UR5e Frames + DH

Frame Assignment:

Z₀: base yaw axis, vertical.

 Z_1 : shoulder pitch axis; perpendicular to Z_0 (points "forward" in a side view).

 Z_2 : elbow pitch axis; parallel to Z_1 .

 Z_3 : wrist-1 pitch axis; typically parallel to Z_1 and Z_2 .

 Z_4 : wrist-2 axis; orthogonal to Z_3 .

 Z_5 : wrist-3 (tool roll) axis; orthogonal to Z_4 .

UR5e Geometric Constants:

 $d_1 = 0.1625 \text{ m}$

 $a_2 = -0.425 \text{ m}$

 $a_3 = -0.392 \text{ m}$

 $d_4 = 0.1333 \text{ m}$

 $d_5 = 0.0997 \text{ m}$

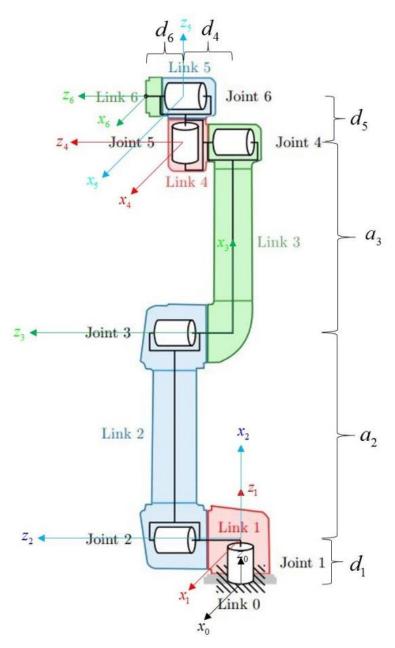
 $d_6 = 0.0996 \text{ m}$

Base height $L_B = 0.163 \text{ m}$

Tool-plate thickness $L_{TP} = 0.1 \text{ m}$

For context, a2 and a3 are the "upper arm" and "forearm" link lengths; d4 and d5 are the wrist stack offsets. L_B is the base pedestal height.

 $\label{thm:parameters} Figure~X:~UR5e~manipulator~with~labeled~DH~parameters~ai~and~di~.~(Source:~Universal~Robots~/~ResearchGate)$



Standard DH Table(UR5e):

Joint(i)	a i-1	lpha _{i-1}	\mathbf{d}_{i}	$oldsymbol{ heta}_{ ext{i}}$
1	0	$\pi/2$	0.1625 m	Θ_1
2	-0.425 m	0	0	θ_2
3	-0.392 m	0	0	θ_3
4	0 m	$\pi/2$	0.1333 m	θ_4
5	0 m	- π/2	0.0997 m	θ_5
6	0 m	0	0.0996 m	θ_6

Sources:

- 1. Universal Robots. *DH Parameters for Calculations of Kinematics and Dynamics*. Retrieved from: https://www.universal-robots.com/articles/ur/application-installation/dh-parameters-for-calculations-of-kinematics-and-dynamics/
- 2. Williams, R. L. (2024). *Universal Robot Kinematics*. Ohio University, Department of Mechanical Engineering. Retrieved from: https://people.ohio.edu/williams/html/PDF/UniversalRobotKinematics.pdf
- 3. ROS-Industrial Consortium. *UR5 Robot Description (URDF file)*. GitHub Repository: https://github.com/ros-industrial/universal_robot/blob/melodic-devel/ur_description/urdf/ur5.urdf.xacro