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Time taken	29 mins 27 secs
Grade	10.00 out of 10.00 (100%)

Question 1

Correct

Mark 4.00 out of 4.00

Consider the following projection.

- Projection Plane is at  $y = 20$  and perpendicular to  $y$ -axis (ie. parallel to  $xz$  plane).
- COP is at distance 70 from  $(0, 20, 0)$ . The direction from  $(0, 20, 0)$  to COP is given by direction vector  $(10, -30, 10)$ . The given direction vector is not normalized.
- P1 is the projection of point  $P(20, 55, 35)$  in the projection plane.

Write the coordinate values for COP and P1. [All calculation should be done with 3 decimal places (round off)]

a) [1 mark] COP = (  ,  ,  )

[No partial marking]



b) [3 marks] x, y and z values of P1:

P1 (x) =



P1 (y) =



P1 (z) =



Your answer is correct.

Detailed Answer:

```
# Normalized direction vector = (dx, dy, dz)
dx = round(10/sqrt(10 * 10 + -30 * -30 + 10 * 10), 3) = 0.302;
dy = round(-30/sqrt(10 * 10 + -30 * -30 + 10 * 10), 3) = -0.905;
dz = round(10/sqrt(10 * 10 + -30 * -30 + 10 * 10), 3) = 0.302;

#COP = (cop_x, cop_y, cop_z)
cop_x = round(0 + 70 * 0.302, 3) = 21.14;
cop_y = round(20 + 70 * -0.905, 3) = -43.35;
cop_z = round(0 + 70 * 0.302, 3) = 21.14;

# compute t
P1(y) = pp_y = 20;
t = round((20 - -43.35)/(55 - -43.35), 3) = 0.644;
P1(x) = round(21.14 + 0.644 * (20 - 21.14), 3) = 20.406 ;
P1(z) = round(21.14 + 0.644 * (35 - 21.14), 3) = 30.066 ;
```

Consider two view volumes as defined below.

View volume-1 (VV-1)	View volume-2 (VV-2)
$x = z; x = -z$	$x = 1; x = -1$
$y = z; y = -z$	$y = 1; y = -1$
$z = -0.4; z = -1$	$z = 0; z = -1$

A line segment  $PQ$  is defined in VV-1 with  $P = (0.6, -0.7, -0.8)$  and  $Q = (-0.5, 0.6, -0.7)$ . The first view volume (VV-1) is transformed to the second view volume (VV-2) with the help of transformation matrix  $M$ . The line segment  $PQ$  becomes  $P_1Q_1$  in VV-2.

Write the transformation matrix  $M$  and the coordinate values for  $P_1$  and  $Q_1$ .

[All calculation should be done with 3 decimal places (round off)]

a) [4 marks] Matrix  $M$ :

$M =$	1	0	0	0
	0	1	0	0
	0	0	0.714	-0.286
	0	0	-1	0

[No partial marking]



Detailed Answer:

$-z_{min} = -0.4$

$z_{min} = 0.4$

# Combined Transformation Matrix:

$M =$	1	0	0	0
	0	1	0	0
	0	0	$\frac{1}{(1+z_{min})}$	$\frac{-z_{min}}{(1+z_{min})}$
	0	0	-1	0
$=$				
	1	0	0	0
	0	1	0	0
	0	0	$round(\frac{1}{(1+0.4)}, 3)$	$round(\frac{-0.4}{(1+0.4)}, 3)$
	0	0	-1	0
$=$				
	1	0	0	0
	0	1	0	0
	0	0	0.714	-0.286
	0	0	-1	0

# Computation for P1 and Q1

[      P1      Q1      ]	=	1	0	0	0	*	0.6	-0.5	=	0.6	-0.5	=	0.75	-0.714
		0	1	0	0		-0.7	0.6		-0.7	0.6		-0.875	0.857
		0	0	0.714	-0.286		-0.8	-0.7		-0.857	-0.786		-1.071	-1.123
		0	0	-1	0		1	1		0.8	0.7		1	1

b) [1 mark]  $P1 = (0.750, -0.875, -1.071)$

[No partial marking]



c) [1 mark]  $Q1 = (-0.714, 0.857, -1.123)$

[No partial marking]



Your answer is correct.

