

## 1. Introduction.

# Implementing the Fuzzy c-Means Algorithm

by Gagarine Yaikhom

This program is in the public domain.

A clustering algorithm organises items into groups based on a similarity criteria. The Fuzzy c-Means algorithm is a clustering algorithm where each item may belong to more than one group (hence the word ‘fuzzy’), where the degree of membership for each item is given by a probability distribution over the clusters.

**2. About.** This program was written by Gagarine Yaikhom in September 2010 when he started learning CWEB. It is in the public domain. Please send comments and suggestions to [gyaikhom@gmail.com](mailto:gyaikhom@gmail.com).

CWEB is a system for “literate programming” that was created by Donald E. Knuth and Silvio Levy. Further details are available [here](#).

**3. Fuzzy c-Means Algorithm.** The fuzzy c-means (FCM) algorithm is a clustering algorithm developed by Dunn, and later on improved by Bezdek. It is useful when the required number of clusters are pre-determined; thus, the algorithm tries to put each of the data points to one of the clusters. What makes FCM different is that it does not decide the absolute membership of a data point to a given cluster; instead, it calculates the likelihood (the degree of membership) that a data point will belong to that cluster. Hence, depending on the accuracy of the clustering that is required in practice, appropriate tolerance measures can be put in place. Since the absolute membership is not calculated, FCM can be extremely fast because the number of iterations required to achieve a specific clustering exercise corresponds to the required accuracy.

**4. Iterations.** In each iteration of the FCM algorithm, the following objective function  $J$  is minimised:

$$J = \sum_{i=1}^N \sum_{j=1}^C \delta_{ij} \|x_i - c_j\|^2 \quad (1)$$

Here,  $N$  is the number of data points,  $C$  is the number of clusters required,  $c_j$  is the centre vector for cluster  $j$ , and  $\delta_{ij}$  is the degree of membership for the  $i$ th data point  $x_i$  in cluster  $j$ . The norm,  $\|x_i - c_j\|$  measures the similarity (or closeness) of the data point  $x_i$  to the centre vector  $c_j$  of cluster  $j$ . Note that, in each iteration, the algorithm maintains a centre vector for each of the clusters. These data-points are calculated as the weighted average of the data-points, where the weights are given by the degrees of membership.

**5. Degree of membership.** For a given data point  $x_i$ , the degree of its membership to cluster  $j$  is calculated as follows:

$$\delta_{ij} = \frac{1}{\sum_{k=1}^C \left( \frac{\|x_i - c_j\|}{\|x_i - c_k\|} \right)^{\frac{2}{m-1}}} \quad (2)$$

where,  $m$  is the fuzziness coefficient and the centre vector  $c_j$  is calculated as follows:

$$c_j = \frac{\sum_{i=1}^N \delta_{ij}^m \cdot x_i}{\sum_{i=1}^N \delta_{ij}^m} \quad (3)$$

In equation (3) above,  $\delta_{ij}$  is the value of the degree of membership calculated in the previous iteration. Note that at the start of the algorithm, the degree of membership for data point  $i$  to cluster  $j$  is initialised with a random value  $\theta_{ij}$ ,  $0 \leq \theta_{ij} \leq 1$ , such that  $\sum_j \delta_{ij} = 1$ .

**6. Fuzziness coefficient.** In equations (2) and (3) the fuzziness coefficient  $m$ , where  $1 \leq m < \infty$ , measures the tolerance of the required clustering. This value determines how much the clusters can overlap with one another. The higher the value of  $m$ , the larger the overlap between clusters. In other words, the higher the fuzziness coefficient the algorithm uses, a larger number of data points will fall inside a ‘fuzzy’ band where the degree of membership is neither 0 nor 1, but somewhere in between.

**7. Termination condition.** The required accuracy of the degree of membership determines the number of iterations completed by the FCM algorithm. This measure of accuracy is calculated using the degree of membership from one iteration to the next, taking the largest of these values across all data points considering all of the clusters. If we represent the measure of accuracy between iteration  $k$  and  $k + 1$  with  $\epsilon$ , we calculate its value as follows:

$$\epsilon = \Delta_i^N \Delta_j^C |\delta_{ij}^{k+1} - \delta_{ij}^k| \quad (4)$$

where,  $\delta_{ij}^k$  and  $\delta_{ij}^{k+1}$  are respectively the degree of membership at iteration  $k$  and  $k + 1$ , and the operator  $\Delta$ , when supplied a vector of values, returns the largest value in that vector.

**8. Errata.** *Wed Nov 13 20:22:26 GMT 2013* HyunJun Park pointed out missing *fuzziness* in equation (3). This is now fixed. Fortunately, the program source code did not contain this error.

**9. FCM Program.** Program `fcm` expects an input file, which contains the parameters for running the FCM algorithm. This input can be easily generated with the related program `gen`.

```

< Include system libraries 19 >;
< Declare global variables 10 >;
< Define global functions 18 >;
int main(int argc, char **argv)
{
    < Print usage information 44 >;
    fcm(argv[1]);    /* run fuzzy c-means algorithm */
    < Print post processing information 45 >;
    return 0;
}

```

**10. Global variables and constants.** The `fcm` program, upon execution, uses several global variables. These variables are the parameters required by the algorithm, and are normally initialised with values from the input data file generated by the `gen` program.

Variable `num_data_points` is initialised with the number of data points to be clustered; whereas, variable `num_clusters` is initialised with the number of clusters required. The FCM algorithm discovers clusters according to a preset number of clusters, in contrast to discovering an arbitrary number of clusters.

```

#define MAX_DATA_POINTS 10000    /* maximum number of data points */
#define MAX_CLUSTER 100          /* maximum number of clusters */
< Declare global variables 10 > ≡
    int num_data_points;
    int num_clusters;

```

See also sections 11, 12, 13, 14, 15, 16, and 17.

This code is used in section 9.

**11.** Variable `num_dimensions` is initialised to the number of dimensions each data point has. For instance, if we are clustering cartesian points in the two-dimensional Euclidean plane, we will have `num_dimensions`  $\equiv$  2.

```

#define MAX_DATA_DIMENSION 5      /* maximum number of data-point dimensions */
< Declare global variables 10 > +=
    int num_dimensions;

```

**12.** For every data point, the value that a dimension can take is bounded. We use a two dimensional matrix, `low_high`, to store the low and high values for each dimension. Every data point must fall within this value range.

```

< Declare global variables 10 > +=
    double low_high[MAX_DATA_DIMENSION][2];

```

**13.** A two dimensional array, `degree_of_memb`, stores the degree of membership for each of the data points to each of the clusters. Thus, for instance, `degree_of_memb[i][j]` gives a measure of how likely the data point  $i$  will belong to cluster  $j$ . This matrix is updated dynamically during the iterations.

```

< Declare global variables 10 > +=
    double degree_of_memb[MAX_DATA_POINTS][MAX_CLUSTER];

```

**14.** The clustering algorithm uses a measure of accuracy, *epsilon*, to judge whether a clustering exercise can be judged satisfactory. This eventually determines the number of iterations that must be executed before the algorithm terminates.

```
< Declare global variables 10 > +=
    double epsilon;    /* termination criterion */
```

**15.** The degree of fuzziness, *fuzziness*, gives a measure of tolerance while carrying out the clustering exercise, and therefore, affects the degree of membership calculations.

```
< Declare global variables 10 > +=
    double fuzziness;
```

**16.** Every data point has a coordinate  $(x_1, x_2, \dots, x_d)$  given by an ordered set of values corresponding to each of the dimensions (where  $d$  gives the highest dimension for a data point). This coordinate depends on the number of dimensions which each data point must have. For instance, for points on a real line, the number of dimensions is 1. For points on the plane, the number of dimensions is 2, where each data point is represented by their 2D-coordinate, e.g.,  $(x, y)$ . For points inside a volume, the number of dimensions is 3, where each data point is represented by their 3D-coordinate, e.g.  $(x, y, z)$ . This implementation of the FCM algorithm works with any number of dimensions less than `MAX_DATA_DIMENSION`.

```
< Declare global variables 10 > +=
    double data_point[MAX_DATA_POINTS][MAX_DATA_DIMENSION];
```

**17.** For each of the clusters, a temporary centre point is maintained during each of the iterations. The centre points for all of the clusters are maintained as a two dimensional array (each row representing a vector in the same coordinate system as the data points). The values stored in this array are updated during the iterations depending on the degree of membership of the data points to each of the clusters.

```
< Declare global variables 10 > +=
    double cluster_centre[MAX_CLUSTER][MAX_DATA_DIMENSION];
```

**18. Initialisation.** Function *init* initialises the execution parameters by parsing the input data file. It takes as input argument the name of the input data file, *fname*, and returns 0 if the initialisation was successful. Otherwise, -1 is returned.

```
< Define global functions 18 > ≡
    int init(char *fname)
    {
        int i, j, r, rval;
        FILE *f;
        double t, s;

        < Open input file 29 >;
        < Read number of data points, clusters and dimensions 30 >;
        < Read fuzziness coefficients 31 >;
        < Read required accuracy 32 >;
        < Initialise data points 33 >;
        < Initialise degree of membership matrix 20 >;
        fclose(f);
        return 0;
    failure: fclose(f);
        exit(1);
    }
```

See also sections 21, 24, 25, 26, 27, 37, 46, and 48.

This code is used in section 9.

**19. Randomise degree-of-membership matrix.** We use a random number generator to initialise the degree of membership before applying the FCM algorithm. To do this, we use the function `rand()` from the standard `math` library.

```
<Include system libraries 19> ≡
#include <math.h>
```

See also section 50.

This code is used in section 9.

**20.** For every data point, in relation to one of the clusters, we assign a random probability that the point will belong to that cluster. The value is a real number between 0.0 and 1.0 inclusive. Since the sum of the probabilities for all of the clusters for a given data point should be 1.0, we adjust the probability of the first cluster after we have assigned probabilities for all of the remaining clusters.

```
<Initialise degree of membership matrix 20> ≡
for (i = 0; i < num_data_points; i++) {
    s = 0.0; /* probability sum */
    r = 100; /* remaining probability */
    for (j = 1; j < num_clusters; j++) {
        rval = rand() % (r + 1);
        r -= rval;
        degree_of_memb[i][j] = rval/100.0;
        s += degree_of_memb[i][j];
    }
    degree_of_memb[i][0] = 1.0 - s;
}
```

This code is used in section 18.

**21. Calculation of centre vectors.** Function `calculate_centre_vectors` updates the centre vectors for each of the clusters. The aim of the algorithm is to continue updating this centre of vectors until it is close to the actual value. The closeness to the actual value is determined by the termination criterion (epsilon).

```
<Define global functions 18> +=
int calculate_centre_vectors()
{
    int i, j, k;
    double numerator, denominator;
    double t[MAX_DATA_POINTS][MAX_CLUSTER];
    <Precompute powers of degree of membership 22>;
    <Calculate centre vectors 23>;
    return 0;
}
```

**22.** Precompute powers of degree-of-membership. The values calculated here are used in two parts of the following calculation of centre of vectors. We have moved the computation of powers here to reuse the values, so that we don't have to calculate the powers again. Calculation of powers are expensive.

```
<Precompute powers of degree of membership 22> ≡
for (i = 0; i < num_data_points; i++) {
    for (j = 0; j < num_clusters; j++) {
        t[i][j] = pow(degree_of_memb[i][j], fuzziness);
    }
}
```

This code is used in section 21.

**23.**  $\langle$  Calculate centre vectors 23  $\rangle \equiv$

```

for (j = 0; j < num_clusters; j++) {
    for (k = 0; k < num_dimensions; k++) {
        numerator = 0.0;
        denominator = 0.0;
        for (i = 0; i < num_data_points; i++) {
            numerator += t[i][j] * data_point[i][k];
            denominator += t[i][j];
        }
        cluster_centre[j][k] = numerator / denominator;
    }
}

```

This code is used in section 21.

**24. Calculation of norm.** Function *get\_norm* is one of the most important calculations of the FCM algorithm. It determines the closeness of a data point to the centre of vectors for a given cluster. The calculation of the norm depends on the number of dimensions the data points have.

$\langle$  Define global functions 18  $\rangle + \equiv$

```

double get_norm(int i, int j)
{
    int k;
    double sum = 0.0;
    for (k = 0; k < num_dimensions; k++) {
        sum += pow(data_point[i][k] - cluster_centre[j][k], 2);
    }
    return sqrt(sum);
}

```

**25. Update degree of membership.** Function *get\_new\_value* calculates the new degree of membership for the data point *i* in cluster *j*.

$\langle$  Define global functions 18  $\rangle + \equiv$

```

double get_new_value(int i, int j)
{
    int k;
    double t, p, sum;
    sum = 0.0;
    p = 2 / (fuzziness - 1);
    for (k = 0; k < num_clusters; k++) {
        t = get_norm(i, j) / get_norm(i, k);
        t = pow(t, p);
        sum += t;
    }
    return 1.0 / sum;
}

```

**26.** Function *update\_degree\_of\_membership* updated the degree-of-membership values for all of the data points. Since we want to stop the iteration when all of the points are close enough to one of the centre of vectors, this function returns the maximum difference between the old value and the new value, so that it can be checked against the termination condition.

```

⟨Define global functions 18⟩ +=
double update_degree_of_membership()
{
    int i, j;
    double new_uj;
    double max_diff = 0.0, diff;
    for (j = 0; j < num_clusters; j++) {
        for (i = 0; i < num_data_points; i++) {
            new_uj = get_new_value(i, j);
            diff = new_uj - degree_of_memb[i][j];
            if (diff > max_diff) max_diff = diff;
            degree_of_memb[i][j] = new_uj;
        }
    }
    return max_diff;
}

```

**27. The FCM algorithm.** Function *fcm* encapsulates the main phases of the FCM algorithm. It contains the skeleton of the algorithm, which corresponds to the mathematical description in the introduction.

```

⟨Define global functions 18⟩ +=
int fcm(char *fname)
{
    double max_diff;
    init(fname);
    do {
        calculate_centre_vectors();
        max_diff = update_degree_of_membership();
    } while (max_diff > epsilon);
    return 0;
}

```

**28. Input.** This sections lists the input functions and code segments that are used for reading initialisation values, parameters from the input data file.

```

29. ⟨Open input file 29⟩ ≡
if ((f = fopen(fname, "r")) == Λ) {
    printf("Failed to open input file.");
    return -1;
}

```

This code is used in section 18.

**30.**  $\langle \text{Read number of data points, clusters and dimensions } 30 \rangle \equiv$

```

fscanf(f, "%d%d%d", &num_data_points, &num_clusters, &num_dimensions);
if (num_clusters > MAX_CLUSTER) {
    printf("Number_of_clusters_should_be_<_%d\n", MAX_CLUSTER);
    goto failure;
}
if (num_data_points > MAX_DATA_POINTS) {
    printf("Number_of_data_points_should_be_<_%d\n", MAX_DATA_POINTS);
    goto failure;
}
if (num_dimensions > MAX_DATA_DIMENSION) {
    printf("Number_of_dimensions_should_be_>=1.0_and_<_%d\n", MAX_DATA_DIMENSION);
    goto failure;
}

```

This code is used in section 18.

**31.**  $\langle \text{Read fuzziness coefficients } 31 \rangle \equiv$

```

fscanf(f, "%lf", &fuzziness);
if (fuzziness ≤ 1.0) {
    printf("Fuzzyness_coefficient_should_be_>1.0\n");
    goto failure;
}

```

This code is used in section 18.

**32.**  $\langle \text{Read required accuracy } 32 \rangle \equiv$

```

fscanf(f, "%lf", &epsilon);
if (epsilon ≤ 0.0 ∨ epsilon > 1.0) {
    printf("Termination_criterion_should_be_>0.0_and_≤1.0\n");
    goto failure;
}

```

This code is used in section 18.

**33.**  $\langle \text{Initialise data points } 33 \rangle \equiv$

```

for (i = 0; i < num_data_points; i++) {
    for (j = 0; j < num_dimensions; j++) {
        fscanf(f, "%lf", &data_point[i][j]);
        if (data_point[i][j] < low_high[j][0]) low_high[j][0] = data_point[i][j];
        if (data_point[i][j] > low_high[j][1]) low_high[j][1] = data_point[i][j];
    }
}

```

This code is used in section 18.

**34. Output.** This sections lists the output functions and code segments that are used when printing output, error messages, etc. either to the standard output stream, of an output file.

**35.**  $\langle \text{Open output file } 35 \rangle \equiv$

```

if (fname ≡ Λ) f = stdout;
else if ((f = fopen(fname, "w")) ≡ Λ) {
    printf("Cannot_create_output_file.\n");
    exit(1);
}

```

This code is used in sections 46 and 48.



**36.**  $\langle$  Print execution parameters 36  $\rangle \equiv$

```
printf("Number_of_data_points:_%d\n", num_data_points);
printf("Number_of_clusters:_%d\n", num_clusters);
printf("Number_of_data-point_dimensions:_%d\n", num_dimensions);
printf("Accuracy_margin:_%lf\n", epsilon);
```

This code is used in section 45.

**37.** This function outputs the current membership matrix so that it can be plotted using Gnuplot. For information on Gnuplot, Google gnuplot. NOTE: This will only work when the number of dimensions is 2. That is the points are on a plane. This may be extended for higher dimensions.

$\langle$  Define global functions 18  $\rangle + \equiv$

```
int gnuplot_membership_matrix()
{
    int i, j, cluster;
    char fname[100];
    double highest;
    FILE *f[MAX_CLUSTER];
     $\langle$  Check number of dimensions is 2 38  $\rangle$ ;
     $\langle$  Create data file for each cluster 39  $\rangle$ ;
     $\langle$  Send data points to respective cluster data file 41  $\rangle$ ;
     $\langle$  Close the cluster data files 42  $\rangle$ ;
     $\langle$  Write the gnuplot script 43  $\rangle$ ;
    return 0;
}
```

**38.**  $\langle$  Check number of dimensions is 2 38  $\rangle \equiv$

```
if (num_dimensions  $\neq$  2) {
    printf("Plotting_the_cluster_only_works_when_the\n");
    printf("number_of_dimensions_is_two.This_will_create\n");
    printf("a_two-dimensional_plot_of_the_cluster_points.\n");
    exit(1);
}
```

This code is used in section 37.

**39.** We create a separate file for each of the clusters. Each file contains data points that has the highest degree of membership.

$\langle$  Create data file for each cluster 39  $\rangle \equiv$

```
for (j = 0; j < num_clusters; j++) {
    sprintf(fname, "cluster.%d", j);
    if ((f[j] = fopen(fname, "w"))  $\equiv$   $\Lambda$ ) {
        printf("Could_not_create%s\n", fname);
         $\langle$  Cleanup cluster data files and return 40  $\rangle$ ;
    }
    fprintf(f[j], "#Data_points_for_cluster:_%d\n", j);
}
```

This code is used in section 37.

40.  $\langle$  Cleanup cluster data files and return 40  $\rangle \equiv$

```
for (i = 0; i < j; i++) {
    fclose(f[i]);
    sprintf(fname, "cluster.%d", i);
    remove(fname);
}
return -1;
```

This code is used in sections 39 and 43.

41.  $\langle$  Send data points to respective cluster data file 41  $\rangle \equiv$

```
for (i = 0; i < num_data_points; i++) {
    cluster = 0;
    highest = 0.0;
    for (j = 0; j < num_clusters; j++) {
        if (degree_of_memb[i][j] > highest) {
            highest = degree_of_memb[i][j];
            cluster = j;
        }
    }
    fprintf(f[cluster], "%lf_%lf\n", data_point[i][0], data_point[i][1]);
}
```

This code is used in section 37.

42.  $\langle$  Close the cluster data files 42  $\rangle \equiv$

```
for (j = 0; j < num_clusters; j++) {
    fclose(f[j]);
}
```

This code is used in section 37.

43.  $\langle$  Write the gnuplot script 43  $\rangle \equiv$

```
if ((f[0] = fopen("gnuplot.script", "w")) == Λ) {
    printf("Could not create gnuplot.script.\n");
     $\langle$  Cleanup cluster data files and return 40  $\rangle$ ;
}
fprintf(f[0], "set terminal png medium\n");
fprintf(f[0], "set output \"cluster_plot.png\"\n");
fprintf(f[0], "set title \"FCM clustering\"\n");
fprintf(f[0], "set xlabel \"x-coordinate\"\n");
fprintf(f[0], "set ylabel \"y-coordinate\"\n");
fprintf(f[0], "set xrange [%lf:%lf]\n", low_high[0][0], low_high[0][1]);
fprintf(f[0], "set yrange [%lf:%lf]\n", low_high[1][0], low_high[1][1]);
fprintf(f[0], "plot 'cluster.0' using 1:2 with points pt 7 ps 1 lc 1 notitle");
for (j = 1; j < num_clusters; j++) {
    sprintf(fname, "cluster.%d", j);
    fprintf(f[0], ", \"\\n'%s' using 1:2 with points pt 7 ps 1 lc %d notitle", fname, j + 1);
}
fprintf(f[0], "\n");
fclose(f[0]);
```

This code is used in section 37.

44.  $\langle$  Print usage information 44  $\rangle \equiv$

```
printf("-----\n");
if (argc  $\neq$  2) {
    printf("USAGE: fcm <input_file>\n");
    exit(1);
}
```

This code is used in section 9.

45.  $\langle$  Print post processing information 45  $\rangle \equiv$

```
 $\langle$  Print execution parameters 36  $\rangle$ ;
print_membership_matrix("membership.matrix");
gnuplot_membership_matrix();
printf("-----\n");
printf("The program run was successful... \n");
printf("Storing membership matrix in file 'membership.matrix'\n\n");
printf("If the points are on a plane (2 dimensions)\n");
printf("the gnuplot script was generated in file 'gnuplot.script', and\n");
printf("the gnuplot data in files cluster.[0]... \n\n");
printf("Process 'gnuplot.script' to generate graph: 'cluster_plot.png'\n\n");
printf("NOTE: While generating the gnuplot data, for each of the data points\n");
printf("the corresponding cluster is the one which has the highest\n");
printf("degree-of-membership as found in 'membership.matrix'.\n");
printf("-----\n");
```

This code is used in section 9.

46. Procedure *print\_data\_points* prints the data points.

$\langle$  Define global functions 18  $\rangle + \equiv$

```
void print_data_points(char *fname)
{
    int i, j;
    FILE *f;
     $\langle$  Open output file 35  $\rangle$ ;
    fprintf(f, "Data_points:\n");
     $\langle$  Print data points 47  $\rangle$ ;
    if (fname  $\equiv$   $\Lambda$ ) fclose(f);
}
```

47.  $\langle$  Print data points 47  $\rangle \equiv$

```
for (i = 0; i < num_data_points; i++) {
    printf("Data[%d]:", i);
    for (j = 0; j < num_dimensions; j++) {
        printf("%.5lf", data_point[i][j]);
    }
    printf("\n");
}
```

This code is used in section 46.

**48.** Procedure *print\_membership\_matrix* prints the current membership matrix. It take as input the name of the output file. If this is `NULL` the output is directed to `stdout`.

```

⟨ Define global functions 18 ⟩ +=
void print_membership_matrix(char *fname)
{
    int i, j;
    FILE *f;
    ⟨ Open output file 35 ⟩;
    fprintf(f, "Membership_matrix:\n");
    ⟨ Print the membership matrix 49 ⟩;
    if (fname == Λ) fclose(f);
}

```

```

49.  ⟨ Print the membership matrix 49 ⟩ ≡
for (i = 0; i < num_data_points; i++) {
    fprintf(f, "Data[%d]:\n", i);
    for (j = 0; j < num_clusters; j++) {
        fprintf(f, "%lf", degree_of_memb[i][j]);
    }
    fprintf(f, "\n");
}

```

This code is used in section 48.

**50.** Includes system libraries that defines constants and function prototypes.

```

⟨ Include system libraries 19 ⟩ +=
#include <stdio.h>
#include <stdlib.h>
#include <string.h>

```

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