Movilens_Project - HarvardX: PH125.9x Data Science

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OVERVIEW

Recommendation systems use ratings that users have given items to make specific recommendations. Companies that sell many products to many customers permit these customers to rate their products. Items for which a high rating is predicted for a given user are then recommended to that user.

In this analysis we focus on Netflix, Which uses a recommendation system to predict how many stars a user will rate a specific movie, being 0.5 stars the minimum rate and 5 stars the maximum.

The original data set was constructed by the convination *movies* and *users*, Where each observation represents a rating given by one user to one movie. This data is divided in a *validation* set with 10% of data (it will be consider as unknown data and will only be used for the final evaluation) and the *edx* set with the 90% (considered as all the known data).

edx

userId	movieId	rating	timestamp	title	genres
1	122	5	838985046	Boomerang (1992)	Comedy Romance

dimensions

[1] 9000055

6

The main goal is to predict the ratings given for the convination of user and movie within the validation set, using the RMSE as a performance messure, with a desireable deviation below of 0.875 stars.

With the mentioned loss function defined as:

$$\text{RMSE} = \sqrt{\frac{1}{N} \sum_{u,i} \left(\hat{y}_{u,i} - y_{u,i} \right)^2}$$

Where $y_{u,i}$ as the rating for movie i by user u, the prediction as $\hat{y}_{u,i}$ with N being the number of user/movie combinations and the sum occurring over all these combinations.

The Method used for the analysis follows the steps:

- 1 Preparing the data.
- 2 Data exploration and visualization.
- 3 Presenting the models, calculating the variables and evaluating the results.
- 4 Cross validation and parameter optimization.
- 5 Final evaluation of the model's predictions on the validation set.

PREPARING DATA

Creating the $train\ set$ and $test\ set$ from the edx data, where the proportions is selected to fit with our $validation\ set$ size.

[1] "dimentions"

 $train_set$

[1] 8000047 6

 $test_set$

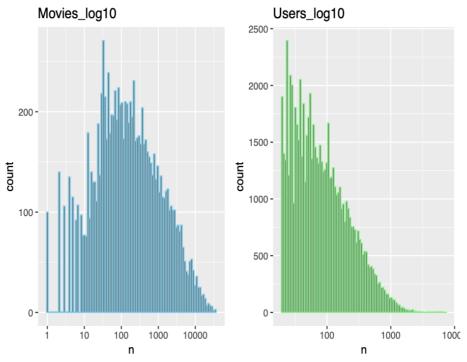
[1] 1000008

DATA EXPLORATION AND VISUALIZATION

We can see the number of unique users that provided ratings and how many unique movies were rated:

n_movies	n_users
10677	69878

Some movies get rated more than others and some users are more active than others as well.



Similarly, some $\it rates$ are more frecuently given than others.

Table 3: Table continues below

rating	4.0	3.0	5.0	3.5	2.0	4.5
num_rates rates share	2588430 $28.8%$	2121240 $23.6%$	1390114 $15.4%$	791624 $8.80%$	$711422 \\ 7.90\%$	526736 $5.85%$

rating	1.0	2.5	1.5	0.5
num_rates	345679	333010	106426	85374
$rates_share$	3.84%	3.70%	1.18%	0.949%

Ratings Summary

Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
0.5	3	4	3.512	4	5

PRESENTING THE MODELS

MEAN MODEL

A model that assumes the global mean mu as the only rating for all movies and users with all the differences explained by random variation:

$$Y_{u,i} = \mu + \varepsilon_{u,i}$$

[1] "mu= 3.5126"

Method	RMSE
Simple-Mean Model	1.0613

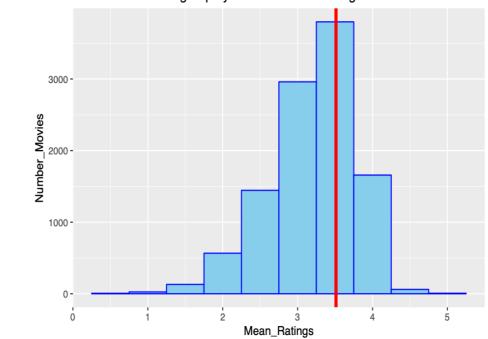
MOVIE EFFECT MODEL

In addition, different movies are rated differently and each movie has its own mean. We can have an idea of how they are distributed grouping them by a rounded mean with a range +/- 0.25 from its center:

- ## [1] "[0.5-0.75)" "[0.75-1.25)" "[1.25-1.75)" "[1.75-2.25)"
 ## [5] "[2.25-2.75)" "[2.75-3.25)" "[3.25,-3.75)" "[3.75,-4.25)"
- ## [9] "[4.25-4.75)" "[4.75-5)"

$mean_rate$	0.5	1	1.5	2	2.5	3	3.5	4	4.5	5
num_rates	7	26	131	567	1445	2960	3798	1658	61	8

Number of Movies group by rounded Mean Rating



We can extend the simple mean model by adding the term b_i to represent average ranking for each movie i:

$$Y_{u,i} = \mu + b_i + \varepsilon_{u,i}$$

Where:

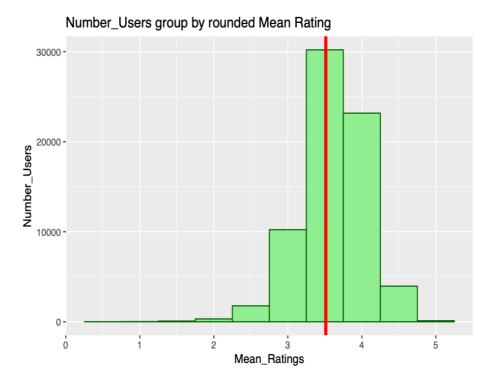
$$b_i = \frac{1}{n_i} \sum_{i=1}^{n_i} (y_{u,i} - \hat{\mu})$$

Method	RMSE
Simple-Mean Model	1.0613
Movie-Effect Model	0.94415

MOVIE-USER EFFECT MODEL

Following the same aproach as for movies, there is substantial variability across users as well.

mean_rate	0.5	1	1.5	2	2.5	3	3.5	4	4.5	5
num_rates	6	20	83	320	1770	10223	30203	23174	3963	116



Its possible to add the user effect term b_u to previous model.

$$Y_{u,i} = \mu + b_i + b_u + \varepsilon_{u,i}$$

Where:

$$b_u = \frac{1}{m_u} \sum_{u,i}^{m_u} (y_{u,i} - \hat{\mu} - b_i)$$

Method	RMSE
Simple-Mean Model	1.0613
Movie-Effect Model	0.94415
Movie-User-Effects Model	0.86613

REGULARIZED MOVIE-USER EFFECT MODEL

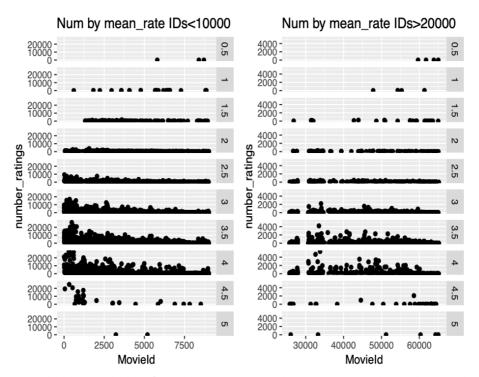
In the scenario that few ratings per user or movies are given, it is better to be conservatives and consider the *user* or *movie* effect just partially, because it may be over or under rating be them.

Here we have some examples, where the minimum and maximum values of the mean by movies are often given by a few number of rates

movieId	title	mean_rate	num_rates
3226	Hellhounds on My Trail (1999)	5	1
51209	Fighting Elegy (Kenka ereji	5	1

movieId	title	$mean_rate$	num_rates
60309	Along Came Jones (1945)	5	1

movieId	title	mean_rate	num_rates
5805	Besotted (2001)	0.5	1
8394	Hi-Line, The (1999)	0.5	1
8707	Grief (1993)	0.5	1



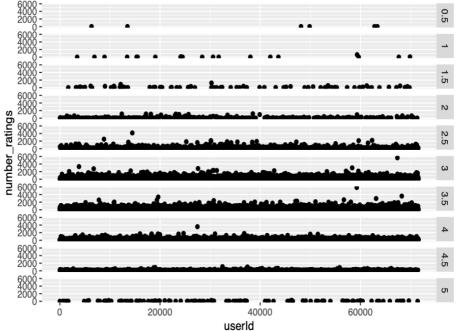
Note: the data was splited just for visualization purposes, and there are not movies' ${\it IDs}$ in between codes 10000 and 20000

Similarly, on the users side for those who gave few rates For instance:

userId	mean_rate	num_rates
26308	5	14
52674	5	14
7984	5	15

userId	$mean_rate$	num_rates
49862	0.5	16
13496	0.5	17
63381	0.5	17

Number of rates by mean_rate



The goal of penalized regression is to control the total variability of the movie effects: $\sum_{i=1}^{n} b_i^2$. Specifically, instead of minimizing the least square equation, we minimize an equation that adds a penalty:

$$\frac{1}{N} \sum_{u,i} (y_{u,i} - \mu - b_i)^2 + \lambda \sum_i b_i^2$$

The first term is just least squares and the second is a penalty that gets larger when many b_i are large.

$$\hat{b}_i(\lambda) = \frac{1}{\lambda + n_i} \sum_{i=1}^{n_i} (Y_{u,i} - \hat{\mu})$$

where n_i is the number of ratings made for movie i. This approach will have our desired effect: when our sample size n_i is very large, a case which will give us a stable estimate, then the penalty λ is effectively ignored since $n_i + \lambda \approx n_i$. However, when the n_i is small, then the estimate $\hat{b}_i(\lambda)$ is shrunken towards 0. The larger λ , the more we shrink.

We can use regularization for the estimate user effects as well. We are minimizing:

$$\hat{b}_u(\lambda) = \frac{1}{\lambda + m_u} \sum_{u=1}^{m_u} \left(Y_{u,i} - \hat{\mu} - \hat{b}_i \right)$$

where m_u is the number of ratings made for user u. This approach will have our desired effect: when our sample size m_u is very large, a case which will give us a stable estimate, then the penalty λ is effectively ignored since $m_u + \lambda \approx m_u$. However, when the m_u is small, then the estimate $\hat{b}_u(\lambda)$ is shrunken towards 0. The larger λ , the more we shrink.

$$\frac{1}{N}\sum_{u,i}\left(y_{u,i}-\mu-b_i-b_u\right)^2+\lambda\left(\sum_i b_i^2+\sum_u b_u^2\right)$$

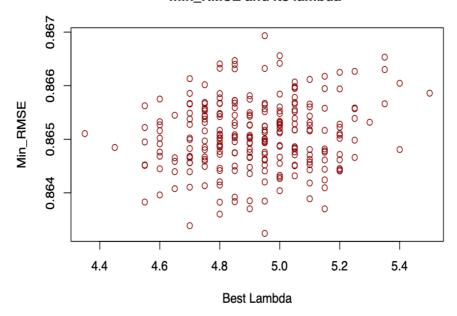
In the next section, we will be implementing full cross validation just on the $train\ set$, without using the $validation\ set$ until the final assessment.

CROSS VALIDATION AND PARAMETER OPTIMIZATION

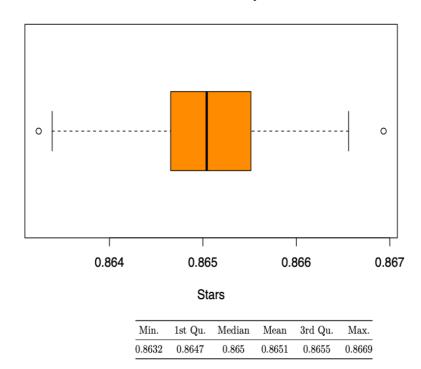
We are taking many new samples of the edx set to pick the values of λ which minimize the RMSE on each sample, the size is the same as in original setup. Within this case 250 new samples were taken.

Choosing the penalty terms λ

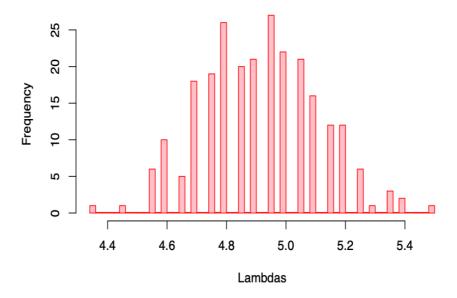
min_RMSE and its lambda



minimum_RMSE Dispersion



Histogram of lambda_min



[1] "Optimized lambdas"

Table 16: Table continues below

4.35	4.45	4.55	4.6	4.65	4.7	4.75	4.8	4.85	4.9	4.95	5
1	1	6	10	5	18	19	26	20	21	27	22
	5.05	5.1	5.15	5.2	5.25	5.	3	5.35	5.4	5.5	
	21	16	12	12	6	1		3	2	1	
	M	in.	1st Qu.	Me	dian	Mean		3rd Qu.	Ma	x.	
	4.	35	4.8	4	1.9	4.918		5.05	5.5	5	

Testing the model results:

Now we can test the Regularized-movie-user-effect-model agaist a the original test set using the optimized value found for lambda $\lambda = 4.9$.

Method	RMSE
Simple-Mean Model	1.0613
Movie-Effect Model	0.94415
Movie-User-Effects Model	0.86613
Regularized-Movie-User Effect Model	0.86552

3. RESULTS

Finally, we are able to evaluate our final Regularized-Movie-User Effect Model using the edx set with our validation set, where the last one remains yet as unknown data, and reveals the results under a possible real scenario.

Method	RMSE
Final Model vs validation set	0.86482

CONCLUSION

Following the steps we learned in the course, we have improved the base line of a Mean-Model for predicting ratings, going through the user and movies effects and finally arriving to the Regularized-Movie-User Effect Model, which was optimized for $\lambda=4.9$ and reflected a RMSE ≈ 0.865 on the validation set, in other words, a deviation of 0.86 stars from the predictions.

 $Please\ follow\ this\ link\ to\ have\ access\ to\ the\ project\ files:\ https://github.com/AmadoLabX/Data-Science-HX$