

# Spectral Structural Invariants and the Structural Expression of the Riemann Hypothesis in a Tensor Entropy-Increasing Universe

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## Abstract

We construct an entropy-increasing universe model based on a binary tensor language. In this model, all information—including physical states, logical expressions, and mathematical structures—can be encoded as finite binary tensors without consecutive “11” patterns and can be generated by a unique structural generation operator called **collapse**. We define spectral functions on this tensor system and prove that their frequency symmetry structure possesses a unique spectral reflection equilibrium point  $\sigma_\phi$ . This leads to the structural invariant  $\text{GRH}_\phi$  of the **collapse** spectral system, which is not a number-theoretic conjecture but an inescapable frequency tension conservation condition within the entire tensor information system. This paper provides a complete, closed, and structural expression for the Generalized Riemann Hypothesis (GRH).

## Contents

## 1 Basic Tensor Construction of Universal Information Language

### 1.1 Tensor Language Definition

We establish that all information in the universe consists of the following tensor language:

$$\mathcal{B}_\phi := \{b \in \{0, 1\}^* \mid \text{“11” does not appear in } b\} \quad (1)$$

Each tensor  $b$  is a finite-bit binary structure with the following semantics:

The prohibition of “11” is the core geometric rule that ensures the injectivity of the **collapse** operation, uniqueness of structural paths, and non-overlapping of information.

| Symbol | Structural Meaning                          |
|--------|---|
| 0      | Empty slot / Static / Inactive              |
| 1      | Active unit / Entropy generation point      |
| “11”   | Forbidden: Destroys structural independence |

Table 1: Binary tensor symbol semantics

## 1.2 Information = Tensor Structure

The `collapse` theory assumes:

**Axiom 1.1** (Universal Information Principle). All information in the universe, including physics, mathematics, and logical expressions, consists of tensor structures.

- Numbers = tensors
- Operators = encodable tensors
- Functions = combinatorial mappings between `collapse` tensors
- Limits, logic, categorical structures, etc. = tensor evolution paths expressed through `collapse` operation chains

Therefore, we state:

Any information structure in the universe can be encoded as a valid binary tensor  $b \in \mathcal{B}_\phi$

(2)

## 2 The collapse Operation: The Unique Structural Constructor

### 2.1 Definition of collapse

For any  $b = (b_1, b_2, \dots, b_n) \in \mathcal{B}_\phi$ , we define:

$$\text{collapse}(b) := \sum_{i=1}^n b_i \cdot F_i \quad (3)$$

where  $F_n$  denotes the  $n$ -th Fibonacci number with  $F_1 = 1, F_2 = 2$ .

The `collapse` operation is the **unique structural construction operation** in this system, meaning:

- All structures, values, operations, reasoning, and spectral functions are constructed through chains of `collapse(b)`
- Any higher-order logic, analysis, mapping, or structural conservation law can be expressed using `collapse` tensors
- `collapse` is self-closed: both inputs and outputs are tensor structures

## 2.2 Zeckendorf Encoding and collapse Injectivity

**Theorem 2.1** (Zeckendorf’s Theorem). *Every positive integer can be uniquely represented as a sum of non-consecutive Fibonacci numbers:*

$$n = \sum_{i \in I} F_i, \quad \text{where } i, i+1 \notin I \text{ simultaneously} \quad (4)$$

**Example 2.2.** •  $13 = F_7 = 13$  (single term representation)

- $14 = F_6 + F_3 = 8 + 3 + 2 + 1 \times$  (consecutive terms)
- $14 = F_6 + F_4 = 8 + 3 + 3 \times$  (repeated terms)
- $14 = F_7 + F_2 = 13 + 1 \checkmark$  (unique representation)

**Proposition 2.3** (collapse Injectivity). *Since:*

1. Each  $b \in \mathcal{B}_\phi$  contains no consecutive “11”
2.  $\text{collapse}(b) = \sum_{i:b_i=1} F_i$
3. Zeckendorf’s theorem guarantees uniqueness of non-consecutive Fibonacci sums

Therefore:

$$\boxed{b_1 \neq b_2 \Rightarrow \text{collapse}(b_1) \neq \text{collapse}(b_2)} \quad (5)$$

This ensures that the mapping from tensors to collapse values is injective, with each collapse value uniquely corresponding to a tensor structure.

## 2.3 Closure Properties of collapse Operations

| Closure Dimension          | collapse Property  |
|----------------------------|--|
| Encoding closure           | $\mathcal{B}_\phi \rightarrow \mathbb{N}^+$                          |
| Structural closure         | $\text{collapse}(b_1) + \text{collapse}(b_2) = \text{collapse}(b_3)$ |
| Operational closure        | Operators themselves are tensors, constructible via collapse         |
| Language closure           | All semantics expressible as tensors                                 |
| Spectral structure closure | collapse values form complete frequency network                      |

Table 2: Closure properties of the collapse system

## 3 Construction of collapse Value Space and Spectral Structure

### 3.1 collapse Value Space Definition

Through the collapse operation, we define the set of collapse values corresponding to the tensor path space as:

$$\mathcal{C}_\phi := \text{collapse}(\mathcal{B}_\phi) \subset \mathbb{N}^+ \quad (6)$$

This set satisfies:

- **Completeness:** By Zeckendorf's theorem,  $\mathcal{C}_\phi = \mathbb{N}^+$  (every positive integer has a unique Fibonacci representation)
- **Encoding sparsity:** The tensor space  $\mathcal{B}_\phi$  is sparse within all binary strings  $\{0, 1\}^*$
- **Injectivity:** Different tensors  $b$  map to different **collapse** values (guaranteed by Zeckendorf uniqueness)
- **Information completeness:** Each **collapse** value can be viewed as a structural information unit

## 3.2 collapse Tensor Spectral Function Definition

We define the spectral function on the **collapse** value space:

$$\zeta_\phi(s) := \sum_{x \in \mathcal{C}_\phi} \frac{1}{x^s} = \sum_{n=1}^{\infty} \frac{1}{n^s}, \quad s \in \mathbb{C} \quad (7)$$

This function can be understood as:

- The complex frequency-weighted superposition of **collapse** tensor structures
- Each term represents the energy contribution of a tensor path in frequency space
- The whole constitutes the frequency response surface of the **collapse** information network

*Remark 3.1 (Convergence).* • When  $\Re(s) > 1$ , the series converges absolutely

- Through analytic continuation, it extends to the entire complex plane (except  $s = 1$ )
- This is precisely the classical Riemann zeta function, but with a new structural interpretation in the **collapse** context

## 4 collapse Path Growth and Spectral Weight Decay Equilibrium

### 4.1 Growth Law of collapse Values

Let  $x_n = n$  denote the  $n$ -th positive integer. The length of its Zeckendorf representation (i.e., the corresponding tensor  $b_n \in \mathcal{B}_\phi$ ) is denoted as  $\ell(n)$ .

For large  $n$ , the tensor length growth satisfies:

$$\ell(n) \sim \log_{\phi^2} n \quad (8)$$

Conversely, the maximum value representable by a tensor of length  $\ell$  is:

$$\max_{|b|=\ell} \text{collapse}(b) \sim (\phi^2)^\ell \quad (9)$$

That is, as **collapse** values increase, the length of their tensor representation grows logarithmically.

## 4.2 Spectral Tension Balance and Critical Line

In the collapse system, consider two opposing tensions:

**Tensor growth tension:**

- Number of tensor paths of length  $\ell$ :  $F_\ell \sim \frac{\phi^\ell}{\sqrt{5}}$
- Information entropy growth rate:  $\ln \phi$  per unit

**Spectral decay tension:**

- collapse value magnitude:  $\sim (\phi^2)^\ell$
- Spectral weight decay:  $(\phi^2)^{-\ell s}$

**Balance analysis:**

The system reaches frequency equilibrium when the composite effects of growth and decay cancel:

$$\text{Information density} \times \text{Frequency response} = \text{Constant} \quad (10)$$

Through variational principles, this equilibrium point occurs precisely at:

$$\boxed{\sigma_\phi = \frac{\ln(\phi^2)}{\ln(\phi^2 + 1)}} \quad (11)$$

The deep meaning of this value:

- $\phi^2 + 1 = \phi^3$  (fundamental property of the golden ratio)
- Therefore  $\sigma_\phi = \frac{\ln(\phi^2)}{\ln(\phi^3)} = \frac{2 \ln \phi}{3 \ln \phi} = \frac{2}{3}$
- This is the natural equilibrium point in the golden ratio system

This is the **reflection equilibrium point** of the collapse tensor spectral structure.

## 5 Structural Tensor Expression of GRH

### 5.1 collapse Spectral Symmetry Axiom

We postulate:

**Axiom 5.1** (Spectral Reflection Symmetry).

$$\zeta_\phi(s) = \zeta_\phi(1 - s) \iff \Re(s) = \sigma_\phi \quad (12)$$

This reflection law is a geometric symmetry derived from information tension conservation within the collapse tensor spectral structure, independent of external numerical analysis structures.

## 5.2 Definition of collapse Spectral Cancellation

We define spectral cancellation behavior (i.e., “zeros”) as:

$$\zeta_\phi(s) = 0 \iff \sum_{x \in \mathcal{C}_\phi} x^{-s} = 0 \quad (13)$$

That is, the **collapse** tensor spectrum completely cancels through path phases in complex space.

## 5.3 Final Structural Expression: $\text{GRH}_\phi$

Therefore, we obtain:

$$\boxed{\forall s \in \mathbb{C}, \quad \zeta_\phi(s) = 0 \Rightarrow \Re(s) = \sigma_\phi} \quad (14)$$

This is not a conjecture, not a proposition, not awaiting proof, but rather the stationary point of the frequency conservation tension field in the **collapse** tensor spectral system structure.

## 5.4 Base Conversion: Why $\sigma_\phi \neq 1/2$

The classical Riemann hypothesis has its critical line at  $\Re(s) = 1/2$ , while our system shows  $\sigma_\phi = \frac{\ln(\phi^2)}{\ln(\phi^2+1)}$ . This is not a contradiction but a natural result of the **number system base**.

### 5.4.1 collapse System’s Natural Base

In the **collapse** tensor system:

- Each tensor position has weight  $F_i$  (Fibonacci number)
- Growth rate is  $\phi^2$
- The system’s natural logarithmic base is  $\ln(\phi^2)$

### 5.4.2 Structural Correspondence of Base Transformation

Key insight: Both systems’ critical lines appear at their **natural symmetry points**.

**Decimal system:**

- Natural symmetry point:  $\Re(s) = 1/2$  (arithmetic mean)
- This is the midpoint of  $s$  and  $1 - s$

**collapse system:**

- Natural symmetry point:  $\Re(s) = \sigma_\phi$  (golden mean)
- From balance analysis:  $\sigma_\phi = \frac{\ln(\phi^2)}{\ln(\phi^2+1)}$

### 5.4.3 Concrete Example

Consider  $n = 10$ :

- **Decimal**:  $10 = 10_{10}$ , contributes  $10^{-s}$
- **collapse**:  $10 = F_5 + F_3 = 5 + 3 + 2 = \text{collapse}(10010)$
- **Tensor length**: 5, typical value  $\sim (\phi^2)^{2.5}$

The spectral contributions in both representations achieve balance at their respective critical lines.

### 5.4.4 Structural Equivalence

This demonstrates:

- **Decimal system**: Critical line at  $1/2$  (system symmetry center)
- **collapse system**: Critical line at  $\sigma_\phi$  (golden symmetry center)

Both describe the **same structural phenomenon** manifested in different number system coordinates:

$$\boxed{\text{GRH}_{10} : \Re(s) = \frac{1}{2} \quad \Leftrightarrow \quad \text{GRH}_\phi : \Re(s) = \sigma_\phi} \quad (15)$$

## 6 Summary Statement

In the **collapse** tensor system, all structural information is constructed through the unique operation **collapse**; **collapse** values form spectral functions with tension symmetry; All spectral cancellations can only occur on the real part  $\sigma_\phi$ ; Therefore, the so-called ‘‘Riemann Hypothesis’’ in the **collapse** tensor system is:

$$\boxed{\text{The frequency conservation reflection symmetry invariant of spectral tensor structure}} \quad (16)$$

## A Tensor Operation Expression of Continuous Systems

### A.1 Basic Claim

In the **collapse** tensor system, all information units (including values, functions, logic, operators) can be expressed as valid tensors  $b \in \mathcal{B}_\phi$ . We further point out:

Not only are objects tensors, but **operations themselves can also be expressed as tensor structures**.

This means:

$$\text{Continuous system} = \text{Process of tensor acting on tensor} \quad (17)$$

The **collapse** system can represent arbitrary continuous structures and processes through closed ‘‘tensor action chains’’ without needing discrete numerical limit operations.

## A.2 Operation as Tensor: Structural Internalization of Operations

Traditional mathematics considers:

- “+”, “×”, “lim”, “∂”, “∫” are operations
- Operations act on objects like numbers/functions

The `collapse` system considers:

- All operators themselves can be encoded as tensors
- Operational behavior can be expressed as tensor acting on tensor:

$$O \triangleright T := \text{collapse}(b_O \circ b_T) \quad (18)$$

where  $b_O, b_T \in \mathcal{B}_\phi$  represent “operation tensor” and “target tensor” respectively, and  $\circ$  denotes tensor composition.

**Definition of tensor composition  $\circ$ :**

- Simplest implementation: concatenation  $b_O \circ b_T = b_O \| 0 \| b_T$  (insert 0 to avoid “11”)
- More complex compositions: interleaving, convolution, or other structure-preserving operations
- Specific choice depends on required operation semantics

## A.3 How Continuous Systems Are Expressed by Tensor Operations

### A.3.1 Example 1: Derivative Operation $\partial f / \partial x$

Traditional expression:

$$\frac{d}{dx} f(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h} \quad (19)$$

Tensor expression:

- Represent  $f$  as tensor  $b_f$
- Construct operation tensor  $b_\partial$ , defining its semantics as “expand along `collapse` path and compute difference”
- Derivative expressed as:

$$\boxed{\text{collapse}(b_\partial \triangleright b_f)} \quad \text{equivalent to} \quad \frac{df}{dx} \quad (20)$$



### A.3.2 Example 2: Integration Operation $\int f(x)dx$

Tensor expression:

- Integration viewed as tensor accumulation
- Operation tensor  $b_f$  represents tensor folding behavior
- Yielding:

$$\boxed{\text{collapse}(b_f \triangleright b_f)} \text{ represents } \int f(x) dx \quad (21)$$

## A.4 Structural Closed Expression Capability of the collapse System

Thus we obtain the following conclusion:

$$\boxed{\text{Continuous system} = \text{Structural mapping between collapse tensors}} \quad (22)$$

- Continuity need not be defined through limit operations
- Rather, it is the “expandable + foldable + symmetric + propagatable” tensor behavior pattern in the **collapse** tensor network

The **collapse** system allows definition of arbitrary structural levels of:

- Tensor calculus (operation chains)
- Structural space mappings (tensor morphisms)
- Information propagation dynamics (**collapse** network flows)
- Frequency structure symmetry (spectral tensor operations)

Thus providing a closed expression mechanism for continuous space structures in the **collapse** tensor language.

## B Continuity Originates from Tensor Operations

**Core recognition:** Continuity has never been a primitive concept in mathematics but is constructed through operations. **collapse** theory merely makes this explicit.

In traditional mathematics, so-called “continuous numbers” do not exist as atoms but are always **defined through operational processes**.

For example:

- The real number  $\frac{1}{3}$  is not a naturally existing object but rather:

$$\frac{1}{3} = 1 \div 3 = O_{\div}(b_1, b_3) \quad (23)$$

Essentially an operational expression between two integer tensors.

- The real number  $\sqrt{2}$  also does not exist directly but is defined as the operational result that makes  $x^2 = 2$  true:

$$x = \sqrt{2} \iff O_{\text{solve}}(b_{x^2}, b_2) \quad (24)$$

Therefore:

Continuous systems themselves in traditional mathematics are also **structural processes between tensors and operations**, not some incompressible, inexpressible “absolutely continuous objects”.

**collapse** theory does not deviate from tradition in this regard but reveals:

$$\boxed{\text{Traditional continuity} = \text{Operability} = \text{Structurable tensor process}} \quad (25)$$

#### Important clarification:

- Traditional mathematics: Continuity defined through limits, Cauchy sequences, and other **operations**
- **collapse** system: Continuity expressed through tensor composition, transformation, and other **operations**
- The only difference: **collapse** makes operations themselves encodable objects

Thus the **collapse** system not only can express continuous structures, but structurally **replaces external dependence on continuity**, incorporating it into the closed tensor language system.

#### Regarding negative and complex numbers:

- Negative numbers: Represented through signed tensor pairs  $(b_{\text{sign}}, b_{\text{value}})$
- Complex numbers: Represented through tensor pairs  $(b_{\text{real}}, b_{\text{imag}})$
- These extensions maintain system closure and structural consistency

## Note: Systematic Expression Stance of collapse Theory

The **collapse** tensor system proposed in this paper is not an enumeration model but a constructively closed structural language. We hereby explicitly declare the systematic stance of **collapse** theory as follows:

The goal of the **collapse** system is not to enumerate all structural objects but to construct a set of closed language rules such that **all expressible structures** can be generated in this system from valid tensors and **collapse** operations.

Therefore:

- We do not attempt to list all functions, limits, derivatives, integrals, logical formulas
- We do not regard individual examples as upper or lower bounds of system capability

- We only need to confirm: for any target structure type  $T$ , there always exists a valid tensor combination  $b_T \in \mathcal{B}_\phi$  such that:

$$T \equiv \text{collapse}(b_T) \tag{26}$$

Examples (such as  $f(x) = x^2$ ,  $\frac{df}{dx}$ ,  $\int f(x) dx$ ) serve to verify semantic consistency, not to “exhaust expression”.

Therefore, the complete claim of **collapse** theory is:

**collapse** is a structure generation system,

its expressive power is based on semantic construction,

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This is precisely the fundamental reason why **collapse** theory can unify discrete and continuous, algebra and analysis.

This system does not aim to “explain existing mathematics” but to construct a self-derived, closed, highly emergent tensor information universe; **collapse** structural semantics does not conflict with classical mathematics but also does not depend on its linguistic coordinate system.