#### **Problem Statement**

Supposed that the Government is planning to open a Volunteer-Run Trap-Neuter-Return (TNR) facility, we would like to know which Queue type I,  $i \in \{Priority Queue (PQ), Shortest Queue (SQ)\}$ , is the most effective one for transporting the cat into the TNR stations at the facility.

Each TNR facility has 3 stations. When a stray cat arrives to the TNR facility, they will queue before entering a TNR station. There are two Queue types, Priority Queue (PQ), Shortest Queue (SQ). For Priority Queue the stray cats will prioritise queue in the West, followed by central then the east. For Shortest Queue the stray cats will enter the station with the lowest queue size at that moment.

For each station, there are 2 Volunteers. At the start of initialization, both workers are already in queue. Due to the TNR machine limitation, only a single worker may operate it at a time. The machine has a processing rate of about 5 seconds. For the neutering process to occur, the following conditions must be met: 1 volunteer,1 needle and 1 stray must be present in the queues. While one worker operates, the other watches from behind. After a worker has finish operation, he proceeds to take a break. The worker waiting behind moves up the queue and follows the same set of conditions to start operation.

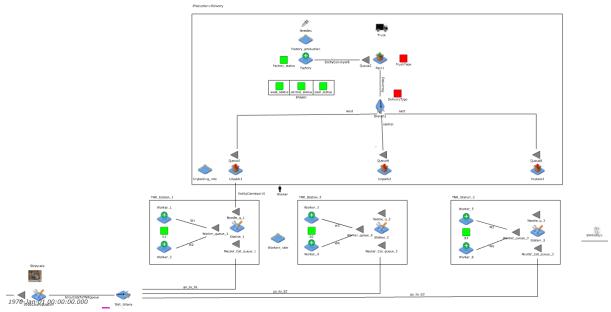
The needles are delivered to the TNR station at a

Supposed that each Volunteers only work 1 hour per day in the TNR facility and Volunteers work at a working rate normally distribution at  $V^N(\mu_V=3 \text{ min}, \sigma_V=5 \text{ min})$ , Stray Cats gets transported into the TNR stations at a normal distribution of  $C^N(\mu_C=5s,\sigma_C=20s)$ 

**Needles delivery** 

Stray cat dying

#### Simulating Effectiveness of TNR



#### Output Analysis #1

We would like to compare which queueing type, Priority Queue type or Shortest Queue type is the most efficient one.

#### Approach

We will do a hypothesis testing with  $\alpha$ = 0.05 to see whether there is a difference in the average queueing time between the two different Queue types.

Let  $\mu_{PQ}$  be the expected average queueing time measure from the Priority Queue type.

Let  $\mu_{SO}$  be the expected average queueing time measure from the Shortest Queue type.

Let  $H_0$  be the hypothesis that there is no difference between the expected average queueing time measure from the Priority Queue type and the expected average queueing time measure from the Shortest Queue type.

Let  $H_1$  be the hypothesis that there is a difference between the expected average queueing time measure from the Priority Queue type and the expected average queueing time measure from the Shortest Queue type.

$$H_0$$
:  $\mu_{PQ} - \mu_{SQ} = 0$   
 $H_1$ :  $\mu_{PO} - \mu_{SO} \neq 0$ 

The average queueing time of stray cats for queueing in each TNR station for both Queue types are run 100 times each, each run lasting for an hour.

Let  $x_{i,k,j}$  be the average queueing time of stray cats in respective Queue type  $i \in \{Priority Queue (PQ), Shortest Queue (SQ)\}$ , Station  $k \in \{1,2,3\}$ , with run  $j \in \{1,2,3,....,100\}$ 

We then find the average queueing time for each Queueing type across the 3 stations to be  $X_{i,j}$  where:  $X_{i,j} = x_{i,1,j} + x_{i,2,j} + x_{i,3,j}$ 

Let  $Z_j = X_{PQ,j} - X_{SQ,j}$  to be the difference between the two Queueing types

With  $Z_j$  we can identify a confidence interval of  $\zeta=\mu_{PQ_j}-\mu_{SQ_j}$  such that  $E(Z_j)=\zeta$ 

Let 
$$\bar{Z}_j = \frac{1}{j} \sum_1^j Z_j$$
 be the sample mean,

Let 
$$\hat{\sigma}_j^2 = \frac{1}{j-1} \sum_1^j \! \left( Z_j - \bar{Z}_j \right)^2$$
 be the sample variance

 $95\%\,$  confidence interval for  $\mu_{PQ}-\mu_{SQ}$  is

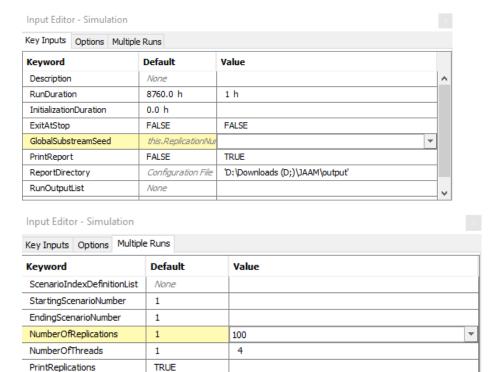
$$\left(\bar{Z}_j - t_{j-1,\frac{\alpha}{2}} * \frac{\hat{\sigma}_j}{\sqrt{j}}, \bar{Z}_j + t_{j-1,\frac{\alpha}{2}} * \frac{\hat{\sigma}_j}{\sqrt{j}}\right)$$

There is 3 possible outcomes:

- 1) If '0' lies within the confidence interval, it means that both Queue types are equally efficient.
- 2) If '0' lies to the left of the confidence interval, it means that PQ is more efficient than SQ
- 3) If '0' lies to the right of the confidence interval, it means that SQ is more efficient than PQ

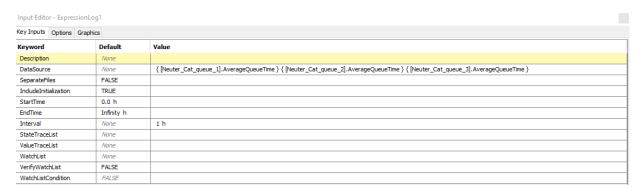
#### Data collected from simulation

**Common Random Number:** To ensure that we can compare the two Queuing types with better confidence, we subject both queueing types to the same random conditions. This is done through setting the attribute 'NumberOfReplication' in the Global Variable 'Simulation' to 100. This means that the 100 unique seeds use for the 100 runs for PQ will be the same 100 unique seeds use for the 100 runs for SQ. The 'ReportDirecttory' is where the data file will be stored.



FALSE

The expression logger creates a txt file that logs all the average queue time data after an hour.



The data is then exported into an excel file for data wrangling and analysis.

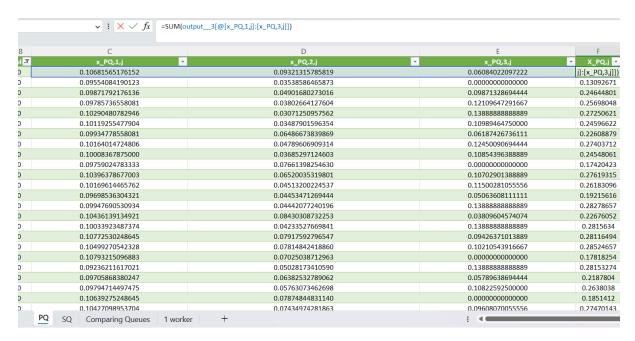
**Priority Queue** 

PrintConfidenceIntervals

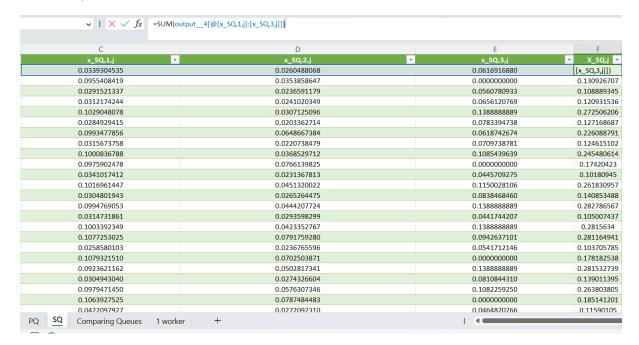
PrintRunLabels

TRUE

TRUE



#### **Shortest Queue**



X_PQ_j		۸	D	C	D	Г	Г		
2	4				U	Е	Г		
3	1	X_PQ,j	X_SQ,j	Z					
4 0.246448 0.108889 0.137559	2	0.260869	0.121671	0.13919	8	Zbar	0.03075		
Description	3	0.130927	0.130927		0	sigma	0.057032		
6 0.272506 0.272506 0	4	0.246448	0.108889	0.13755	9	t_0.025,99	2.276003		
7 0.245966 0.127169 0.118798 8 0.226089 0.226089 0 9 0.274037 0.124615 0.149422 10 0.245481 0.245481 0 11 0.174204 0.174204 0 12 0.276193 0.101809 0.174384 13 0.261831 0.261831 0 14 0.192156 0.140853 0.051303 15 0.282787 0.822787 0 16 0.226761 0.105007 0.121753 17 0.281563 0.281563 0 18 0.281165 0.281165 0 19 0.285247 0.103706 0.181541 20 0.178183 0.178183 0 21 0.281533 0.281533 0 22 0.21878 0.139011 0.079769 10 0.281563 0.281563 0 10 0.21878 0.139011 0.079769 11	5	0.25698	0.120932	0.13604	9	Low CI	0.017769		
8	6	0.272506	0.272506		0	High CI	0.04373		
9 0.274037 0.124615 0.149422	7	0.245966	0.127169	0.11879	8				
10	8	0.226089	0.226089		0				
11	9	0.274037	0.124615	0.14942	.2				
11	10	0.245481	0.245481		0				
12					-				
13					-				
14				0.17430					
15				0.05120	-				
16				0.05130					
17 0.281563 0.281563 0 0 1 18 0.281165 0.281165 0 0 1 19 0.285247 0.103706 0.181541 20 0.178183 0.178183 0 0 2 21 0.281533 0.281533 0 0 2 22 0.21878 0.139011 0.079769 2 23 0.260869030591926 0.121670948316017 = A2-B2					-				
18									
19 0.285247 0.103706 0.181541 20 0.178183 0.281533 0.281533 0 21 0.281533 0.281533 0 22 0.21878 0.139011 0.079769  E16 V I X Q, J Z 2 0.260869030591926 0.121670948316017 =A2-B2 Zbar =AVERAGE(C2:C10 1.30926706559965 0.130926706559965 0.130926706559965 -A3-B3 sigma =STDEV.S(C2:C101 1.30926706559965 0.130926706559965 -A4-B4 t_0.025,99 =T.INV.27(0.05,99)					0				
20 0.178183 0.178183 0 0 21 0.281533 0.281533 0 0 22 0.21878 0.139011 0.079769  E16	18	0.281165	0.281165		0				
21 0.281533 0.281533 0 0 0 0.774037153856919 0.17420423037963 0.1742042303	19	0.285247	0.103706	0.18154	1				
22  0.21878  0.139011  0.079769	20	0.178183	0.178183		0				
E16	21	0.281533	0.281533		0				
A B C D E F  X_PQ,j X_SQ,j Z 2 0.260869030591926 0.121670948316017 =A2-B2 Zbar =AVERAGE(C2:C10 3 0.130926706559965 0.130926706559965   A3-B3 sigma =STDEV.S(C2:C101 4 0.24648011435967 0.108889344802366   A4-B4	22	0.21878	0.139011	0.07976	i9				
A B C D E F  X_PQ,j X_SQ,j Z  0.260869030591926 0.121670948316017 =A2-B2 Zbar =AVERAGE(C2:C10 3 0.130926706559965 0.130926706559965 =A3-B3 sigma =5TDEV.S(C2:C101 4 0.246448011435967 0.108889344802366 =A4-B4 t_0.025,99 =T.INV.ZT(0.05,99) 5 0.256980479773516 0.120931536189106 =A5-B5 Low CI =F2-F4*F3/SQRT(J 6 0.272506206293962 0.272506206293962 =A6-B6 High CI =F2+F4*F3/SQRT(J 7 0.245966218242582 0.127168686714703 =A7-B7 8 0.226088791340612 0.226088791340612 =A8-B8 9 0.274037123285643 0.124615101701929 =A9-B9 10 0.24548061388492 0.24548061388492 =A10-B10 11 0.17420423037963 0.17420423037963 =A11-B11 20 0.276193153856919 0.101809450007936 =A11-B11 40 0.192156156848765 0.140853487865206 =A41-B14 5 0.28278656600192 0.282786566600192 =A15-B15 5 0.28278656600192 0.282786566600192 =A15-B15 16 0.226760524412478 0.105007436729995 =A16-B16 17 0.281563400461038 0.281164940590803 -A18-B18 18 0.281164940590803 0.281164940590803 =A18-B18 19 0.285246568778542 0.103705784549176 =A19-B19	22		0.000004		_				
1         X_PQ,j         X_SQ,j         Z           2         0.260869030591926         0.121670948316017         =A2-B2         Zbar         =AVERAGE(C2:C10           3         0.130926706559965         0.130926706559965         -A3-B3         sigma         =STDEV.S(C2:C101           4         0.246448011435967         0.108889344802366         -A4-B4         t_0.025,99         =T.INV.2T(0.05,99)           5         0.256980479773516         0.120931536189106         -A5-B5         Low CI         =F2-F4*F3/SQRT(J           6         0.227506206293962         0.272506206293962         -A6-B6         High CI         =F2+F4*F3/SQRT(J           7         0.245966218242582         0.127168686714703         -A7-B7         -A8-B8         -A9-B9           8         0.226088791340612         0.226088791340612         -A8-B8         -A9-B9         -A10-B10           10         0.24548061388492         0.24548061388492         0.24548061388492         -A10-B10         -A10-B10         -A10-B10           12         0.276193153856919         0.101809450007936         -A12-B12         -A13-B13         -A13-B13           14         0.192156156848765         0.140853487865206         -A14-B14         -A15-B15         -A16-B16           15	E16		<b>v</b> !	$\times \checkmark f_{x}$					
2 0.260869030591926 0.121670948316017 =A2-B2 Zbar =AVERAGE(C2:C10 3 0.130926706559965 0.130926706559965 =A3-B3 sigma =STDEV.S(C2:C101 4 0.246448011435967 0.108889344802366 =A4-B4 t_0.025,99 =T.INV.2T(0.05,99) 5 0.256980479773516 0.120931536189106 =A5-B5 Low CI =F2-F4*F3/SQRT(J 6 0.272506206293962 0.272506206293962 =A6-B6 High CI =F2+F4*F3/SQRT(J 7 0.245966218242582 0.127168686714703 =A7-B7 8 0.226088791340612 0.226088791340612 =A8-B8 9 0.274037123285643 0.124615101701929 =A9-B9 10 0.24548061388492 0.24548061388492 =A10-B10 10 1.7420423037963 0.17420423037963 =A11-B11 12 0.276193153856919 0.101809450007936 =A11-B11 13 0.261830957458547 0.261830957458547 =A13-B13 14 0.192156156848765 0.140853487865206 =A14-B14 15 0.282786566600192 0.282786566600192 =A15-B15 16 0.226760524412478 0.105007436729995 =A16-B16 17 0.281563400461038 0.281563400461038 -A17-B17 18 0.281164940590803 0.281164940590803 =A18-B18 19 0.285246568778542 0.103705784549176 =A19-B19		А	E	3	С	D		Е	F
3       0.130926706559965       0.130926706559965       =A3-B3       sigma       =STDEV.S(C2:C101         4       0.246448011435967       0.108889344802366       =A4-B4       t_0.025,99       =T.INV.2T(0.05,99)         5       0.256980479773516       0.120931536189106       =A5-B5       Low CI       =F2-F4*F3/SQRT(J         6       0.272506206293962       0.272506206293962       =A6-B6       High CI       =F2+F4*F3/SQRT(J         7       0.245966218242582       0.127168686714703       =A7-B7       =A8-B8       =A9-B9         9       0.274037123285643       0.124615101701929       =A9-B9       =A10-B10       =A11-B11         10       0.17420423037963       0.17420423037963       =A11-B11       =A12-B12       =A13-B13         12       0.261830957458547       0.261830957458547       0.261830957458547       A14-B14       =A13-B13         15       0.282786566600192       0.282786566600192       -A15-B15       =A16-B16       =A16-B16         16       0.281563400461038       0.281563400461038       -A18-B18       =A18-B18         19       0.2825246568778542       0.103705784549176       =A18-B19       =A19-B19									
4       0.246448011435967       0.108889344802366       =A4-B4       t_0.025,99       =T.INV.2T(0.05,99)         5       0.256980479773516       0.120931536189106       -A5-B5       Low CI       =F2-F4*F3/SQRT(J         6       0.272506206293962       0.272506206293962       -A6-B6       High CI       =F2+F4*F3/SQRT(J         7       0.245966218242582       0.127168686714703       -A7-B7       -A8-B8         9       0.274037123285643       0.124615101701929       -A9-B9       -A9-B9         10       0.17420423037963       0.17420423037963       -A11-B11       -A12-B12         12       0.261830957458547       0.261830957458547       -A13-B13       -A13-B13         14       0.192156156848765       0.140853487865206       -A14-B14       -A15-B15         15       0.282786566600192       0.282786566600192       -A15-B15       -A16-B16         17       0.281563400461038       0.281164940590803       0.281164940590803       0.281164940590803       -A18-B18         19       0.285246568778542       0.103705784549176       -A19-B19									=AVERAGE(C2:C101
5       0.256980479773516       0.120931536189106       =A5-B5       Low CI       =F2-F4*F3/SQRT(J         6       0.272506206293962       0.272506206293962       -A6-B6       High CI       =F2+F4*F3/SQRT(J         7       0.245966218242582       0.127168686714703       -A7-B7       -A8-B8         8       0.226088791340612       -A8-B8       -A9-B9         9       0.24548061388492       -A10-B10       -A1-B11         10       0.17420423037963       0.17420423037963       -A11-B11         12       0.261830957458547       0.261830957458547       -A13-B13         14       0.192156156848765       0.140853487865206       -A14-B14         15       0.282786566600192       0.282786566600192       -A15-B15         16       0.281563400461038       0.281164940590803       0.281164940590803       0.281164940590803         18       0.2825246568778542       0.103705784549176       -A19-B19								•	, ,
6 0.272506206293962 0.272506206293962								9	
7       0.245966218242582       0.127168686714703       =A7-B7         8       0.226088791340612       0.226088791340612       =A8-B8         9       0.274037123285643       0.124615101701929       =A9-B9         10       0.17420423037963       0.17420423037963       =A11-B10         12       0.276193153856919       0.101809450007936       =A12-B12         13       0.261830957458547       0.261830957458547       =A13-B13         14       0.192156156848765       0.140853487865206       =A14-B14         15       0.282786566600192       0.282786566600192       =A15-B15         16       0.226760524412478       0.105007436729995       =A16-B16         17       0.281563400461038       0.281164940590803       0.281164940590803       0.281164940590803         18       0.2825246568778542       0.103705784549176       =A19-B19									
8       0.226088791340612       0.226088791340612       =A8-B8         9       0.274037123285643       0.124615101701929       =A9-B9         10       0.24548061388492       0.24548061388492       =A10-B10         11       0.17420423037963       0.17420423037963       =A11-B11         12       0.261830957458547       0.261830957458547       =A12-B12         13       0.192156156848765       0.140853487865206       =A14-B14         15       0.282786566600192       0.282786566600192       =A15-B15         16       0.226760524412478       0.105007436729995       =A16-B16         17       0.281563400461038       0.281164940590803       0.281164940590803       0.281164940590803         18       0.285246568778542       0.103705784549176       =A19-B19							Tilgir Ci		-12114 13/30(11(3)
9 0.274037123285643 0.124615101701929 =A9-B9 10 0.24548061388492 0.24548061388492 =A10-B10 11 0.17420423037963 0.17420423037963 =A11-B11 12 0.276193153856919 0.101809450007936 =A12-B12 13 0.261830957458547 0.261830957458547 =A13-B13 14 0.192156156848765 0.140853487865206 =A14-B14 15 0.282786566600192 0.282786566600192 =A15-B15 16 0.226760524412478 0.105007436729995 =A16-B16 17 0.281563400461038 0.281563400461038 =A17-B17 18 0.281164940590803 0.281164940590803 =A18-B18 19 0.285246568778542 0.103705784549176 =A19-B19									
11       0.17420423037963       0.17420423037963       =A11-B11         12       0.276193153856919       0.101809450007936       =A12-B12         13       0.261830957458547       0.261830957458547       =A13-B13         14       0.192156156848765       0.140853487865206       =A14-B14         15       0.282786566600192       0.282786566600192       =A15-B15         16       0.226760524412478       0.105007436729995       =A16-B16         17       0.281563400461038       0.281563400461038       =A17-B17         18       0.281164940590803       0.281164940590803       -A18-B18         19       0.285246568778542       0.103705784549176       =A19-B19	9 0	.274037123285	643 0.1246151	01701929 =/	49-B9				
12     0.276193153856919     0.101809450007936     =A12-B12       13     0.261830957458547     0.261830957458547     =A13-B13       14     0.192156156848765     0.140853487865206     =A14-B14       15     0.282786566600192     0.282786566600192     -A15-B15       16     0.226760524412478     0.105007436729995     =A16-B16       17     0.281563400461038     0.281563400461038     -A17-B17       18     0.281164940590803     0.281164940590803     -A18-B18       19     0.285246568778542     0.103705784549176     -A19-B19	10 0	.245480613884	92 0.2454806	1388492 =/	A10-B10				
13     0.261830957458547     0.261830957458547     =A13-B13       14     0.192156156848765     0.140853487865206     =A14-B14       15     0.282786566600192     0.282786566600192     =A15-B15       16     0.226760524412478     0.105007436729995     =A16-B16       17     0.281563400461038     0.281563400461038     =A17-B17       18     0.281164940590803     0.281164940590803     -A18-B18       19     0.285246568778542     0.103705784549176     =A19-B19	11 0			3037963 =	A11-B11				
14     0.192156156848765     0.140853487865206     =A14-B14       15     0.282786566600192     0.282786566600192     =A15-B15       16     0.226760524412478     0.105007436729995     =A16-B16       17     0.281563400461038     0.281563400461038     =A17-B17       18     0.281164940590803     0.281164940590803     -A18-B18       19     0.285246568778542     0.103705784549176     =A19-B19									
15     0.282786566600192     0.282786566600192     =A15-B15       16     0.226760524412478     0.105007436729995     =A16-B16       17     0.281563400461038     0.281563400461038     =A17-B17       18     0.281164940590803     0.281164940590803     =A18-B18       19     0.285246568778542     0.103705784549176     =A19-B19		201020057450	547 0.2618309						
16     0.226760524412478     0.105007436729995     =A16-B16       17     0.281563400461038     0.281563400461038     =A17-B17       18     0.281164940590803     0.281164940590803     =A18-B18       19     0.285246568778542     0.103705784549176     =A19-B19			36E 6		\1/LQ1/I				
17 0.281563400461038 0.281563400461038 =A17-B17 18 0.281164940590803 0.281164940590803 =A18-B18 19 0.285246568778542 0.103705784549176 =A19-B19	14 0	.192156156848							
18	14 0 15 0	.192156156848 .282786566600	192 0.2827865	66600192 =	A15-B15				
19 0.285246568778542 0.103705784549176 =A19-B19	14 0. 15 0. 16 0.	.192156156848 .282786566600 .226760524412	192 0.2827865 478 0.1050074	66600192 = A 36729995 = A	A15-B15 A16-B16				
	14 0. 15 0. 16 0. 17 0.	.192156156848 .282786566600 .226760524412 .281563400461	192 0.2827865 478 0.1050074 038 0.2815634	66600192 = A 36729995 = A 00461038 = A	A15-B15 A16-B16 A17-B17				
	14 0. 15 0. 16 0. 17 0. 18 0.	192156156848 282786566600 226760524412 281563400461 281164940590	192 0.2827865 478 0.1050074 038 0.2815634 803 0.2811649	66600192 = / 36729995 = / 00461038 = / 40590803 = /	A15-B15 A16-B16 A17-B17 A18-B18				

# Output result:

95% confidence interval for  $\mu_{PQ}-\mu_{SQ}$  is (0.019433 ,0.042066)

Since 0 lies to the left of the confidence interval, PQ is more efficient than SQ.

#### Output Analysis #2

We would like to find out what number of workers for each station for Priority Queue type and Shortest Queue type is the most efficient one for different Delivery Types

#### **Approach**

We will plot a graph of 100 unique runs lasting for an hour each for average queueing time vs different number of workers.

Let  $u_{i,k,d,w,j}$  be the average queueing time of stray cats in respective Queue type  $i \in \{Priority Queue (PQ), Shortest Queue (SQ)\}$ , Station  $k \in \{1,2,3\}$ , Delivery type  $d \in \{Priority Delivery (PD), Shortest Delivery (SD)\}$ , number of workers in respective station  $w \in Z^+$ , with run  $j \in \{1,2,3,...,100\}$ 

We then find the average queueing time for each station over 100 unique runs to be  $U_{i,k,d,w}$  where:  $U_{i,k,d,w}=\frac{1}{100}\sum_{j=1}^{100}u_{i,k,d,w,j}$ 

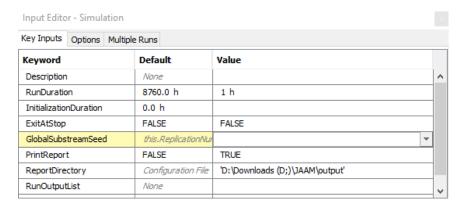
Allowing us to arrive to all possible combinations of outputs with varying w:

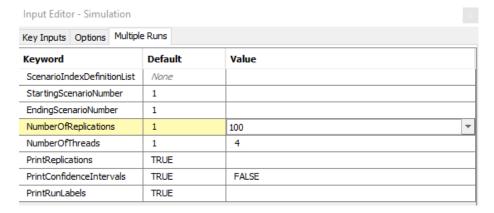
- 1.  $U_{PO,1,PD,w}$  vs  $U_{PO,2,PD,w}$  vs  $U_{PO,3,PD,w}$
- 2.  $U_{SO,1,PD,w}$  vs  $U_{SO,2,PD,w}$  vs  $U_{SO,3,PD,w}$
- 3.  $U_{PQ,1,SD,W}$  vs  $U_{PQ,2,SD,W}$  vs  $U_{PQ,3,SD,W}$
- 4.  $U_{SQ,1,SD,w}$  vs  $U_{SQ,2,SD,w}$  vs  $U_{SQ,3,SD,w}$

We can then plot a line graph of each combination with varying w to help us find which number w would provide us with the smallest queueing time for respective station.

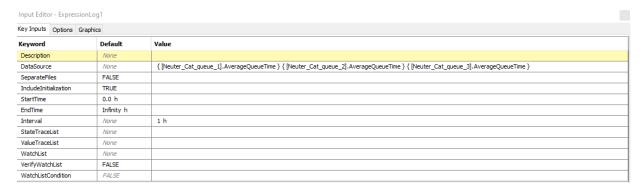
#### Data collected from simulation

**Common Random Number:** To ensure that we can compare the two Queuing types with better confidence, we subject both queueing types to the same random conditions. This is done through setting the attribute 'NumberOfReplication' in the Global Variable 'Simulation' to 100. This means that the 100 unique seeds use for the 100 runs for PQ will be the same 100 unique seeds use for the 100 runs for SQ. The 'ReportDirecttory' is where the data file will be stored.





The expression logger creates a txt file that logs all the average queue time data after an hour.

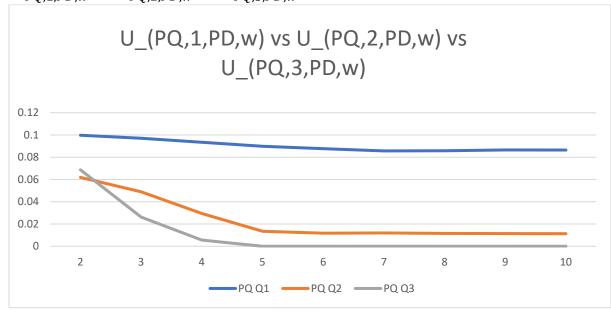


The data is then exported into an excel file for data wrangling and analysis.

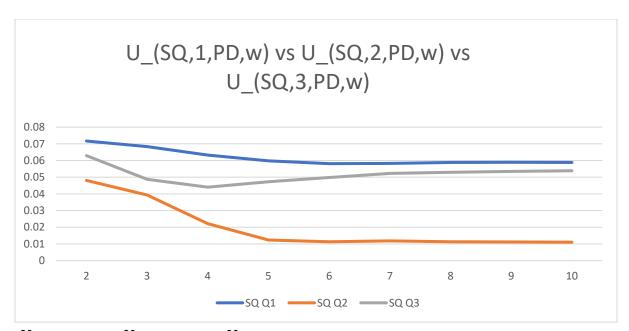
	Α		В		С		D		Е		F		G	
1	Truck						PD							
2	Station				PQ						SQ			
3	#worker	rs	Q1		Q2		Q3		Q1		Q2		Q3	
4		2	0.099	978	0.06	519	0.06	587	0.07	168	0.048	806	0.062	293
5		3	0.09	708	0.048	394	0.026	523	0.068	833	0.03	393	0.048	372
6		4	0.0	935	0.029	943	0.005	556	0.063	327	0.022	214	0.044	103
7		5	0.089	984	0.013	349		0	0.059	981	0.012	238	0.047	728
8		6	0.08	774	0.013	175		0	0.058	811	0.013	132	0.049	982
9		7	0.0	857	0.013	198		0	0.058	326	0.013	181	0.052	228
10		8	0.08	585	0.013	153		0	0.058	886	0.03	113	0.052	292
11		9	0.08658		0.013	141	.41 0		0.058	895	0.01	121	0.053	345
12		10	0.08	648	0.013	129	0		0.058	882	0.01	107	0.053	384
Tru	ck						S	D						
	tion				PQ		SQ							
	orkers	Q1		Q2	ı Q	Q3		Q1		Q2	JQ	Q3		
,,,,,,	2		09983		06206		06667		07037		04687		0.0639	
	3		09724		04896		02382		06822		03885		03764	
	4		09364		02924		00498		06326		02147		03604	
	5		08984		01346	0.	00-50		05971		01224		04059	
	6		08774				0		05661		01224		05517	
	7		08539		01173		0		05675		01173		05544	
	8		08604		01105		0		05552		01108		05929	
	9		08656				_		05552		01108			
	_				0.0109		0						05809	
	10	U.	08658	U.	01077		0	U.	05698	(	0.0111	U.	05772	

# Y-axis: average Queuing time , X-axis: # of workers

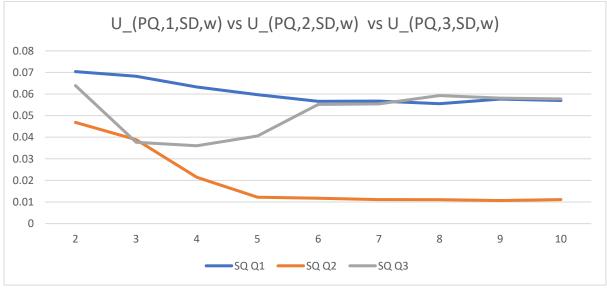
1.  $U_{PQ,1,PD,w}$  vs  $U_{PQ,2,PD,w}$  vs  $U_{PQ,3,PD,w}$ 



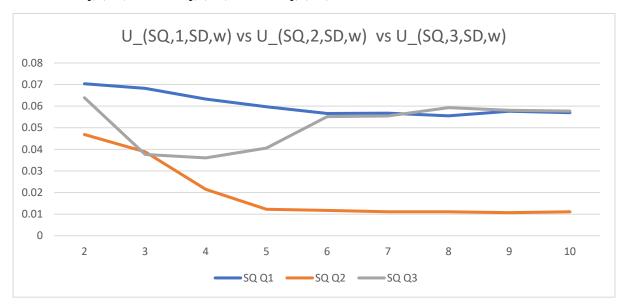
2.  $\overline{U_{SQ,1,PD,w}}$  vs  $U_{SQ,2,PD,w}$  vs  $U_{SQ,3,PD,w}$ 



# 3. $U_{PQ,1,SD,w}$ vs $U_{PQ,2,SD,w}$ vs $U_{PQ,3,SD,w}$



# 4. $U_{SQ,1,SD,w}$ vs $U_{SQ,2,SD,w}$ vs $U_{SQ,3,SD,w}$

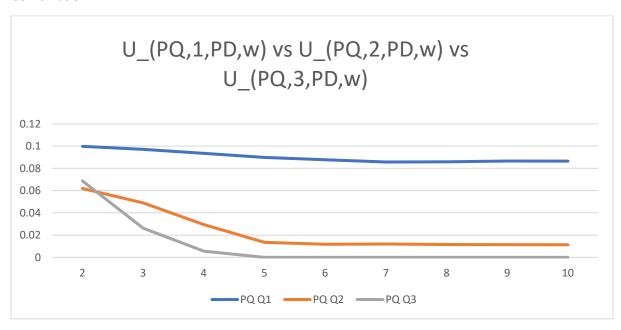


#### Output result:

Across all four combinations we noticed that combination 1 and 2 can provide the relatively lower average queueing time. Hence, we will now compare combination 1 and 2 with varying workers for each station.

Let  $w_{stnk}$  be the number of workers in station k that has the lowest average waiting time by referring to the lowest value of the y axis of the plot.

#### Combination 1:



	P1			
w_stn1, w_stn2, w_stn3	Q1	Q2	Q3	Sum of all average queueing times across stations
7, 5, 4	0.08603	0.01371	0	0.099738677
5, 5, 5	0.08984	0.01349	0	0.103334303

#### Combination 2



	SQ			
w_stn1, w_stn2, w_stn3	Q1	Q2	Q3	Sum of all average queueing times across stations
5, 5, 4	0.05957	0.01282	0.04741	0.119803795
5, 5, 5	0.05981	0.01238	0.04728	0.119474796
5, 5, 7	0.06207	0.01327	0.04109	0.116430403
2, 4, 2	0.06963	0.02961	0.08444	0.183687457
5, 2, 5	0.06256	0.02996	0.02704	0.119562799

We then sum across the stations and found out that the lowest average queueing type is 0.0997 with combination of  $U_{PQ,1,PD,7}$  vs  $U_{PQ,2,PD,5}$  vs  $U_{PQ,3,PD,4}$ 

# Output Analysis #3

Jaamsim allows users to directly infer output data with the graph function. Users are able change inputs before the simulation start, or anytime during the simulation to get different output results.

These are the following User Inputs in Jaamsim:

Initial_State_Inputs	Value(s)
Abandon Rate Min inflation	2
Abandon Rate Max inflation Green: High Demand for Cats Red: Low Demand for Cats	10  Click_To_Change_DemandType_button

TNR\_Stations\_Inputs

11417_2	TNK_Stations_Inputs					
	No. Of Workers	Max Queue Leng	gth Service Rate	Safety stock		
Stn1	2	5	5 s	10		
Stn2	2	5	5 s	10		
Stn3	2	5	5 s	10		
	n: ShortestQueue Priority Q1		Click_To_change_Qu	ieueTypeButton		
Green: High Workers Speed Rate Red: Low Workers Speed Rate			Click_To_Change_Worker	sSpeedType_button		
	n: High Unpackain Low Unpacking Sp		Click_To_Change_Unpack	ng≲peedType_button		

Factory_Inputs	Value(s)
Reorder quantity	20
Green: High Factory ProdRate Red: Low Factory ProdRate	Click_To_Change_WorkType
Green: ShortestQueue Red: Priority Queue	Click_To_Change_DeliveryType
Black: Fast Delivery Red: Slow Delivery	Click_To_Change_TruckSpeedButton

Outputs that users can infer from:

Outputs	Value(s)
Average queuing time Stn1	0.05629485909722222[h]
Average queuing time Stn2	0.08381247055555556[h]
Average queuing time Stn3	0.09526216298611112[h]
# Angel Zombies	{7.0}
# Zombies	{2.0}
# of Mega-Zombies	{0.0}

#### Approach

We can experiment with **one control variable** (High demand of cats) and have other different user inputs to get different outputs:

#### Experiment #1:

- All Green and Black button for high speed, fast delivery, high demand of cats
- Pause Simulation at 24hrs,
- Priority Queue
- Priority Delivery

#### Experiment #2:

- All Red button for low speed, slow delivery
- Keep Demand button Green for high demand for cats
- Pause Simulation at 24hrs,
- Priority Queue
- Priority Delivery

# Output result:

# Experiment #1

# Inputs:

Initial_State_Inputs	Value(s)
Abandon Rate Min inflation	2
Abandon Rate Max inflation	10
Green: High Demand for Cats Red: Low Demand for Cats	Click_Te_Change_DemandType_button

TNR_S	Stations_Inputs				
	No. Of Workers	Max Queue Ler	ngth	Service Rate	Safety stock
Stn1	2	5		5 s	10
Stn2	2	5		5 s	10
Stn3	2	5		5 s	10
Green: ShortestQueue Red: Priority Q1				Click_To_change_Q	ueveTypeButton •
	Green: High Workers Speed Rate Red: Low Workers Speed Rate			Click_To_Change_Works	rrsSpeedType_button
	ı: High Unpackain Low Unpacking S <sub>l</sub>	D .		Click_To_Change_Unpac	kingSpeedType_button

Factory_Inputs	Value(s)
Reorder quantity	20
Green: High Factory ProdRate Red: Low Factory ProdRate	Click_To_Change_WorkType
Green: ShortestQueue Red: Priority Queue	Click_To_Change_DeliveryType
Black: Fast Delivery Red: Slow Delivery	Click_To_Change_TruckSpeedButton

# Outputs:

Outputs	Value(s)
Average queuing time Stn1	0.01597928673421846[h]
Average queuing time Stn2	0.0069831941877350106[h]
Average queuing time Stn3	0.006756855256813419[h]
# Angel Zombies	{1912.0}
# Zombies	{4.0}
# of Mega-Zombies	{0.0}

### Experiment #2

### Inputs:

Initial_State_Inputs	Value(s)
Abandon Rate Min inflation	2
Abandon Rate Max inflation	10
Green: High Demand for Cats Red: Low Demand for Cats	Click_To_Change_DemandType_button

TNR_Stations_Inputs					
	No. Of Workers	Max Queue Length	Service Rate	Safety stock	
Stn1	2	5	5 s	10	
Stn2	2	5	5 s	10	
Stn3	2	5	5 s	10	
Green: ShortestQueue Red: Priority Q1			Click_To_change_QueueTypeButton		
Green: High Workers Speed Rate Red: Low Workers Speed Rate			Click_To_Change_WorkersSpeedType_button		
Green: High Unpackaing Speed Rate Red: Low Unpacking Speed Rate			Click_To_Change_Unpack	ingSpeedType_button	

Factory_Inputs	Value(s)
Reorder quantity	20
Green: High Factory ProdRate Red: Low Factory ProdRate	Click_To_Change_WorkType
Green: ShortestQueue Red: Priority Queue	Click_To_Change_DeliveryType
Black: Fast Delivery Red: Slow Delivery	Circk_To_Change_TruckSpeedButton

### Outputs:

Outputs	Value(s)	
Average queuing time Stn1	0.12137927857962974[h]	
Average queuing time Stn2	0.11729497007762933[h]	
Average queuing time Stn3	0.003663646739690723[h]	
# Angel Zombies	{1347.0}	
# Zombies	{560.0}	
# of Mega-Zombies	{27.0}	

Comparing Experiment 1 and Experiment 2 with a control variable of high demand of cats suggests that with a working rate, delivery speed, and factory production rate affects the average queueing

time for the all stations, and decrease the number of cats getting neutered (higher number of zombies).

# Other possible Output analysis:

- Using Priority Queue, compare the average queueing rate for having 2 slow workers for all 3 stations and 1 fast worker for all 3 stations.
- Using Priority Queue and Shortest Delivery repeat the experiment for Output analysis #1.
- Using Shortest Queue and Shortest Delivery repeat the experiment for Output analysis #1.