



南开大学
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半同态加密应用实践实验报告

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1. 实验要求

基于Paillier算法实现隐私信息获取:从服务器给定的 m 个消息中获取其中一个，不得向服务器泄露获取了哪一个消息，同时客户端能完成获取消息的解密。

扩展实验:有能力的同学可以在客户端保存对称密钥 k ，在服务器端存储 m 个用对称密钥 k 加密的密文，通过隐私信息获取方法得到指定密文后能解密得到对应的明文。

2. 实验过程

2.1 安装环境

1. 安装python环境在 Windows 下安装 python 开发环境。到官方网站

<https://www.python.org/downloads/> 下载 windows 版本的 python 安装包。下载后双击安装即可。提示：安装过程一定要勾选“Add python.exe to PATH”，这样会使得安装后的 python 程序路径直接加入到系统的环境变量中，在控制台可以直接使用 python 命令。如果忘记勾选，则需要通过“我的电脑”->右键“属性”->“高级系统设置”->“环境变量”的 path 中将安装的路径手动填入。

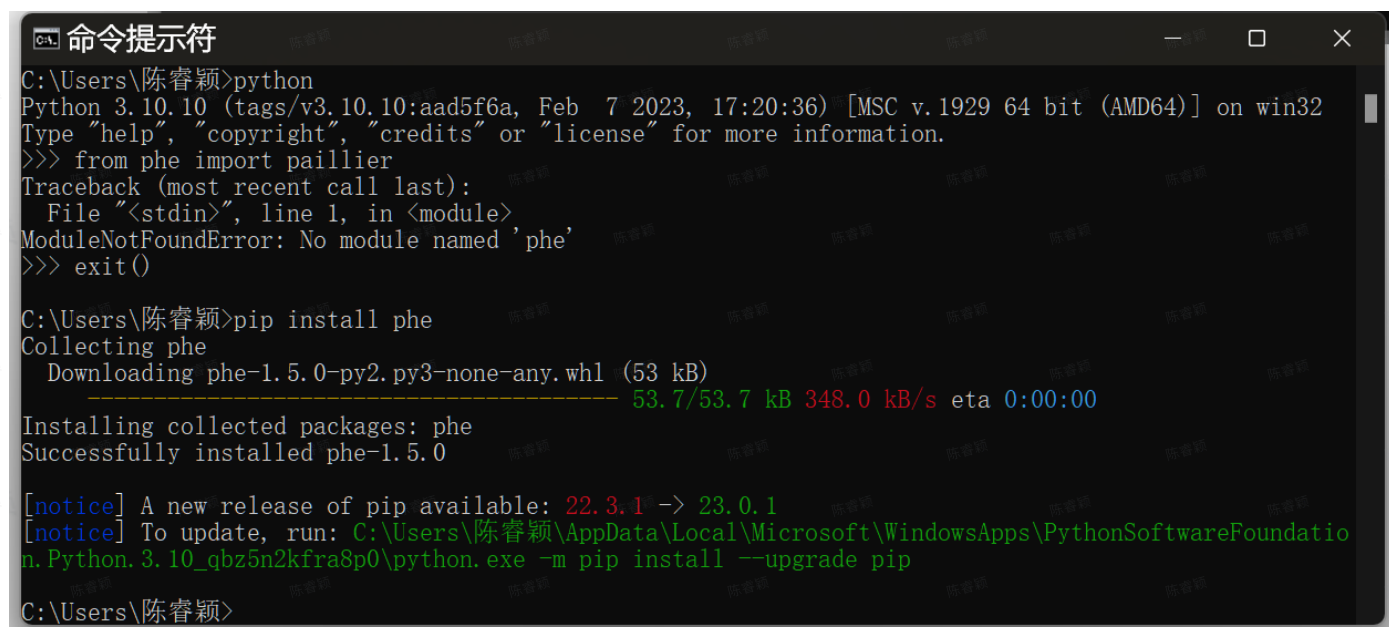
安装完毕，打开控制台，输入 `python` 命令，会显示：



```
命令提示符 - python
Microsoft Windows [版本 10.0.22621.1265]
(c) Microsoft Corporation。保留所有权利。

C:\Users\陈睿颖>python
Python 3.10.10 (tags/v3.10.10:aad5f6a, Feb  7 2023, 17:20:36) [MSC v.1929 64 bit (AMD64)] on win32
Type "help", "copyright", "credits" or "license" for more information.
>>> _
```

2. 安装 phe 库 输入命令：`pip install phe` 完成 phe 库的安装。



```
命令提示符
C:\Users\陈睿颖>python
Python 3.10.10 (tags/v3.10.10:aad5f6a, Feb  7 2023, 17:20:36) [MSC v.1929 64 bit (AMD64)] on win32
Type "help", "copyright", "credits" or "license" for more information.
>>> from phe import paillier
Traceback (most recent call last):
  File "<stdin>", line 1, in <module>
ModuleNotFoundError: No module named 'phe'
>>> exit()

C:\Users\陈睿颖>pip install phe
Collecting phe
  Downloading phe-1.5.0-py2.py3-none-any.whl (53 kB)
----- 53.7/53.7 kB 348.0 kB/s eta 0:00:00
Installing collected packages: phe
Successfully installed phe-1.5.0

[notice] A new release of pip available: 22.3.1 -> 23.0.1
[notice] To update, run: C:\Users\陈睿颖\AppData\Local\Microsoft\WindowsApps\PythonSoftwareFoundation.Python.3.10_qbz5n2kfra8p0\python.exe -m pip install --upgrade pip

C:\Users\陈睿颖>
```

3. 验证环境的正确性

```
命令提示符 - python
n.Python.3.10_qbz5n2kfra8p0\python.exe -m pip install --upgrade pip

C:\Users\陈睿颖>python
Python 3.10.10 (tags/v3.10.10:aad5f6a, Feb 7 2023, 17:20:36) [MSC v.1929 64 bit (AMD64)] on win32
Type "help", "copyright", "credits" or "license" for more information.
>>> from phe import paillier
>>>
```

没有报错，正确！

2.2 基于 Python 的 phe 库完成加法和标量乘法的验证

使用的代码如下：

```
1 from phe import paillier # 开源库
2 import time # 做性能测试
3
4 ##### 设置参数
5 print("默认私钥大小: ", paillier.DEFAULT_KEYSIZE)
6 #生成公私钥
7 public_key, private_key = paillier.generate_paillier_keypair()
8 # 测试需要加密的数据
9 message_list = [3.1415926,100,-4.6e-12]
10
11 ##### 加密操作
12 time_start_enc = time.time()
13 encrypted_message_list = [public_key.encrypt(m) for m in message_list]
14 time_end_enc = time.time()
15 print("加密耗时s: ",time_end_enc-time_start_enc)
16 print("加密数据 (3.1415926) :",encrypted_message_list[0].ciphertext())
17
18 ##### 解密操作
19 time_start_dec = time.time()
20 decrypted_message_list = [private_key.decrypt(c) for c in encrypted_message_list]
21 time_end_dec = time.time()
22 print("解密耗时s: ",time_end_dec-time_start_dec)
23 print("原始数据 (3.1415926) :",decrypted_message_list[0])
24
25 ##### 测试加法和乘法同态
```

```
26 a,b,c = encrypted_message_list # a,b,c分别为对应密文
27 a_sum = a + 5 # 密文加明文, 已经重载了+运算符
28 a_sub = a - 3 # 密文加明文的相反数, 已经重载了-运算符
29 b_mul = b * 6 # 密文乘明文, 数乘
30 c_div = c / -10.0 # 密文乘明文的倒数
31
32 print("a+5 密文:",a.ciphertext()) # 密文纯文本形式
33 print("a+5=",private_key.decrypt(a_sum))
34 print("a-3=",private_key.decrypt(a_sub))
35 print("b*6=",private_key.decrypt(b_mul))
36 print("c/-10.0=",private_key.decrypt(c_div))
37
38 ##密文加密文
39 print((private_key.decrypt(a)+private_key.decrypt(b))==private_key.decrypt(a+b))
40 #报错, 不支持a*b, 即两个密文直接相乘
41 #print((private_key.decrypt(a)+private_key.decrypt(b))==private_key.decrypt(a*b))
42
```

运行结果如图所示:

```

IDLE Shell 3.10.10
File Edit Shell Debug Options Window Help
>>>
===== RESTART: D:\MyFiles\data security\test1.py =====
默认私钥大小: 3072
加密耗时s: 0.8625626564025879
加密数据 (3.1415926) : 836880651419730288245181682857985016338485670898718278234
80373771140459943749858361512160577315046723773657845401816081610801597944541365
86127321175397706303008247325514842113296551971026085169002554139397470177039354
48890810699604596956400120200629797627126961789993623131541799970183516160505656
79387342268595449639791630178620576322948997088955252694698441340454672726659594
45269545203119390549102143728850242275504638421787803275525612576952382290568318
95978621115743943240472899210014888230169411498064424595474785230684720873761491
00116353502519844109030734290282610619680991885064715904604068961423560413366292
68028534486277314156496776423696463692721740350485589512258778656254565351054900
34284568386229857163561424792303615352403350127123217234499756450530460487947929
95401565111025188806995104053441092828058027021814950652454832533757067907241852
19625953916489865206626928330783344456657285229502647140361203502591281936671839
36063665313204352464631656658646888391198305272614544910086527720190870584708135
68725103067912840219308167954130252199535694851884081111536135811926460151526083
73716565813315812566684693674138469683162513631582888969428924157270283054766696
3569691488849934002215955721148171610390408910080856648792857188981783217022877
64922536177079903477765886596878085037373531026797602857865574607017402706609195
83368460560007250122948978629435692579277589066588582080345783012778303425575414
64407760136812791337057194540631247490185745771375097153164214550185133237488495
20261331383662543052208046759355751360153368471851751937658475062581641466559364
47989885682581554894369471093052005532740216585481168570326219628650900881840139
51538195728363732638642919306482678555291512987767334145849422768457985347271011
80249504940447248578139460155139134049235089370081364209716904937171750080389117
71114426518661060023142769892584
解密耗时s: 0.2369976043701172
原始数据 (3.1415926) : 3.1415926
a+5 密文: 8368806514197302882451816828579850163384856708987182782348037377114045
99437498583615121605773150467237736578454018160816108015979445413658612732117539
77063030082473255148421132965519710260851690025541393974701770393544889081069960
45969564001202006297976271269617899936231315417999701835161605056567938734226859
54496397916301786205763229489970889552526946984413404546727266595944526954520311
93905491021437288502422755046384217878032755256125769523822905683189597862111574
39432404728992100148882301694114980644245954747852306847208737614910011635350251
98441090307342902826106196809918850647159046040689614235604133662926802853448627
73141564967764236964636927217403504855895122587786562545653510549003428456838622
98571635614247923036153524033501271232172344997564505304604879479299540156511102

```

2.3 基于 Python 的 phe 库完成隐私信息获取的功能

服务器端拥有多个数值，要求客户端能基于 Paillier 实现从服务器读取一个指定的数值并正确解密，但服务器不知道所读取的是哪一个。

基于 Paillier 协议进行设计：由于数值“0”的密文与任意数值的标量乘也是 0，数值“1”的密文与任意数值的标量乘将是数值本身。

设计如下：

服务器端：产生数据列表 $\text{data_list}=\{m_1, m_2, \dots, m_n\}$

客户端：

- 设置要选择的数据位置为 pos
- 生成选择向量 $\text{select_list}=\{0,...,1,...,0\}$ ，其中，仅有 pos 的位置为 1
- 生成密文向量 $\text{enc_list}=\{E(0),..., E(1),..., E(0)\}$
- 发送密文向量 enc_list 给服务器

服务器端：

- 将数据与对应的向量相乘后累加得到密文 $c = m_1 * \text{enc_list}[1] + ... + m_n * \text{enc_list}[n]$
- 返回密文 c 给客户端

客户端：解密密文 c 得到想要的结果

具体代码实现如下：

```

1 from phe import paillier # 开源库
2 import random # 选择随机数
3
4 ##### 设置参数
5 # 服务器端保存的数值
6 message_list = [100,200,300,400,500,600,700,800,900,1000]
7 length = len(message_list)
8 # 客户端生成公私钥
9 public_key, private_key = paillier.generate_paillier_keypair()
10 # 客户端随机选择一个要读的位置
11 pos = random.randint(0,length-1)
12 print("要读起的数值位置为: ",pos)
13
14 ##### 客户端生成密文选择向量
15 select_list=[]
16 enc_list=[]
17 for i in range(length):
18     select_list.append( i == pos )
19     enc_list.append( public_key.encrypt(select_list[i]) )
20
21 # for element in select_list:
22 #     print(element)
23 # for element in enc_list:
24 #     print(private_key.decrypt(element))
25
26 ##### 服务器端进行运算
27 c=0
28 for i in range(length):
29     c = c + message_list[i] * enc_list[i]
30 print("产生密文: ",c.ciphertext())

```



```

31
32 ##### 客户端进行解密
33 m=private_key.decrypt(c)
34 print("得到数值:",m)
35

```

如图所示：



```

IDLE Shell 3.10.10
File Edit Shell Debug Options Window Help
Python 3.10.10 (tags/v3.10.10:aad5f6a, Feb 7 2023, 17:20:36) [MSC v.1929 64 bit
(AMD64)] on win32
Type "help", "copyright", "credits" or "license()" for more information.
>>> ##### RESTART: D:\MyFiles\data security\test.py #####
要读起的数值位置为： 7
产生密文： 117857625478825833632130291639522661814706091049209968992914681646684
75408309375974111233956385004108551969325724601443231778579932451259773915523367
69694257022732768435318156245861920011096177980950798325265593474426659796177370
30445507726847298054913662237051845210811284219551744303194070775965930091280063
13175569414573047456785957501171471363412050933459570458170582377373997560461207
92076485215649697403296276188117073488808379626811404591306283273965043706096750
23305150498559588392502443938277564277512355469264400425534422295229070190029657
11145115855937452613837318676649246203930274793901504737825568953570885291540011
31112112030984662461090970227731931620341806568469234941906418643495950294797603
50127471325806444977022695269337866769165751894874228480801300250566568538123846
49101044429288164568272907858867896046487184874098410554887818703025443687675930
35617124292235321572269304249851354124549057141694177414576185164671262532124282
90527036272662658342152071292597444819142406351176427725328472390342442569078874
89160995851070712632151891233996665768866739078515502984118103021680925809584670
84311675128965852762799298770338947921342652766363435036863852271755837998309635
15463046082899817721397064516780230937257877696704469211864401537213229347248715
22063445028911712636068785777035282684675304871677983005935549491365308547462217
07273865750761960457608536206832279661026754720120894901813787118408582794269668
59076411376536480088573751370460138570801893653576671565478000899655276629640774
93303089560721945495495093603157205743219836310560084267940417181603801430124918
91644332805884308527202772286235126078213027218283683524010012243040990670312399
18420043480189770721713770635387343677927980051277871121052473943914555003979459
74085049267092714027644068972066677562185044472215838982538771839622309250105729
7902196419984372587
得到数值： 800

```

2.4 扩展实验

在客户端保存对称密钥k，在服务器端存储m个用对称密钥k加密的密文，通过隐私信息获取方法得到指定密文后能解密得到对应的明文。

首先要使用如下命令安装：

```

1 pip3 install pycryptodome
2
3 pip3 install crypto
4

```

```
5 pip3 install pycrypto
```

```
6
```

python3的PyCryptodome库用于密码学，是一个低级密码基元的独立Python包，常见对称密码在Crypto.Cipher 库下，主要有：DES 3DES AES RC4 Salsa20，这次我们使用的是AES。

可参照前面两个实验，仿照编写代码如下：

```
1 from phe import paillier # 开源库
2 from Crypto.Cipher import AES
3 import random # 选择随机数
4
5 ##### 设置参数
6 # 服务器端保存的数值
7 plaintext_list = [
8     b'0123456789abcdef',
9     b'qwertyuiopasdfgh',
10    b'-----nku-----',
11    b'thisisalabreport',
12    b'**chenruiying** '
13 ]
14 ciphertext_list = []
15 ciphernum_list = []
16 symmetric_key = b'-----nku-----'
17 aes = AES.new(symmetric_key, AES.MODE_ECB) # 创建一个aes对象
18 for text in plaintext_list:
19     ciphertext_list.append(aes.encrypt(text)) # 加密明文
20     ciphernum_list.append(int.from_bytes(text, byteorder='big'))
21
22 for element in ciphertext_list:
23     print(element)
24
25 length = len(ciphertext_list)
26 # 客户端生成公私钥
27 public_key, private_key = paillier.generate_paillier_keypair()
28 # 客户端随机选择一个要读的位置
29 pos = random.randint(0, length - 1)
30 print("要读起的数值位置为：", pos)
31
32 ##### 客户端生成密文选择向量
33 select_list = []
34 enc_list = []
35 for i in range(length):
36     select_list.append(i == pos)
37     enc_list.append(public_key.encrypt(select_list[i]))
```



```

38
39 for element in select_list:
40     print(element)
41 for element in enc_list:
42     print(element)
43 for element in enc_list:
44     print(private_key.decrypt(element))
45
46 ##### 服务器端进行运算
47 c = 0
48 for i in range(length):
49     c = c + ciphernum_list[i] * enc_list[i]
50 print("产生密文: ", c.ciphertext())
51
52 ##### 客户端进行解密
53 m = private_key.decrypt(c)
54 print("得到数值: ", m)
55
56 message = m.to_bytes(16, byteorder='big')
57 x = aes.decrypt(message)
58 print(message)
59

```

运行结果如下:

```

IDLE Shell 3.10.10
File Edit Shell Debug Options Window Help
>>> ===== RESTART: D:\MyFiles\data security\symmetricEnc.py =====
b'\x02\x0b\xe5\xd5\x0f\xb1\xe0\x1e\x11\x03\xd0\xfb#\xca\xf9'
b'\xb8\x9c1\xaem\x1e\xabW\xe7\x12\xecj\xd5\xd1\x84\xa0'
b'\N\xcb\xbcUc\xed\xd4\x8f\x02\x1e\xe5\x1eY\xa8\xd7\xdd'
b'!\x93\xe5\x14$\xac\x9e\x84\xe4\x06\x08h7f\t\xe7'
b'\xdb\x16\x83\xb6\xef\xca\x08\xa8c\xb4p\x93\x0c\x97\x8f8'
要读起的数值位置为: 2
False
False
True
False
False
<phe.paillier.EncryptedNumber object at 0x000001C61FBAF340>
<phe.paillier.EncryptedNumber object at 0x000001C61FBAF370>
<phe.paillier.EncryptedNumber object at 0x000001C61FBAF3D0>
<phe.paillier.EncryptedNumber object at 0x000001C61FBAF400>
<phe.paillier.EncryptedNumber object at 0x000001C61FBAF460>
0
0
1
0
0
产生密文:  454619451039933775818166518501336377389910400497745366588492697809717009765855967919922442894490557274776609144209954703786587
99432256789006712343997036556414050152067697180611753399897768108618633735190729936058475613221077714745365519336916162614681373388989303
80610322661185973248896769401170854161326997972371483537351415441465126717533161018017324209308868033375925534636382480286693138477519330
45315636660976597659756025956674073902154821505018571020876972869864600129272876373026580832653897408409378160828516448249830187927881759
74412752816214338413025144714063298396446660746785897089368517405765716003380360428921674873501059145578707553767045305596954954885627175
17628733388694979130973502441196161576514570709831116356914137036283528502947684178715204705737817608218937144576188301935020373010889342
72678616833759864580780603078977358608604864715483062908845691225059279885100286520768701239615862026331110275509434641205820906657115594
21535868369500757795203193800628427633196066434882753640372625561534397210153776202893657578139922166401451028139280429403153454909330445
46934029179883425871505526892738218561335917247281579319204368292619479902700701021582558029255242404534978279757620095039955681278796032
98749349832971013035300991612967850738984418220230417802905417297049356177759485504158517589113047245396726555869231516820880878663182847
18931810578718301499372752991996243128487328528768010418628830016143387272986634208014252549702703877086650743796419922389687417838534799
14622851947033417177320519670418130993308802642091185999094091432098017226967553748228508464003278133408169255636520034700581717472225587
72782719592930261351074066701484430399825456758784431581106228650705835256456346426778952836535058442622408550504518119415536691040679743
9883260362218590951286266821034939834243094886324989168152084123183630804589765
得到数值:  60049829456636507537420831885032762669
b'-----nku-----'
>>>
>>>
>>>

```

解密完成！

3. 心得体会

- 复习了python环境的安装，学习了phe库的安装
- 在实验2.2中，学会了基于 Paillier 协议进行设计：由于数值“0”的密文与任意数值的标量乘也是0，数值“1”的密文与任意数值的标量乘将是数值本身
- 尝试完成了扩展实验，了解了包PyCryptodome，学会了其安装及使用方法