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Grade	16.00 out of 16.00 (100%)

Question 1

Correct

Mark 8.00 out of 8.00

Consider a clipping window defined with vertices A(25, 30), B(75, 30), C(75, 80) and D(25, 80). Let P_1P_2 be a line from (5, 20) to (55, 90) to be clipped against the clipping window. Write the answers of following questions. [All calculation should be done with 3 decimal places (round off)]

a) [4Marks] Fill the following table using Liang-Barsky line clipping algorithm. [Notation are used as per lecture]

i	Edge	p_i	q_i	t_i
1	DA	-50	-20	0.4

✓

2	CB	50	70	1.4
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✓

3	AB	-70	-10	0.143
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✓

4	DC	70	60	0.857
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✓

b) [2 marks] Write the t_{min} and t_{max} values.

$t_{min} = 0.4$ and $t_{max} = 0.857$

✓

c) [2 marks] Write the coordinate values at t_{min} and t_{max}

At t_{min} : x = 25 and y = 48

✓

At t_{max} : x = 47.857 and y = 80

✓

Your answer is correct.

Answer with detailed calculations:

For Edge DA

$p_1 = -(55 - 5) = -50; \quad q_1 = (5 - 25) = -20; \quad t_1 = \text{round}(q_1/p_1, 3) = 0.4;$

For Edge CB

$p_2 = (55 - 5) = 50; \quad q_2 = (75 - 5) = 70; \quad t_2 = \text{round}(q_2/p_2, 3) = 1.4;$

For Edge AB

$p_3 = -(90 - 20) = -70; \quad q_3 = (20 - 30) = -10; \quad t_3 = \text{round}(q_3/p_3, 3) = 0.143;$

For Edge DC

$p_4 = (90 - 20) = 70; \quad q_4 = (80 - 20) = 60; \quad t_4 = \text{round}(q_4/p_4, 3) = 0.857;$

$t_{min} = \max(0, t_1, t_3) = \max(0, 0.4, 0.143) = 0.4;$

$t_{max} = \min(1, t_2, t_4) = \min(1, 1.4, 0.857) = 0.857;$

At t_{min} :

$x(0.4) = \text{round}(5 + (55 - 5) \cdot 0.4, 3) = 25;$

$y(0.4) = \text{round}(20 + (90 - 20) \cdot 0.4, 3) = 48;$

At t_{max} :

$x(0.857) = \text{round}(5 + (55 - 5) \cdot 0.857, 3) = 47.85;$

$y(0.857) = \text{round}(20 + (90 - 20) \cdot 0.857, 3) = 79.99;$

Consider a clipping window defined with vertices A(50, 90), B(70, 110), C(60, 120) and D(40, 80). Let P_1P_2 be a line from (25, 105) to (85, 105) to be clipped against the clipping window. Write the answers of following questions.

[All calculation should be done with 3 decimal places (round off)]

a) [4Marks] Fill the following information for Cyrus-Beck line clipping algorithm. Consider outward normal vector for each edge ie. direction of normal is towards outside. [Notation are used as per lecture]

$Edge(E_i)$	$Normal(N_i)$	P_{E_i}	t	PE/PL
DA	(+i , -j)	A	0.667	PL



CB	(+i , +j)	C	0.833	PL
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AB	(+i , -j)	A	0.667	PL
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DC	(-i , +j)	C	0.458	PE
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Detailed Answer:
Clipping Window : $A(50, 90)B(70, 110)C(60, 120)D(40, 80)$
Line to be clipped : $P_1(25, 105)P_2(85, 105)$
 $D = (P_1 - P_2) = (60, 0)$
#For DA edge
 $N_{DA} = (1, -1)$
Direction Symbol $N_{DA} = (+i, -j)$
 $PE_{DA} = (50, 90)$
 $P_1 - PE_{DA} = (-25, 15)$
 $N_{DA} \cdot (P_1 - PE_{DA}) = -40$
 $(N_{DA} \cdot D) = 60$
 $t_{DA} = -\frac{N_{DA} \cdot (P_1 - PE_{DA})}{(N_{DA} \cdot D)} = round(-\frac{-40}{60}, 3) = 0.667$
 $PE/PL = PL$

#For CB edge
 $N_{CB} = (1, 1)$
Direction Symbol $N_{CB} = (+i, +j)$
 $PE_{CB} = (60, 120)$
 $P_1 - PE_{CB} = (-35, -15)$
 $N_{CB} \cdot (P_1 - PE_{CB}) = -50$
 $(N_{CB} \cdot D) = 60$
 $t_{CB} = -\frac{N_{CB} \cdot (P_1 - PE_{CB})}{(N_{CB} \cdot D)} = round(-\frac{-50}{60}, 3) = 0.833$
 $PE/PL = PL$

#For AB edge
 $N_{AB} = (1, -1)$
Direction Symbol $N_{AB} = (+i, -j)$
 $PE_{AB} = (50, 90)$
 $P_1 - PE_{AB} = (-25, 15)$
 $N_{AB} \cdot (P_1 - PE_{AB}) = -40$
 $(N_{AB} \cdot D) = 60$
 $t_{AB} = -\frac{N_{AB} \cdot (P_1 - PE_{AB})}{(N_{AB} \cdot D)} = round(-\frac{-40}{60}, 3) = 0.667$
 $PE/PL = PL$

#For DC edge
 $N_{DC} = (-2, 1)$
Direction Symbol $N_{DC} = (-i, +j)$
 $PE_{DC} = (60, 120)$

$$P_1 - PE_{DC} = (-35, -15)$$

$$N_{DC} \cdot (P_1 - PE_{DC}) = 55$$

$$(N_{DC} \cdot D) = -120$$

$$t_{DC} = -\frac{N_{DC} \cdot (P_1 - PE_{DC})}{(N_{DC} \cdot D)} = \text{round}\left(-\frac{55}{-120}, 3\right) = 0.458$$

$$PE/PL = PE$$

b) [2 marks] Write the t_{min} and t_{max} values.

$$t_{min} = \boxed{0.458} \text{ and } t_{max} = \boxed{0.667}$$



Detailed Answer:

$$t_{min} = \max(0, t_{DC}) = \max(0, 0.458) = 0.458 \text{ \#PE}$$

$$t_{max} = \min(1, t_{DA}, t_{CB}, t_{AB}) = \min(1, 0.667, 0.833, 0.667) = 0.667 \text{ \#PL}$$

c) [2 mark] Write the coordinate values at t_{min} and t_{max}

$$\text{At } t_{min}: x = \boxed{52.5} \text{ and } y = \boxed{105}$$



Detailed Answer:

Line Eqn:

$$P(t) = P_1 + (P_2 - P_1) * t$$

At t_{min}

$$x(0.458) = \text{round}(25 + (85 - 25) * 0.458, 3) = 52.48;$$

$$y(0.458) = \text{round}(105 + (105 - 105) * 0.458, 3) = 105;$$

$$\text{At } t_{max}: x = \boxed{65} \text{ and } y = \boxed{105}$$



Detailed Answer:

Line Eqn:

$$P(t) = P_1 + (P_2 - P_1) * t$$

At t_{max}

$$x(0.667) = \text{round}(25 + (85 - 25) * 0.667, 3) = 65.02;$$

$$y(0.667) = \text{round}(105 + (105 - 105) * 0.667, 3) = 105;$$