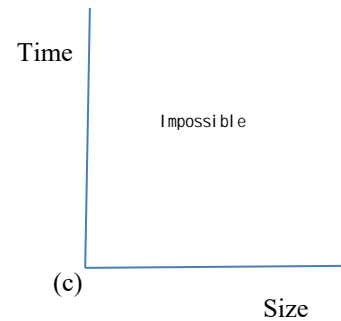
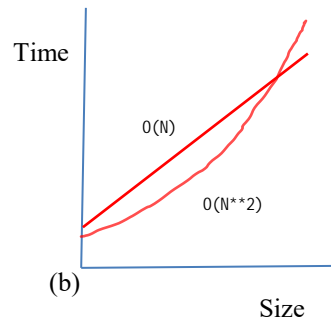
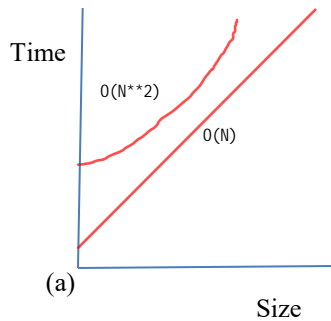


1.



2. (a)

Because log is a really slowly growing function.

(b)

When N is big enough, the f_a with lower complexity class will be faster than f_b .

(c)

When the problem size is too small, the complexity class analysis cannot help to understand the behavior of different algorithms accurately.

3. (a1)

$3.00 \times 10^{(-5)}$

(a2)

$2.00 \times 10^{(-7)} + 6.00 \times 10^{(-4)}$

((b1)

$3.00 \times 10^{(-1)}$

(b2)

$2.00 \times 10^{(-5)} + 6.00 \times 10^{(-2)}$

(c1)

2

(c2)

0

4(a).

```
def sumsto_1 (alist, asum):
    for f in alist:           N
        for s in alist:       N**2
            if f+s == asum:    N**2
                return (f,s)   N**2
    return None                1
```

```
def sumsto_2 (alist, asum):
    aset = set(alist)         1
    for v in alist:           N
        if asum-v in aset     N
            return(v,asum-v)  N
    return None                1
```

(b) $3N^2 + N + 1$

(b) $3N + 2$

(c) N^2

(c) N

(d)

5. (a) $T(N) \sim cN(\log N)^2$
 $T(1000) \sim c1000(\log 1000)^2 \sim 0.003$
 $c \cdot 1000 \cdot 100 \sim 0.003$
 $c \cdot 100000 \sim 0.003$
 $c \sim 3 \cdot (10)^{-7}$
 formula: $T(N) \sim 3 \cdot (10)^{-7} \cdot N \cdot (\log N)^2$

(b) $1000000/1000 = 1000$
 $\text{time} = 3 \cdot (10)^{-7} \cdot 1000 + 1000 \cdot 0.003$
 $\text{time} = 3.0003$

6.

N = Problem Size	Complexity Class	Time to Solve on Old Machine (secs)	M Solvable in the same Time on a New Machine 10x as Fast
10^6	$O(\log_2 N)$	1	$2^{(10 \cdot \log_2(10^6))}$
10^6	$O(N)$	1	10×10^6
10^6	$O(N \log_2 N)$	1	$(2^{((10^7) \cdot \log_2(10^6))})$
10^6	$O(N^2)$	1	$(10^{(13)})$ square root