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1.2 Improving Deep Neural Nets

1.2.1 Bias and Variance

- High bias means that you aren't fitting the training set well. Use a bigger network or train for longer.
- High variance means that there is a big difference between performance on the training and dev set.

1.2.2 Regularization

There are several ways to regularize your network:

1. L_2 regularization penalizes higher weights:

$$J(w,b) = \frac{1}{m} \sum_{i=1}^{m} L(\hat{y}^{(i)}, y^{(i)}) + \frac{\lambda}{2m} ||w||_2^2$$
(3)

- 2. Dropout: randomly set some of the weight values to zero. To avoid scaling output values at test time, use the *inverted dropout* technique, where during training, you divide the output by the keep_prob. The intuition is that you can't rely on any one feature, so you have to spread out the weights. Slows down training by a factor of two.
- 3. Data augmentation.
- 4. Early stopping is bad because it mixes optimization and not overfitting.

1.2.3 Activation functions

- 1. Sigmoid: $\sigma(z) = \frac{1}{1+e^{-x}}$ is almost never used, except for the output layer in binary classification.
- 2. Tanh: $tanh(z) = \frac{e^z e^{-z}}{e^z + e^{-z}}$ works better than sigmoid because the activations are closer to zero and you often normalize your input data to have zero mean.
- 3. ReLU: $a(z) = \max(0, z)$ solves the vanishing gradient problem for positive values and therefore helps the network learn faster. Also, it's derivative is faster to compute. It suffers from the *dying ReLU* problem, however, where a neuron will output zero if it's inputs are negative.
- 4. Leaky ReLU where $a(z) = \max(0.01z, z)$ gives dying ReLUs a chance to wake up.
- 5. ELU: $a(z) = \max(e^z 1, z)$ is the best. It beats Leaky ReLU because it is smooth around z = 0, which speeds up gradient descent because it does not bounch as much left and right of z = 0. It is slower to compute but compensates for this by its faster convergence rate.

1.2.4 Initialization

The more hidden units in a layer, the smaller the initialized weights should be. You can initialize the weights with a normal distribution with mean 0 and standard deviation of:

 \bullet For the xavier initialization, use $\sqrt{\frac{2}{n_{\tt inputs} + n_{\tt outputs}}}$

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1.2.5 Optimization algorithms

- Mini-batching
 - Say m = 5,000,000, then make mini-batches of 1000 for t = 5,000 minibatches. Then for t = 1 to 5,000, gradient descent like usual.
 - Mini-batch size 1 is stochastic gradient descent, where you lose speedup from vectorization.
 - Best mini-batch size typically between 1 and m, i.e., 64, 128, 256, 512.
- Momentum calculates an exponentially weighted average of examples, i.e., smooths out the steps of gradient descent. For each iteration,
 - 1. Compute dW for the mini-batch.
 - 2. $v_{dW} = \beta v_{dW} + (1 \beta)dW$ (think of v_{dW} as velocity and dW as acceleration)
 - 3. $W = W \alpha v_{dW}$
- RMSprop aims to dampen oscillations. For each iteration,
 - 1. Compute dW for the mini-batch.
 - 2. $s_{dW} = \beta \ s_{dW} + (1 \beta)dW^2 \ (s_{dW} \text{ is large when } dW \text{ oscillates a lot})$
 - 3. $W = W \alpha \frac{dW}{\sqrt{s_{dW}}}$ (slower updates when s_{dW} is large)
- Adam (adaptive moment estimation) optimization combines momentum and RMSprop, where typically $\beta_1 = 0.9$ and $\beta_2 = 0.999$. Initialize $v_{dw} = 0$, $s_{dw} = 0$. For each iteration t,
 - 1. Compute dW for the mini-batch.
 - 2. $v_{dW} = \beta_1 \ v_{dW} + (1 \beta_1)dW$
 - 3. $s_{dW} = \beta_2 \ s_{dW} + (1 \beta_2)dW^2$
 - 4. $v_{dW}^{\text{corrected}} = \frac{v_{dW}}{1-\beta_1^t}$
 - 5. $s_{dW}^{\text{corrected}} = \frac{s_{dW}}{1-\beta_2^t}$
 - 6. $W = W \alpha \frac{v_{dW}^{\text{cor}}}{\sqrt{s_{dW}^{\text{cor}}}}$
- Batch normalization normalizes the hidden layer outputs $z^{[l]}$. Given some intermediate values $z^{(1)}...z^{(m)}$,
 - 1. Compute mean $\mu = \frac{1}{m} \sum z$ and variance $\sigma^2 = \frac{1}{m} \sum (z \mu)^2$
 - 2. Compute the normalized output $z_{\text{norm}}^{(i)} = \frac{z^{(i)} \mu}{\sqrt{\sigma^2}}$
 - 3. Use $\tilde{z}^{(i)} = \gamma z_{\mathtt{norm}}^{(i)} + \beta$ instead of $z^{(i)}$, where γ and β are learnable parameters.

This sort of gets rid of the bias terms and allows the layers to learn independently.

- Learning rate decay: at each epoch, $\alpha_t = 0.95 \ \alpha_{t-1}$.
- Use the *softmax* function for multi-class classification:

$$softmax(y_i) = \frac{e^{y_i}}{\sum e^{y_i}} \tag{4}$$

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1.2.6 Q & A

1. Why does L_2 regularization work? Think of it as making a simpler network. A higher regularization parameter λ makes $w \to 0$. And so if you are using a tanh activation function, for example, then the activation is more linear at $w \to 0$, so it is harder to form complex decision boundaries that overfit.

- 2. Why is L_2 regularization better than L_1 ? L_1 creates sparse matrices, because it penalizes smaller values more than L_2 does. L_2 is more popular.
- 3. Why do you need non-linear activation functions? Because $a^{[2]} = w^{[2]}w^{[1]}x$ and you can express $w^{[2]}w^{[1]}$ as some w so there's no point in multiple hidden layers. I.e., the decomposition of two linear activation functions is a single linear activation function.