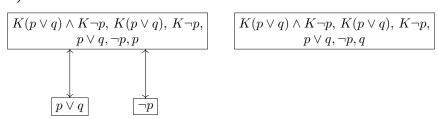
Exercise 3.1

a)



This yields the model M=(W,R,V) with $W=\{w_1\},\ R(K)=\{(w_1,w_1)\},\ V(p)=\ {\rm and}\ V(q)=\{w_1\}.$

Exercise 3.2

| ϕ | $M, w_2 \models$ | $M, w_2 \models$ | $M, w_2 \models$ | $M, w_2 \models$ | $M, w_1 \models$ | $M, w_1 \models$ |
|----------------|------------------|------------------|------------------|------------------|------------------|------------------|
| | $K_1\phi$ | $K_2\phi$ | $C\phi$ | $D\phi$ | $C\phi$ | $D\phi$ |
| \overline{p} | | \boxtimes | | \boxtimes | | |
| q | \boxtimes | | | \boxtimes | | \boxtimes |
| $p \wedge q$ | | | | \boxtimes | | |
| $p \vee q$ | \boxtimes | \boxtimes | \boxtimes | \boxtimes | \boxtimes | \boxtimes |