

## Search Algorithms?



Looking for

5

You can use different algorithms for different kinds of lists –  
with different time complexities

# Linear Search



Looking for

5

Linear search works on **ordered and unordered** lists and **checks all items** until it finds the element you're searching.

## Linear Search – Time Complexity

Best Case

The item we're looking for is the very **first** item in the list

$O(1)$

Average Case

Random order, we don't know where the item is

Tends to be  $O(n)$

Worst Case

The item we're looking for is the very **last** item in the list

$O(n)$

## Binary Search

3

10

-3

48

5

33

99

Looking for

5

**Doesn't work on unordered lists!** You need  
to sort the list first!

# Binary Search



Looking for

5

Find median and compare  
it to the element you're  
trying to find

Is it the element you're  
looking for?

If element wasn't found,  
take the half in which must  
be inside

Repeat!

## Binary Search – Time Complexity

Best Case

The item we're looking for  
is **right in the middle**

$O(1)$

Average Case

We don't know where the  
item will be

Tends to be  $O(\log n)$

Worst Case

The item we're looking for  
is **at the beginning or end**

$O(\log n)$

Because we split  
the array in half in  
every iteration

# Recursion & Big O (The Master Theorem)

How do you derive Big O for more complex recursive algorithms?

## Master Theorem

Runtime of recursion:  $O(n^{\log_b a})$

Overall algorithm runtime (time complexity) - three cases:

Recursion does more work

$$O(n^{\log_b a})$$

Same work inside and outside of recursion

$$O(n^{\log_b a} \log n)$$

Non-recursive part does more work

$$O(f(n))$$

where

**a** equals the number of subproblems (number of recursion splits)

**b** equals the relative subproblem size (input reduction per split)

**f(n)** equals the runtime outside of the recursion