## Welcome Tutorial :-) Tutorial 8

GAO Ming

SE & DaSE @ ECNU

Foundations of Data Science, 2016

## Tutorial 8

- **1** Let L be the Laplacian of graph G of n vertices, please prove that the regularization term  $\frac{1}{2}\sum_{i,j=1}^{n}A_{i,j}(f_i-f_j)^2=F^TLF$ , where  $F\in\mathbb{R}^{n\times 1}$ .
- ② Let  $\mathscr{L}$  be the normalized Laplacian of a weighted graph G of n vertices, please prove that the regularization  $\frac{1}{2}\sum_{i,j=1}^n w_{i,j} \Big(\frac{f_i}{\sqrt{d_{ii}}} \frac{f_j}{\sqrt{d_{ij}}}\Big)^2 = F^T \mathscr{L} F, \text{ where } F \in \mathbb{R}^{n \times 1}.$
- Please extend the modularity to detect communities structures from directed graph and signed graph (encourage to read some papers).