++i)
    smalls[i] = (i + 1) / 2;
  int s = (v + 1) / 2;
  vector<int> roughs(s);
  for (int i = 0; i < s; ++i)
    roughs[i] = 2 * i + 1;
  vector<int64_t> larges(s);
  for (int i = 0; i < s; ++i)
larges[i] = (n / (2 * i + 1) + 1) / 2;
  vector<bool> skip(v + 1);
  int pc = 0;
  for (int p = 3; p <= v; ++p) {
    if (smalls[p] > smalls[p - 1]) {
      int q = p * p;
      pc++;
      if (1LL * q * q > n)
        break;
      skip[p] = true;
      for (int i = q; i <= v; i += 2 * p)
        skip[i] = true;
      int ns = 0;
      for (int k = 0; k < s; ++k) {
        int i = roughs[k];
        if (skip[i])
          continue;
        int64_t d = 1LL * i * p;
        larges[ns] =
            larges[k] - (d <= v ? larges[smalls[d] - pc</pre>
                ] : smalls[n / d]) + pc;
        roughs[ns++] = i;
      s = ns;
      for (int j = v / p; j >= p; --j) {
        int c = smalls[j] - pc;
        for (int i = j * p, e = min(i + p, v + 1); i < p
            e; ++i)
          smalls[i] -= c;
      }
  for (int k = 1; k < s; ++k) {
    const int64_t m = n / roughs[k];
    int64_t = larges[k] - (pc + k - 1);
    for (int l = 1; l < k; ++1) {
      int p = roughs[1];
      if (1LL * p * p > m)
        break;
      s -= smalls[m / p] - (pc + l - 1);
    larges[0] -= s;
  }
  return larges[0];
```

6.14 Primes

```
/*
12721 13331 14341 75577 123457 222557 556679 999983
1097774749 1076767633
100102021 999997771 1001010013 1000512343 987654361
999991231 999888733
98789101 987777733 999991921 1010101333 1010102101
1000000000039
100000000000037 2305843009213693951
4611686018427387847 9223372036854775783
```

18446744073709551557 */

6.15 Theorem

6.15.1 Kirchhoff's Theorem

Denote L be a $n\times n$ matrix as the Laplacian matrix of graph G, where $L_{ii}=d(i)$, $L_{ij}=-c$ where c is the number of edge (i,j) in G.

- •The number of undirected spanning in G is $|\det(\tilde{L}_{11})|$.
- •The number of directed spanning tree rooted at r in G is $|\det(\tilde{L}_{rr})|$.

6.15.2 Tutte's Matrix

Let D be a $n \times n$ matrix, where $d_{ij} = x_{ij}$ $(x_{ij}$ is chosen uniformly at random) if i < j and $(i,j) \in E$, otherwise $d_{ij} = -d_{ji}$. $\frac{rank(D)}{2}$ is the maximum matching on G.

6.15.3 Cayley's Formula

- •Given a degree sequence d_1,d_2,\ldots,d_n for each labeled vertices, there are $\frac{(n-2)!}{(d_1-1)!(d_2-1)!\cdots(d_n-1)!}$ spanning trees.
- •Let $T_{n,k}$ be the number of labeled forests on n vertices with k components, such that vertex $1,2,\ldots,k$ belong to different components. Then $T_{n,k}=kn^{n-k-1}$.

6.15.4 Erdős-Gallai theorem

A sequence of nonnegative integers $d_1 \ge \cdots \ge d_n$ can be represented as the degree sequence of a finite simple graph on n vertices if and only

if $d_1+\cdots+d_n$ is even and $\sum_{i=1}^\kappa d_i \le k(k-1)+\sum_{i=k+1}^n \min(d_i,k)$ holds for every $1\le k\le n$.

6.15.5 Gale-Ryser theorem

A pair of sequences of nonnegative integers $a_1 \geq \cdots \geq a_n$ and b_1, \ldots, b_n is bigraphic if and only if $\sum_{i=1}^n a_i = \sum_{i=1}^n b_i$ and $\sum_{i=1}^k a_i \leq \sum_{i=1}^n \min(b_i,k)$ holds for every $1 \leq k \leq n$.

6.15.6 Fulkerson-Chen-Anstee theorem

A sequence $(a_1,b_1),\ldots,(a_n,b_n)$ of nonnegative integer pairs with $a_1\geq\cdots\geq a_n$ is digraphic if and only if $\sum_{i=1}^n a_i=\sum_{i=1}^n b_i$ and $\sum_{i=1}^k a_i\leq\cdots\geq a_n$

$$\sum_{i=1}^k \min(b_i,k-1) + \sum_{i=k+1}^n \min(b_i,k) \text{ holds for every } 1 \leq k \leq n.$$

6.15.7 Pick's theorem

給定頂點座標均是整點(或正方形格子點)的簡單多邊形,皮克定理說明了其面積A和內部格點數目i、邊上格點數目b的關係: $A=i+\frac{b}{2}-1$

6.16 Euclidean Algorithms

- $\bullet m = \lfloor \frac{an+b}{a} \rfloor$
- •Time complexity: $O(\log n)$

$$\begin{split} f(a,b,c,n) &= \sum_{i=0}^n \lfloor \frac{ai+b}{c} \rfloor \\ &= \begin{cases} \lfloor \frac{a}{c} \rfloor \cdot \frac{n(n+1)}{2} + \lfloor \frac{b}{c} \rfloor \cdot (n+1) \\ +f(a \text{ mod } c,b \text{ mod } c,c,n), & a \geq c \vee b \geq c \\ 0, & n < 0 \vee a = 0 \\ nm - f(c,c-b-1,a,m-1), & \text{otherwise} \end{cases} \end{split}$$

$$\begin{split} g(a,b,c,n) &= \sum_{i=0}^n i \lfloor \frac{ai+b}{c} \rfloor \\ &= \begin{cases} \lfloor \frac{a}{c} \rfloor \cdot \frac{n(n+1)(2n+1)}{6} + \lfloor \frac{b}{c} \rfloor \cdot \frac{n(n+1)}{2} \\ +g(a \bmod c, b \bmod c, c, n), & a \geq c \lor b \geq c \\ 0, & n < 0 \lor a = 0 \\ \frac{1}{2} \cdot (n(n+1)m - f(c, c - b - 1, a, m - 1) \\ -h(c, c - b - 1, a, m - 1)), & \text{otherwise} \end{cases} \end{split}$$

$$\begin{split} h(a,b,c,n) &= \sum_{i=0}^n \lfloor \frac{ai+b}{c} \rfloor^2 \\ &= \begin{cases} \lfloor \frac{a}{c} \rfloor^2 \cdot \frac{n(n+1)(2n+1)}{6} + \lfloor \frac{b}{c} \rfloor^2 \cdot (n+1) \\ + \lfloor \frac{a}{c} \rfloor \cdot \lfloor \frac{b}{c} \rfloor \cdot n(n+1) \\ + h(a \bmod c, b \bmod c, c, n) \\ + 2 \lfloor \frac{a}{c} \rfloor \cdot g(a \bmod c, b \bmod c, c, n) \\ + 2 \lfloor \frac{b}{c} \rfloor \cdot f(a \bmod c, b \bmod c, c, n), & a \geq c \lor b \geq c \\ 0, & n < 0 \lor a = 0 \\ nm(m+1) - 2g(c, c-b-1, a, m-1) \\ - 2f(c, c-b-1, a, m-1) - f(a, b, c, n), & \text{otherwise} \end{cases} \end{split}$$

7 Polynomial

7.1 Fast Fourier Transform

7.2 Number Theory Transform

```
//(2^16)+1, 65537, 3
// 7*17*(2^23)+1, 998244353, 3
// 1255*(2^20)+1, 1315962881, 3
// 51*(2^25)+1, 1711276033, 29
template <int MAXN, LL P, LL RT> // MAXN must be 2^k
struct NTT {
  LL w[MAXN];
  LL mpow(LL a, LL n);
  LL minv(LL a) { return mpow(a, P - 2); }
  NTT() {
    LL dw = mpow(RT, (P - 1) / MAXN);
     for (int i = 1; i < MAXN; ++i)</pre>
       w[i] = w[i - 1] * dw % P;
  void bitrev(LL *a, int n) {
    int i = 0;
for (int j = 1; j < n - 1; ++j) {
       for (int k = n \gg 1; (i ^{\circ} = k) \langle k; k \gg 1 \rangle
       if (j < i)</pre>
         swap(a[i], a[j]);
  void operator()(LL *a, int n, bool inv = false) { //
       0 \leftarrow a[i] \leftarrow P
     bitrev(a, n);
     for (int L = 2; L <= n; L <<= 1) {
       int dx = MAXN / L, dl = L >> 1;
       for (int i = 0; i < n; i += L) {
         for (int j = i, x = 0; j < i + dl; ++j, x += dx
           LL tmp = a[j + dl] * w[x] % P;
           if ((a[j + dl] = a[j] - tmp) < 0)
             a[j + dl] += P;
            if ((a[j] += tmp) >= P)
              a[j] -= P;
         }
      }
     if (inv) {
       reverse(a + 1, a + n);
       LL invn = minv(n);
       for (int i = 0; i < n; ++i)
  a[i] = a[i] * invn % P;</pre>
};
```

7.3 Fast Walsh Transform*

```
/* x: a[j], y: a[j + (L >> 1)]
or: (y += x * op), and: (x += y * op)
xor: (x, y = (x + y) * op, (x - y) * op)
invop: or, and, xor = -1, -1, 1/2 */
void fwt(int *a, int n, int op) { // or
  for (int L = 2; L <= n; L <<= 1)
    for (int i = 0; i < n; i += L)
    for (int j = i; j < i + (L >> 1); ++j)
```

```
a[j + (L >> 1)] += a[j] * op;
const int N = 21;
int f[N][1 << N], g[N][1 << N], h[N][1 << N], ct[1 << N
    ];
void subset_convolution(int *a, int *b, int *c, int L)
  // c_k = \sum_{i = 0} a_i * b_j
 int n = 1 \ll L;
  for (int i = 1; i < n; ++i)
   ct[i] = ct[i & (i - 1)] + 1;
  for (int i = 0; i < n; ++i)
   f[ct[i]][i] = a[i], g[ct[i]][i] = b[i];
 for (int i = 0; i <= L; ++i)
  fwt(f[i], n, 1), fwt(g[i], n, 1);</pre>
  for (int i = 0; i <= L; ++i)
   for (int j = 0; j <= i; ++j)
      for (int x = 0; x < n; ++x)
        h[i][x] += f[j][x] * g[i - j][x];
 for (int i = 0; i <= L; ++i)
   fwt(h[i], n, -1);
  for (int i = 0; i < n; ++i)
   c[i] = h[ct[i]][i];
```

7.4 Newton's Method

Given F(x) where

$$F(x) = \sum_{i=0}^{\infty} \alpha_i (x - \beta)^i$$

for β being some constant. Polynomial P such that F(P)=0 can be found iteratively. Denote by Q_k the polynomial such that $F(Q_k)=0$ (mod ${x^2}^k$), then

$$Q_{k+1} = Q_k - \frac{F(Q_k)}{F'(Q_k)} \pmod{x^{2^{k+1}}}$$

8 Geometry

8.1 Default Code

```
typedef pair<double, double> pdd;
typedef pair<pdd, pdd> Line;
struct Cir {
 pdd 0;
 double R;
const double eps = 1e-8;
pdd operator+(const pdd &a, const pdd &b) { return pdd(
    a.X + b.X, a.Y + b.Y); }
pdd operator-(const pdd &a, const pdd &b) { return pdd(
    a.X - b.X, a.Y - b.Y); }
pdd operator*(const pdd &a, const double &b) { return
    pdd(a.X * b, a.Y * b); }
pdd operator/(const pdd &a, const double &b) { return
    pdd(a.X / b, a.Y / b); }
double dot(const pdd &a, const pdd &b) { return a.X * b
    .X + a.Y * b.Y; }
double cross(const pdd &a, const pdd &b) { return a.X *
     b.Y - a.Y * b.X; }
double abs2(const pdd &a) { return dot(a, a); }
double abs(const pdd &a) { return sqrt(dot(a, a)); }
int sign(const double &a) { return fabs(a) < eps ? 0 :</pre>
    a > 0 ? 1 : -1; }
int ori(const pdd &a, const pdd &b, const pdd &c) {
 return sign(cross(b - a, c - a));
bool collinearity(const pdd &p1, const pdd &p2, const
  return fabs(cross(p1 - p3, p2 - p3)) < eps;</pre>
bool btw(const pdd &p1, const pdd &p2, const pdd &p3) {
 if (!collinearity(p1, p2, p3))
   return 0;
 return dot(p1 - p3, p2 - p3) < eps;</pre>
bool seg_intersect(const pdd &p1, const pdd &p2, const
    pdd &p3, const pdd &p4) {
  int a123 = ori(p1, p2, p3);
 int a124 = ori(p1, p2, p4);
 int a341 = ori(p3, p4, p1);
 int a342 = ori(p3, p4, p2);
```

8.2 Convex hull*

8.3 External bisector

```
pdd external_bisector(pdd p1, pdd p2, pdd p3) { // 213
  pdd L1 = p2 - p1, L2 = p3 - p1;
  L2 = L2 * abs(L1) / abs(L2);
  return L1 + L2;
}
```

8.4 Heart

```
pdd excenter(pdd p0, pdd p1, pdd p2, double &radius) {
  p1 = p1 - p0, p2 = p2 - p0;
  double x1 = p1.X, y1 = p1.Y, x2 = p2.X, y2 = p2.Y;
  double m = 2. * (x1 * y2 - y1 * x2);
  center.X = (x1 * x1 * y2 - x2 * x2 * y1 + y1 * y2 * (
      y1 - y2)) / m;
  center.Y = (x1 * x2 * (x2 - x1) - y1 * y1 * x2 + x1 *
       y2 * y2) / m;
  return radius = abs(center), center + p0;
}
pdd incenter(pdd p1, pdd p2, pdd p3, double &radius) {
  double a = abs(p2 - p1), b = abs(p3 - p1), c = abs(p3
       - p2);
  double s = (a + b + c) / 2, area = sqrt(s * (s - a) *
       (s - b) * (s - c);
  pdd L1 = external_bisector(p1, p2, p3), L2 =
      external_bisector(p2, p1, p3);
  return radius = area / s, intersect(p1, p1 + L1, p2,
      p2 + L2),
pdd escenter(pdd p1, pdd p2, pdd p3) { // 213
  pdd L1 = external_bisector(p1, p2, p3),
     L2 = external_bisector(p2, p2 + p2 - p1, p3);
  return intersect(p1, p1 + L1, p2, p2 + L2);
pdd barycenter(pdd p1, pdd p2, pdd p3) { return (p1 +
    p2 + p3) / 3; }
pdd orthocenter(pdd p1, pdd p2, pdd p3) {
  pdd L1 = p3 - p2, L2 = p3 - p1;
  swap(L1.X, L1.Y), L1.X *= -1;
  swap(L2, X, L2.Y), L2.X *= -1;
  return intersect(p1, p1 + L1, p2, p2 + L2);
```

8.5 Minimum Enclosing Circle*

```
pdd Minimum_Enclosing_Circle(vector<pdd> dots, double &
    r) {
  pdd cent:
  random_shuffle(ALL(dots));
  cent = dots[0], r = 0;
  for (int i = 1; i < SZ(dots); ++i)</pre>
    if (abs(dots[i] - cent) > r) {
      cent = dots[i], r = 0;
      for (int j = 0; j < i; ++j)
        if (abs(dots[j] - cent) > r) {
          cent = (dots[i] + dots[j]) / 2;
          r = abs(dots[i] - cent);
          for (int k = 0; k < j; ++k)
            if (abs(dots[k] - cent) > r)
              cent = excenter(dots[i], dots[j], dots[k
                   ], r);
        }
  return cent:
}
```

8.6 Polar Angle Sort*

```
pdd center; // sort base
int Quadrant(pdd a) {
  if (a.X > 0 && a.Y >= 0)
    return 1;
  if (a.X <= 0 && a.Y > 0)
    return 2;
  if (a.X < 0 && a.Y <= 0)
    return 3;
  if (a.X >= 0 && a.Y < 0)
   return 4:
bool cmp(pll a, pll b) {
  a = a - center, b = b - center;
  if (Quadrant(a) != Quadrant(b))
    return Quadrant(a) < Quadrant(b);</pre>
  if (cross(b, a) == 0)
    return abs2(a) < abs2(b);</pre>
 return cross(a, b) > 0;
bool cmp(pdd a, pdd b) {
  a = a - center, b = b - center;
  if (fabs(atan2(a.Y, a.X) - atan2(b.Y, b.X)) > eps)
    return atan2(a.Y, a.X) < atan2(b.Y, b.X);</pre>
  return abs(a) < abs(b);</pre>
```

8.7 Intersection of two circles*

8.8 Intersection of polygon and circle

```
// Divides into multiple triangle, and sum up
// test by HDU2892
const double PI = acos(-1);
double _area(pdd pa, pdd pb, double r) {
  if (abs(pa) < abs(pb))
    swap(pa, pb);
  if (abs(pb) < eps)
    return 0;
  double S, h, theta;
  double a = abs(pb), b = abs(pa), c = abs(pb - pa);
  double cosB = dot(pb, pb - pa) / a / c, B = acos(cosB
    );</pre>
```

```
double cosC = dot(pa, pb) / a / b, C = acos(cosC);
  if (a > r) {
  S = (C / 2) * r * r;
    h = a * b * sin(C) / c;
    if (h < r && B < PI / 2)
      S = (acos(h / r) * r * r - h * sqrt(r * r - h *
          h));
  } else if (b > r) {
    theta = PI - B - asin(sin(B) / r * a);
    S = .5 * a * r * sin(theta) + (C - theta) / 2 * r *
  } else
    S = .5 * sin(C) * a * b;
  return S;
double area_poly_circle(const vector<pdd> poly, const
    pdd &O, const double r) {
  double S = 0;
  for (int i = 0; i < SZ(poly); ++i)</pre>
    S += _area(poly[i] - 0, poly[(i + 1) % SZ(poly)] -
        0, r) '
         ori(0, poly[i], poly[(i + 1) % SZ(poly)]);
  return fabs(S);
}
```

8.9 Intersection of line and circle

8.10 point in circle

```
// return p4 is strictly in circumcircle of tri(p1,p2,
long long sqr(long long x) { return x * x; }
bool in_cc(const pll &p1, const pll &p2, const pll &p3,
      const pll &p4) {
  long long u11 = p1.X - p4.X;
  long long u12 = p1.Y - p4.Y;
  long long u21 = p2.X - p4.X;
  long long u22 = p2.Y - p4.Y;
  long long u31 = p3.X - p4.X;
  long long u32 = p3.Y - p4.Y;
  long long u13 = sqr(p1.X) - sqr(p4.X) + sqr(p1.Y) -
       sqr(p4.Y);
  long long u23 = sqr(p2.X) - sqr(p4.X) + sqr(p2.Y) -
      sqr(p4.Y);
  long long u33 = sqr(p3.X) - sqr(p4.X) + sqr(p3.Y) -
       sqr(p4.Y);
    _int128 det = (__int128)-u13 * u22 * u31 + (__int128
       )u12 * u23 * u31 +
                  (__int128)u13 * u21 * u32 - (__int128)
                      u11 * u23 * u32
                    _int128)u12 * u21 * u33 + (__int128)
                      u11 * u22 * u33;
  return det > eps;
}
```

8.11 Half plane intersection

```
bool isin(Line 10, Line 11, Line 12) {
    // Check inter(11, 12) in 10
    pdd p = intersect(11.X, 11.Y, 12.X, 12.Y);
    return cross(10.Y - 10.X, p - 10.X) > eps;
}

/* If no solution, check: 1. ret.size() < 3
    * Or more precisely, 2. interPnt(ret[0], ret[1])
    * in all the lines. (use (1.Y - 1.X) ^ (p - 1.X) > 0
    */
    /* --^- Line.X --^- Line.Y --^- */
vector<Line> halfPlaneInter(vector<Line> lines) {
    int sz = lines.size();
```

```
vector<double> ata(sz), ord(sz);
  for (int i = 0; i < sz; ++i) {
    ord[i] = i;
    pdd d = lines[i].Y - lines[i].X;
    ata[i] = atan2(d.Y, d.X);
  sort(ord.begin(), ord.end(), [&](int i, int j) {
    if (fabs(ata[i] - ata[j]) < eps)</pre>
      return (cross(lines[i].Y - lines[i].X, lines[j].Y
            - lines[i].X)) < 0;</pre>
    return ata[i] < ata[j];</pre>
  });
  vector<Line> fin;
  for (int i = 0; i < sz; ++i)
    if (!i || fabs(ata[ord[i]] - ata[ord[i - 1]]) > eps
      fin.pb(lines[ord[i]]);
  deque<Line> dq;
  for (int i = 0; i < SZ(fin); i++) {</pre>
    while (SZ(dq) \ge 2 \&\& !isin(fin[i], dq[SZ(dq) - 2],
          dq.back()))
       dq.pop_back();
    while (SZ(dq) \ge 2 \&\& !isin(fin[i], dq[0], dq[1]))
      dq.pop_front();
    dq.push_back(fin[i]);
  while (SZ(dq) >= 3 \&\& !isin(dq[0], dq[SZ(dq) - 2], dq
       .back()))
    dq.pop_back();
  while (SZ(dq) >= 3 \&\& !isin(dq.back(), dq[0], dq[1]))
    dq.pop_front();
  vector<Line> res(ALL(dq));
  return res:
}
```

8.12 CircleCover*

```
const int N = 1021;
struct CircleCover {
 int C;
 Cir c[N];
 bool g[N][N], overlap[N][N];
  // Area[i] : area covered by at least i circles
  double Area[N];
  void init(int _C) { C = _C; }
 struct Teve {
   pdd p;
    double ang;
    int add:
    Teve() {}
    Teve(pdd _a, double _b, int _c) : p(_a), ang(_b),
        add(_c) {}
    bool operator<(const Teve &a) const { return ang <
        a.ang; }
 } eve[N * 2];
  // strict: x = 0, otherwise x = -1
 bool disjuct(Cir &a, Cir &b, int x) {
   return sign(abs(a.0 - b.0) - a.R - b.R) > x;
 bool contain(Cir &a, Cir &b, int x) {
    return sign(a.R - b.R - abs(a.0 - b.0)) > x;
 bool contain(int i, int j) {
   /* c[j] is non-strictly in c[i]. */
    return (sign(c[i].R - c[j].R) > 0 ||
(sign(c[i].R - c[j].R) == 0 && i < j)) &&
           contain(c[i], c[j], -1);
  void solve() {
    fill_n(Area, C + 2, 0);
    for (int i = 0; i < C; ++i)
      for (int j = 0; j < C; ++j)
       overlap[i][j] = contain(i, j);
    for (int i = 0; i < C; ++i)
      for (int j = 0; j < C; ++j)
        g[i][j] = !(overlap[i][j] || overlap[j][i] ||
            disjuct(c[i], c[j], -1));
    for (int i = 0; i < C; ++i) {
      int E = 0, cnt = 1;
      for (int j = 0; j < C; ++j)
        if (j != i && overlap[j][i])
          ++cnt;
```

```
for (int j = 0; j < C; ++j)
        if (i != j && g[i][j]) {
           pdd aa. bb:
           CCinter(c[i], c[j], aa, bb);
           double A = atan2(aa.Y - c[i].0.Y, aa.X - c[i
               ].O.X);
           double B = atan2(bb.Y - c[i].0.Y, bb.X - c[i
               ].O.X);
           eve[E++] = Teve(bb, B, 1), eve[E++] = Teve(aa
               , A, -1);
           if (B > A)
             ++cnt;
       if (E == 0)
        Area[cnt] += pi * c[i].R * c[i].R;
       else {
        sort(eve, eve + E);
         eve[E] = eve[0];
         for (int j = 0; j < E; ++j) {
           cnt += eve[j].add;
           Area[cnt] += cross(eve[j].p, eve[j + 1].p) *
               .5;
           double theta = eve[j + 1].ang - eve[j].ang;
           if (theta < 0)</pre>
             theta += 2. * pi;
           Area[cnt] += (theta - sin(theta)) * c[i].R *
               c[i].R * .5;
        }
    }
  }
|};
```

8.13 3Dpoint*

```
struct Point {
  double x, y, z;
  Point(double _x = 0, double _y = 0, double _z = 0):
      x(_x), y(_y), z(_z) \{ \}
  Point(pdd p) { x = p.X, y = p.Y, z = abs2(p); }
Point operator-(const Point &p1, const Point &p2) {
 return Point(p1.x - p2.x, p1.y - p2.y, p1.z - p2.z);
Point cross(const Point &p1, const Point &p2) {
  return Point(p1.y * p2.z - p1.z * p2.y, p1.z * p2.x -
       p1.x * p2.z,
               p1.x * p2.y - p1.y * p2.x);
double dot(const Point &p1, const Point &p2) {
  return p1.x * p2.x + p1.y * p2.y + p1.z * p2.z;
double abs(const Point &a) { return sqrt(dot(a, a)); }
Point cross3(const Point &a, const Point &b, const
    Point &c) {
  return cross(b - a, c - a);
double area(Point a, Point b, Point c) { return abs(
    cross3(a, b, c)); }
double volume(Point a, Point b, Point c, Point d) {
  return dot(cross3(a, b, c), d - a);
pdd proj(Point a, Point b, Point c, Point u) {
  \ensuremath{//} proj. u to the plane of a, b, and c
  Point e1 = b - a;
  Point e2 = c - a;
  e1 = e1 / abs(e1);
  e2 = e2 - e1 * dot(e2, e1);
  e2 = e2 / abs(e2);
  Point p = u - a;
  return pdd(dot(p, e1), dot(p, e2));
```

8.14 Convexhull3D*

```
struct CH3D {
  struct face {
    int a, b, c;
    bool ok;
  } F[8 * N];
  double dblcmp(Point &p, face &f) {
```

```
return dot(cross3(P[f.a], P[f.b], P[f.c]), p - P[f.
int g[N][N], num, n;
Point P[N];
void deal(int p, int a, int b) {
 int f = g[a][b];
  face add;
  if (F[f].ok) {
    if (dblcmp(P[p], F[f]) > eps)
      dfs(p, f);
      add.a = b, add.b = a, add.c = p, add.ok = 1,
      g[p][b] = g[a][p] = g[b][a] = num, F[num++] =
          add:
 }
}
void dfs(int p, int now) {
  F[now].ok = 0;
  deal(p, F[now].b, F[now].a), deal(p, F[now].c, F[
      now].b),
      deal(p, F[now].a, F[now].c);
bool same(int s, int t) {
  Point &a = P[F[s].a];
  Point \&b = P[F[s].b];
  Point &c = P[F[s].c];
  return fabs(volume(a, b, c, P[F[t].a])) < eps &&</pre>
         fabs(volume(a, b, c, P[F[t].b])) < eps &&
         fabs(volume(a, b, c, P[F[t].c])) < eps;</pre>
void init(int _n) { n = _n, num = 0; }
void solve() {
 face add;
  num = 0;
 if (n < 4)
   return;
  if ([&]() {
        for (int i = 1; i < n; ++i)
          if (abs(P[0] - P[i]) > eps)
            return swap(P[1], P[i]), 0;
        return 1;
      }() ||
      [&]() {
        for (int i = 2; i < n; ++i)
          if (abs(cross3(P[i], P[0], P[1])) > eps)
           return swap(P[2], P[i]), 0;
        return 1;
      }() ||
      [&]() {
        for (int i = 3; i < n; ++i)
          if (fabs(dot(cross(P[0] - P[1], P[1] - P
              [2]), P[0] - P[i])) > eps)
            return swap(P[3], P[i]), 0;
        return 1;
      }())
    return;
  for (int i = 0; i < 4; ++i) {
    add.a = (i + 1) \% 4, add.b = (i + 2) \% 4, add.c =
         (i + 3) \% 4,
    add.ok = true:
    if (dblcmp(P[i], add) > 0)
      swap(add.b, add.c);
    g[add.a][add.b] = g[add.b][add.c] = g[add.c][add.
        a] = num;
   F[num++] = add;
  for (int i = 4; i < n; ++i)
    for (int j = 0; j < num; ++j)
      if (F[j].ok && dblcmp(P[i], F[j]) > eps) {
        dfs(i, j);
        break;
  for (int tmp = num, i = (num = 0); i < tmp; ++i)
    if (F[i].ok)
      F[num++] = F[i];
double get_area() {
  double res = 0.0;
  if (n == 3)
    return abs(cross3(P[0], P[1], P[2])) / 2.0;
  for (int i = 0; i < num; ++i)
```

```
res += area(P[F[i].a], P[F[i].b], P[F[i].c]);
    return res / 2.0;
  double get_volume() {
    double res = 0.0;
    for (int i = 0; i < num; ++i)</pre>
      res += volume(Point(0, 0, 0), P[F[i].a], P[F[i].b
           ], P[F[i].c]);
    return fabs(res / 6.0);
  int triangle() { return num; }
  int polygon() {
    int res = 0;
    for (int i = 0, flag = 1; i < num; ++i, res += flag
         , flag = 1)
      for (int j = 0; j < i && flag; ++j)</pre>
        flag &= !same(i, j);
    return res;
  Point getcent() {
    Point ans(0, 0, 0), temp = P[F[0].a];
    double v = 0.0, t2;
    for (int i = 0; i < num; ++i)</pre>
      if (F[i].ok == true) {
        Point p1 = P[F[i].a], p2 = P[F[i].b], p3 = P[F[i].b]
            i].c];
        t2 = volume(temp, p1, p2, p3) / 6.0;
        if (t2 > 0)
           ans.x += (p1.x + p2.x + p3.x + temp.x) * t2,
               ans.y += (p1.y + p2.y + p3.y + temp.y)
                   t2.
               ans.z += (p1.z + p2.z + p3.z + temp.z) *
                   t2, v += t2;
    ans.x /= (4 * v), ans.y /= (4 * v), ans.z /= (4 * v)
        );
    return ans;
  double pointmindis(Point p) {
    double rt = 99999999;
    for (int i = 0; i < num; ++i)
      if (F[i].ok == true) -
        Point p1 = P[F[i].a], p2 = P[F[i].b], p3 = P[F[i].b]
             i].c];
         double a =
             (p2.y - p1.y) * (p3.z - p1.z) - (p2.z - p1.
z) * (p3.y - p1.y);
         double b =
             (p2.z - p1.z) * (p3.x - p1.x) - (p2.x - p1.x)
                x) * (p3.z - p1.z);
        double c =
             (p2.x - p1.x) * (p3.y - p1.y) - (p2.y - p1.
        y) * (p3.x - p1.x);
double d = 0 - (a * p1.x + b * p1.y + c * p1.z)
         double temp =
            fabs(a * p.x + b * p.y + c * p.z + d) /
                 sqrt(a * a + b * b + c * c);
        rt = min(rt, temp);
      }
    return rt;
  }
};
8.15 Tangent line of two circles
```

```
vector<Line> go(const Cir &c1, const Cir &c2, int sign1
  // sign1 = 1 for outer tang, -1 for inter tang
  vector<Line> ret;
  double d_{sq} = norm2(c1.0 - c2.0);
  if (d_sq < eps)</pre>
    return ret;
  double d = sqrt(d_sq);
  Pt v = (c2.0 - c1.0) / d;
  double c = (c1.R - sign1 * c2.R) / d;
  if (c * c > 1)
    return ret;
  double h = sqrt(max(0.0, 1.0 - c * c));
  for (int sign2 = 1; sign2 >= -1; sign2 -= 2) {
    Pt n = \{v.X * c - sign2 * h * v.Y, v.Y * c + sign2\}
        * h * v.X};
```

8.16 minMaxEnclosingRectangle

```
pdd solve(vector<pll> &dots) {
 vector<pll> hull;
  const double INF = 1e18, qi = acos(-1) / 2 * 3;
  cv.dots = dots;
 hull = cv.hull();
  double Max = 0, Min = INF, deg;
 11 n = hull.size();
 hull.pb(hull[0]);
  for (int i = 0, u = 1, r = 1, l; i < n; ++i) {
   pll nw = hull[i + 1] - hull[i];
    while (cross(nw, hull[u + 1] - hull[i]) > cross(nw,
        hull[u] - hull[i]))
      u = (u + 1) \% n;
    while (dot(nw, hull[r + 1] - hull[i]) > dot(nw,
       hull[r] - hull[i]))
      r = (r + 1) \% n;
    if (!i)
      1 = (r + 1) \% n;
    while (dot(nw, hull[l + 1] - hull[i]) < dot(nw,</pre>
        hull[1] - hull[i]))
      1 = (1 + 1) \% n;
   Min = min(
        Min, (double)(dot(nw, hull[r] - hull[i]) - dot(
            nw, hull[1] - hull[i]))
                 cross(nw, hull[u] - hull[i]) / abs2(nw
                     ));
    deg = acos((double)dot(hull[r] - hull[l], hull[u] -
         hull[i]) /
               abs(hull[r] - hull[l]) / abs(hull[u] -
                   hull[i]));
    deg = (qi - deg) / 2;
   Max = max(Max, (double)abs(hull[r] - hull[l]) * abs
        (hull[u] - hull[i]) '
                       sin(deg) * sin(deg));
  return pdd(Min, Max);
```

8.17 minDistOfTwoConvex

```
// p, q is convex
double TwoConvexHullMinDist(Point P[], Point Q[], int n
    , int m) {
  int YMinP = 0, YMaxQ = 0;
  double tmp, ans = 999999999;
  for (i = 0; i < n; ++i)
   if (P[i].y < P[YMinP].y)</pre>
      YMinP = i;
  for (i = 0; i < m; ++i)
    if (Q[i].y > Q[YMaxQ].y)
      YMaxQ = i;
  P[n] = P[0], Q[m] = Q[0];
  for (int i = 0; i < n; ++i) {</pre>
   while (tmp = Cross(Q[YMaxQ + 1] - P[YMinP + 1], P[
        YMinP] - P[YMinP + 1]) >
                 Cross(Q[YMaxQ] - P[YMinP + 1], P[YMinP
                     ] - P[YMinP + 1]))
      YMaxQ = (YMaxQ + 1) % m;
    if (tmp < 0)
      ans = min(ans, PointToSegDist(P[YMinP], P[YMinP +
           1], Q[YMaxQ]));
    else
      ans = min(ans,
                TwoSegMinDist(P[YMinP], P[YMinP + 1], Q
                    [YMaxQ], Q[YMaxQ + 1]));
   YMinP = (YMinP + 1) % n;
 }
 return ans;
```

8.18 Minkowski Sum*

```
vector<pll> Minkowski(vector<pll> A, vector<pll> B) {
  hull(A), hull(B);
  vector<pll> C(1, A[0] + B[0]), s1, s2;
  for (int i = 0; i < SZ(A); ++i)
    s1.pb(A[(i + 1) % SZ(A)] - A[i]);
  for (int i = 0; i < SZ(B); i++)
    s2.pb(B[(i + 1) % SZ(B)] - B[i]);
  for (int p1 = 0, p2 = 0; p1 < SZ(A) || p2 < SZ(B);)
    if (p2 >= SZ(B) || (p1 < SZ(A) && cross(s1[p1], s2[
        p2]) >= 0))
        C.pb(C.back() + s1[p1++]);
    else
        C.pb(C.back() + s2[p2++]);
  return hull(C), C;
}
```

8.19 RotatingSweepLine

```
void rotatingSweepLine(vector<pii> &ps) {
  int n = SZ(ps);
  vector<int> id(n), pos(n);
  vector<pii> line(n * (n - 1) / 2);
  int m = 0;
  for (int i = 0; i < n; ++i)
    for (int j = i + 1; j < n; ++j)
      line[m++] = pii(i, j);
  sort(ALL(line), [&](const pii &a, const pii &b) ->
      bool {
    if (ps[a.X].X == ps[a.Y].X)
      return 0;
    if (ps[b.X].X == ps[b.Y].X)
     return 1;
    return (double)(ps[a.X].Y - ps[a.Y].Y) / (ps[a.X].X
         - ps[a.Y].X) <
           (double)(ps[b.X].Y - ps[b.Y].Y) / (ps[b.X].X
                 - ps[b.Y].X);
  });
  iota(id, id + n, 0);
  sort(ALL(id), [&](const int &a, const int &b) {
      return ps[a] < ps[b]; });</pre>
  for (int i = 0; i < n; ++i)</pre>
    pos[id[i]] = i;
  for (int i = 0; i < m; ++i) {
    auto 1 = line[i];
    // meow
    tie(pos[1.X], pos[1.Y], id[pos[1.X]], id[pos[1.Y]])
        make_tuple(pos[1.Y], pos[1.X], 1.Y, 1.X);
```

9 Else

9.1 Mo's Alogrithm(With modification)

```
struct QUERY { // BLOCK=N^{2/3}
  int L, R, id, LBid, RBid, T;
  QUERY(int 1, int r, int id, int 1b, int rb, int t)
      : L(1), R(r), id(id), LBid(lb), RBid(rb), T(t) {}
  bool operator<(const QUERY &b) const {</pre>
    if (LBid != b.LBid)
      return LBid < b.LBid;</pre>
    if (RBid != b.RBid)
      return RBid < b.RBid;</pre>
    return T < b.T;</pre>
  }
};
vector<QUERY> query;
int cur_ans, arr[MAXN], ans[MAXN];
void addTime(int L, int R, int T) {}
void subTime(int L, int R, int T) {}
void add(int x) {}
void sub(int x) {}
void solve() {
  sort(ALL(query));
  int L = 0, R = 0, T = -1;
  for (auto q : query) {
    while (T < q.T)
      addTime(L, R, ++T);
    while (T > q.T)
```

```
subTime(L, R, T--);
while (R < q.R)
   add(arr[++R]);
while (L > q.L)
   add(arr[--L]);
while (R > q.R)
   sub(arr[R--]);
while (L < q.L)
   sub(arr[L++]);
   ans[q.id] = cur_ans;
}
</pre>
```

9.2 Mo's Alogrithm On Tree

```
const int MAXN = 40005;
vector<int> G[MAXN]; // 1-base
int n, B, arr[MAXN], ans[100005], cur_ans;
int in[MAXN], out[MAXN], dfn[MAXN * 2], dft;
int deep[MAXN], sp[__lg(MAXN * 2) + 1][MAXN * 2], bln[
    MAXN], spt;
bitset<MAXN> inset;
struct QUERY {
  int L, R, Lid, id, lca;
  QUERY(int 1, int r, int _id) : L(1), R(r), lca(0), id
      (_id) {}
  bool operator<(const QUERY &b) {</pre>
   if (Lid != b.Lid)
      return Lid < b.Lid;</pre>
    return R < b.R;</pre>
 }
vector<QUERY> query;
void dfs(int u, int f, int d) {
 deep[u] = d, sp[0][spt] = u, bln[u] = spt++;
  dfn[dft] = u, in[u] = dft++;
  for (int v : G[u])
    if (v != f)
      dfs(v, u, d + 1), sp[0][spt] = u, bln[u] = spt++;
  dfn[dft] = u, out[u] = dft++;
int lca(int u, int v) {
 if (bln[u] > bln[v])
    swap(u, v);
  int t = __lg(bln[v] - bln[u] + 1);
  int a = sp[t][bln[u]], b = sp[t][bln[v] - (1 << t) +
      1];
  if (deep[a] < deep[b])</pre>
    return a;
  return b;
void sub(int x) {}
void add(int x) {}
void flip(int x) {
  if (inset[x])
    sub(arr[x]);
  else
    add(arr[x]);
  inset[x] = ~inset[x];
void solve() {
 B = sqrt(2 * n), dft = spt = cur_ans = 0, dfs(1, 1,
      0);
  for (int i = 1, x = 2; x < 2 * n; ++i, x <<= 1)
    for (int j = 0; j + x <= 2 * n; ++j)
      if (deep[sp[i - 1][j]] < deep[sp[i - 1][j + x /</pre>
          2]])
        sp[i][j] = sp[i - 1][j];
      else
        sp[i][j] = sp[i - 1][j + x / 2];
  for (auto &q : query) {
    int c = lca(q.L, q.R);
    if (c == q.L || c == q.R)
      q.L = out[c == q.L ? q.R : q.L], q.R = out[c];
    else if (out[q.L] < in[q.R])</pre>
      q.lca = c, q.L = out[q.L], q.R = in[q.R];
    else
      q.lca = c, c = in[q.L], q.L = out[q.R], q.R = c;
    q.Lid = q.L / B;
  sort(ALL(query));
  int L = 0, R = -1;
```

```
for (auto q : query) {
    while (R < q.R)
      flip(dfn[++R]);
    while (L > q.L)
      flip(dfn[--L]);
    while (R > q.R)
      flip(dfn[R--]);
    while (L < q.L)
      flip(dfn[L++]);
    if (q.lca)
      add(arr[q.lca]);
    ans[q.id] = cur_ans;
    if (q.lca)
      sub(arr[q.lca]);
  }
}
```

9.3 DynamicConvexTrick*

```
// only works for integer coordinates!!
struct Line {
  mutable 11 a, b, p;
  bool operator<(const Line &rhs) const { return a <</pre>
       rhs.a; }
  bool operator<(ll x) const { return p < x; }</pre>
struct DynamicHull : multiset<Line, less<>>> {
  static const ll kInf = 1e18;
  11 Div(11 a, 11 b) { return a / b - ((a ^ b) < 0 && a</pre>
        % b); }
  bool isect(iterator x, iterator y) {
     if (y == end()) {
      x - p = kInf;
       return 0;
     if (x->a == y->a)
       x->p = x->b > y->b ? kInf : -kInf;
      x->p = Div(y->b - x->b, x->a - y->a);
    return x->p >= y->p;
  void addline(ll a, ll b) {
     auto z = insert(\{a, b, 0\}), y = z++, x = y;
     while (isect(y, z))
      z = erase(z);
     if (x != begin() && isect(--x, y))
       isect(x, y = erase(y));
     while ((y = x) != begin() && (--x)->p >= y->p)
       isect(x, erase(y));
  11 query(11 x) {
     auto 1 = *lower_bound(x);
     return 1.a * x + 1.b;
};
```

9.4 Matroid Intersection Start from $S = \emptyset$. In each iteration, let

```
 \begin{split} \bullet Y_1 &= \{x \not \in S \mid S \cup \{x\} \in I_1\} \\ \bullet Y_2 &= \{x \not \in S \mid S \cup \{x\} \in I_2\} \end{split}  If there exists x \in Y_1 \cap Y_2, insert x into S. Otherwise for each x \in S, y \not \in S, create edges  \bullet x \to y \text{ if } S - \{x\} \cup \{y\} \in I_1.
```

Find a shortest path (with BFS) starting from a vertex in Y_1 and ending at a vertex in Y_2 which doesn't pass through any other vertices in Y_2 , and alternate the path. The size of S will be incremented by 1 in each iteration. For the weighted case, assign weight w(x) to vertex x if $x \in S$ and -w(x) if $x \not\in S$. Find the path with the minimum number of edges among all minimum length paths and alternate it.

9.5 AdaptiveSimpson

ullet y
ightarrow x if $S - \{x\} \cup \{y\} \in I_2$.

```
double simpson_ada(const F_t &f, double 1, double r,
    double fl, double fm,
                   double fr, double eps) {
  double m = (1 + r) / 2, s = simpson(f, 1, r, fl, fr,
      fm).second;
  auto [flm, sl] = simpson(f, l, m, fl, fm);
  auto [fmr, sr] = simpson(f, m, r, fm, fr);
  double delta = sl + sr - s;
 if (abs(delta) <= 15 * eps)</pre>
    return sl + sr + delta / 15;
 return simpson_ada(f, 1, m, f1, f1m, fm, eps / 2) +
         simpson_ada(f, m, r, fm, fmr, fr, eps / 2);
double simpson_ada(const F_t &f, double 1, double r) {
 return simpson_ada(f, 1, r, f(1), f((1 + r) / 2), f(r)
      ), 1e-9 / 7122);
double simpson_ada2(const F_t &f, double 1, double r) {
  double h = (r - 1) / 7122, s = 0;
  for (int i = 0; i < 7122; ++i, l += h)
    s += simpson_ada(f, l, l + h);
 return s;
```

10 More

10.1 Binary Indexed Tree.cpp

```
int sum(int i) {
  int s = 0;
  while (i > 0) {
    s += bit[i];
    i -= i & -i;
  }
  return s;
}
void add(int i, int x) {
  while (i <= n) {
    bit[i] += x;
    i += i & -i;
  }
}</pre>
```

10.2 Bipartite Matching.cpp

```
// x nodes are numbered 1 to n, y nodes are numbered n
    +1 to n+m
// g[X].push_back[Y] / g[u].push_back(nx + v)
vector<int> g[200007];
int nx, ny, ma[200007], d[200007];
bool bfs() {
 int i, u, v, len;
  queue<int> Q;
  for (i = 1; i <= nx; i++) {
    if (ma[i] == 0) {
      d[i] = 0;
      Q.push(i);
    } else
      d[i] = INF;
  d[0] = INF;
  while (!Q.empty()) {
   u = Q.front();
    Q.pop();
    if (u != 0) {
      len = g[u].size();
      for (i = 0; i < len; i++) {
        v = g[u][i];
        if (d[ma[v]] == INF) {
          d[ma[v]] = d[u] + 1;
          Q.push(ma[v]);
      }
   }
  return (d[0] != INF);
bool dfs(int u) {
 int i, v, len;
  if (u != 0) {
    len = g[u].size();
    for (i = 0; i < len; i++) {</pre>
```

```
v = g[u][i];
       if (d[ma[v]] == d[u] + 1) {
         if (dfs(ma[v])) {
           ma[v] = u;
           ma[u] = v;
           return true;
         }
      }
    }
     d[u] = INF;
    return false;
  }
  return true;
int hopcroft_karp() {
  int res = 0, i;
  while (bfs())
    for (i = 1; i <= nx; i++)
       if (ma[i] == 0 && dfs(i))
        res++;
  return res;
}
```

10.3 Closest Pair.cpp

```
pair<double, double> p[50007], t[50007];
double solve(int 1, int r) {
  if (1 == r)
    return INF;
  int mid = (1 + r) >> 1;
  double x = p[mid].first;
  double d = min(solve(l, mid), solve(mid + 1, r));
  int i = 1, j = mid + 1, id = 1;
  while (i <= mid || j <= r) {
    if (i <= mid && (j > r \mid\mid p[i].second < p[j].second
        ))
      t[id++] = p[i++];
    else
      t[id++] = p[j++];
  for (int i = 1; i <= r; i++)
    p[i] = t[i];
  vector<pair<double, double>> v;
  for (int i = 1; i <= r; i++)
    if (abs(p[i].first - x) < d)
      v.push_back(p[i]);
  for (int i = 0; i < v.size(); i++) {
    for (int j = i + 1; j < v.size(); j++) {</pre>
      if (v[j].second - v[i].second >= d)
        break;
              sqrt((v[i].first - v[j].first) * (v[i].
                   first - v[j].first) +
                   (v[i].second - v[j].second) * (v[i].
                        second - v[j].second)));
   }
  }
  return d;
main() {
  sort(p + 1, p + n + 1);
  solve(1, n);
```

10.4 Dijkstra.cpp

```
// luogu4779
vector<pii> edge[100020];
int dis[100020];
int vis[100020];
void dijkstra(int s) {
  CLR(dis, 0x3f);
  dis[s] = 0;
  priority_queue<pii, vector<pii>, greater<pii>> pq;
  pq.emplace(0, s);
  while (pq.size()) -
    int now = pq.top().Y;
    pq.pop();
    if (vis[now])
      continue;
    vis[now] = 1;
    for (pii e : edge[now]) {
```

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```
Test123 codebook
      if (!vis[e.X] && dis[e.X] > dis[now] + e.Y) {
                                                                  dfs1(i.X. stk):
        dis[e.X] = dis[now] + e.Y;
                                                              stk.emplace_back(x);
        pq.emplace(dis[e.X], e.X);
                                                            void dfs2(int x, int id) {
                                                              scc[x] = id;
                                                              for (pii i : redge[x])
 }
}
                                                                if (!scc[i.X])
                                                                  dfs2(i.X, id);
10.5 Dinic.cpp
                                                            void kosaraju() {
                                                              int nscc = 0;
struct MaxFlow { // 0-base
                                                              vector<int> stk;
  struct edge {
    int to, cap, flow, rev;
                                                              for (int i = 1; i <= n; i++)
                                                                if (!vis[i])
  vector<edge> G[MAXN];
                                                                  dfs1(i, stk);
  int s, t, dis[MAXN], cur[MAXN], n;
                                                              while (stk.size()) {
  int dfs(int u, int cap) {
  if (u == t || !cap)
                                                                if (!scc[stk.back()])
                                                                  dfs2(stk.back(), ++nscc);
      return cap;
                                                                 stk.pop_back();
    for (int &i = cur[u]; i < (int)G[u].size(); ++i) {</pre>
      edge &e = G[u][i];
      if (dis[e.to] == dis[u] + 1 && e.flow != e.cap) {
                                                            10.7 Segment Tree with tag.cpp
        int df = dfs(e.to, min(e.cap - e.flow, cap));
        if (df) {
          e.flow += df;
                                                            void push(int id, int 1, int r) {
          G[e.to][e.rev].flow -= df;
                                                              int mid = (1 + r) >> 1;
          return df;
                                                              seg[id * 2] += tag[id] * (mid - 1 + 1);
                                                              seg[id * 2 + 1] += tag[id] * (r - mid);
        }
      }
                                                              tag[id * 2] += tag[id];
                                                              tag[id * 2 + 1] += tag[id];
    dis[u] = -1;
                                                              tag[id] = 0;
    return 0;
                                                            void modify(int id, int l, int r, int ql, int qr, int
  bool bfs() {
                                                                val) {
    FILL(dis, -1);
                                                              if (ql > r \mid\mid qr < 1)
                                                                return;
    queue<int> q;
    q.push(s), dis[s] = 0;
                                                              if (ql <= 1 && r <= qr) {
    while (!q.empty()) {
                                                                seg[id] += val * (r - l + 1);
                                                                tag[id] += val;
      int tmp = q.front();
      q.pop();
                                                                return;
      for (auto &u : G[tmp])
        if (!~dis[u.to] && u.flow != u.cap) {
                                                              if (1 == r)
          q.push(u.to);
                                                                return;
          dis[u.to] = dis[tmp] + 1;
                                                              push(id, 1, r);
                                                              int mid = (l + r) >> 1;
modify(id * 2, l, mid, ql, qr, val);
        }
    }
                                                              modify(id * 2 + 1, mid + 1, r, ql, qr, val);
    return dis[t] != -1;
                                                              seg[id] = seg[id * 2] + seg[id * 2 + 1];
  int maxflow(int _s, int _t) {
                                                            int query(int id, int l, int r, int ql, int qr) {
    s = _s, t = _t;
    int flow = 0, df;
                                                              if (ql > r || qr < 1)</pre>
    while (bfs()) {
                                                                return 0;
      FILL(cur, 0);
                                                              if (ql <= 1 && r <= qr)</pre>
                                                                return seg[id];
      while (df = dfs(s, INF))
                                                              push(id, 1, r);
        flow += df;
                                                              int mid = (1 + r) >> 1;
                                                              return query(id * 2, 1, mid, ql, qr) + query(id * 2 +
    return flow;
                                                                   1, mid + 1, r, ql, qr);
  void init(int _n) {
    n = _n;
for (int i = 0; i < n; ++i)</pre>
                                                            10.8 Suffix Array.cpp
      G[i].clear();
                                                            // array c is eventually equal to the position of the
  void reset() {
                                                                 suffixes in the suffix
    for (int i = 0; i < n; ++i)
                                                            // array don't add another '$' to the string
      for (auto &j : G[i])
                                                            int sa[400007], c[400007], sa_new[400007], c_new
        j.flow = 0;
                                                                [400007], cnt[400007],
                                                                pos[400007], lcp[400007];
  void add_edge(int u, int v, int cap) {
                                                            pair<char, int> P[400007];
    G[u].pb(edge{v, cap, 0, (int)G[v].size()});
                                                            void calc_suffix_array(string s) {
                                                              s += '$';
    G[v].pb(edge{u, 0, 0, (int)G[u].size() - 1});
                                                              int n = s.size();
};
                                                              for (int i = 0; i < n; i++)
                                                                P[i] = {s[i], i};
10.6 Kosaraju.cpp
                                                              sort(P, P + n);
                                                              for (int i = 0; i < n; i++)</pre>
vector<pii> edge[100020], redge[100020];
                                                                sa[i] = P[i].second;
int vis[100020], scc[100020];
                                                              c[sa[0]] = 0;
                                                              for (int i = 1; i < n; i++)
void dfs1(int x, vector<int> &stk) {
  vis[x] = 1;
                                                                c[sa[i]] = c[sa[i - 1]] + (P[i].first > P[i - 1].
  for (pii i : edge[x])
                                                                     first ? 1 : 0);
```

int k = 1;

if (!vis[i.X])

```
while (k < n) {
                                                               if (!t)
    for (int i = 0; i < n; i++)</pre>
                                                                 a = b = NULL;
      sa[i] = (sa[i] - k + n) \% n;
                                                               else {
    for (int i = 0; i < n; i++)
                                                                 push(t):
      cnt[i] = 0;
                                                                 if (size(t->lc) + 1 <= k) {
    for (int i = 0; i < n; i++)
                                                                   a = t:
      cnt[c[i]]++;
                                                                   split(t\rightarrow rc, k - size(t\rightarrow lc) - 1, a\rightarrow rc, b);
    pos[0] = cnt[0] - 1;
                                                                   pull(a);
    for (int i = 1; i < n; i++)
                                                                 } else {
                                                                   b = t;
      pos[i] = pos[i - 1] + cnt[i];
    for (int i = n - 1; i >= 0; i --)
                                                                   split(t->lc, k, a, b->lc);
      sa_new[pos[c[sa[i]]]--] = sa[i];
                                                                   pull(b);
    for (int i = 0; i < n; i++)</pre>
      sa[i] = sa_new[i];
                                                               }
    c_new[sa[0]] = 0;
                                                             }
    for (int i = 1; i < n; i++) {
      c_new[sa[i]] = c_new[sa[i - 1]];
                                                             10.10 Simple Graph Matching.cpp
      pair<int, int> prev = {c[sa[i - 1]], c[(sa[i - 1]
           + k) % n]};
                                                             #include <bits/stdc++.h>
      pair<int, int> now = {c[sa[i]], c[(sa[i] + k) % n
                                                             using namespace std;
          ]};
                                                             #define FOR(i, a, b) for (int i = a; i \leftarrow b; i++)
      if (now > prev)
                                                             #define REP(u) for (int i = h[u], v; v = e[i].t, i; i = h[u]
        c_new[sa[i]]++;
                                                                  e[i].n)
                                                             const int N = 520, M = 2e5 + 1;
    for (int i = 0; i < n; i++)
                                                             queue<int> q;
     c[i] = c_new[i];
                                                             int n, m, tot, qwq, ans;
                                                             int h[N], lk[N], tag[N], fa[N], pre[N], dfn[N];
 }
                                                             struct edge {
                                                               int t, n;
void calc_lcp_array(string s) {
                                                             } e[M];
                                                             void link(int x, int y) { lk[x] = y, lk[y] = x; }
 int n = s.size(), k = 0;
  for (int i = 0; i < n; i++) {
                                                             void add_edge(int x, int y) {
    int j = sa[c[i] - 1];
                                                               if (!lk[x] && !lk[y])
    while (i + k < n \&\& j + k < n \&\& s[i + k] == s[j + k]
                                                                 link(x, y), ans++;
        k])
                                                               e[++tot] = (edge)\{y, h[x]\}, h[x] = tot;
      k++;
                                                               e[++tot] = (edge)\{x, h[y]\}, h[y] = tot;
    lcp[c[i] - 1] = k;
    k = max(k - 1, 011);
                                                             void rev(int x) {
 }
                                                               if(x)
}
                                                                 rev(x[pre][lk]), link(x, pre[x]);
10.9
        Treap.cpp
                                                             int find(int x) { return fa[x] == x ? x : fa[x] = find(
                                                                  fa[x]); }
// Zerojudge a063: subsequence reversal
                                                             int lca(int x, int y) {
struct Treap {
                                                               for (qwq++;; x = x[lk][pre], swap(x, y))
 Treap *lc, *rc;
                                                                 if (dfn[x = find(x)] == qwq)
                                                                   return x;
  int pri, sz, val;
  bool tag;
                                                                 else if (x)
                                                                   dfn[x] = qwq;
 Treap(int x) {
   1c = rc = NULL;
    pri = rand(), sz = 1, val = x, tag = 0;
                                                             int shrink(int x, int y, int p) {
                                                               for (; find(x) != p; x = pre[y]) {
 }
                                                                 pre[x] = y, y = lk[x], fa[x] = fa[y] = p;
                                                                 if (tag[y] == 2)
inline int size(Treap *t) { return t ? t->sz : 0; }
inline void pull(Treap *t) { t->sz = size(t->lc) + 1 +
                                                                   tag[y] = 1, q.push(y);
    size(t->rc); }
void push(Treap *t) {
 if (t->tag) {
                                                             int blossom(int u) {
                                                               FOR(i, 1, n) tag[i] = pre[i] = 0, fa[i] = i;
    swap(t->lc, t->rc);
                                                               tag[u] = 1, q = queue < int > (), q.push(u);
    if (t->lc)
      t->lc->tag = !t->lc->tag;
                                                               for (int p; !q.empty(); q.pop())
    if (t->rc)
                                                                 REP(u = q.front())
                                                               if (tag[v] == 1)
     t->rc->tag = !t->rc->tag;
                                                                 p = lca(u, v), shrink(u, v, p), shrink(v, u, p);
    t \rightarrow tag = 0;
 }
                                                               else if (!tag[v]) {
                                                                 pre[v] = u, tag[v] = 2;
Treap *merge(Treap *a, Treap *b) {
                                                                 if (!lk[v])
 if (!a || !b)
                                                                   return rev(v), 1;
                                                                 else
    return a ? a : b;
  if (a->pri > b->pri) {
                                                                   tag[lk[v]] = 1, q.push(lk[v]);
    push(a);
                                                               }
    a->rc = merge(a->rc, b);
                                                               return 0;
   pull(a);
    return a;
                                                             int main() {
                                                               scanf("%d%d", &n, &m);
  } else {
                                                               for (int x, y; m--; add_edge(x, y))
  scanf("%d%d", &x, &y);
    push(b);
    b->lc = merge(a, b->lc);
                                                               FOR(i, 1, n) ans += !lk[i] && blossom(i);
    pull(b);
                                                               cout << ans << '\n';</pre>
    return b:
```

}

void split(Treap *t, int k, Treap *&a, Treap *&b) {

for (int i = 1; i <= n; i++)
 cout << i << ' ' << lk[i] << '\n' return 0;</pre>