



National University of Sciences and Technology (NUST)
School of Electrical Engineering and Computer Science

Department of Computing

EE 433: Digital Image Processing

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Class: BSCS 9C

Lab 7: Local Histogram Equalization

Date: 1st November 2021

Time: 2.00Pm to 5.00Pm

Instructor: Dr. Imran Malik



Local Histogram Equalization

Task 1

Global Histogram Equalization

CODE

```
from PIL import Image
from matplotlib import pyplot as plt

L = 256

# returns the width and height of the image
def imageProperties(img):
    return img.size

# returns the number of pixels of each intensity level
def populateCountArray(img):
    countArray = [0] * 256

    # load the pixels
    pix = img.load()

    # M is the width and N is the height of the image
    M, N = imageProperties(img)

    # iterate through the pixels
    for x in range(M):
```



```
for y in range(N):  
    # add 1 to the countArray whenever a particular intensity pixel is found  
    countArray[pix[x, y]] += 1  
  
return countArray  
  
# probability distribution function  
def pdf(array, img):  
    pdfArray = [0] * 256  
    M, N = imageProperties(img)  
  
    # pdf = frequency / total no. of pixels  
    for i in range(len(array)):  
        # M * N is the total no. of pixels  
        pdfArray[i] = array[i] / (M * N)  
  
    return pdfArray  
  
# cumulative frequency distribution function  
def cdf(array):  
    cdfArray = [0] * 256  
  
    # at every index, find the sum of current and all previous pdfs  
    for i in range(len(array)):  
        for j in range(i):  
            cdfArray[i] += array[j]  
    return cdfArray  
  
# map cdf to intensity values  
def transformation(array):
```



```
transformed = [0] * 256

for i in range(len(array)):
    transformed[i] = round(array[i] * (L - 1))

return transformed

# plot the histogram

def showAndSaveHistogram(array, string):
    plt.title("Intensity Histogram")
    plt.xlabel("Intensity")
    plt.ylabel("Frequency")
    plt.bar([i for i in range(256)], array)
    plt.savefig(string + " histogram")
    plt.show()

# apply histogram equalization to the input image

def outputImage(array, img):
    pix = img.load()
    M, N = imageProperties(img)

    # iterate the pixels
    for x in range(M):
        for y in range(N):
            # change the intensity of the pixel to the transformed one
            pix[x, y] = array[pix[x, y]]

    return img

# open image
```



```
image = Image.open("lab07_img.png").convert('L')
histArray = populateCountArray(image)
pdfArray = pdf(histArray, image)
cdfArray = cdf(pdfArray)
transformed = transformation(cdfArray)
# save and show the histogram for the input image
showAndSaveHistogram(histArray, "input")
# get output image
output = outputImage(transformed, image)
histOutput = populateCountArray(image)
# save and show the histogram for the output image
showAndSaveHistogram(histOutput, "output")
# save output image
output.save("Transformed Image.jpg")
```

```
1  from PIL import Image
2  from matplotlib import pyplot as plt
3
4  L = 256
5
6  # returns the width and height of the image
7  def imageProperties(img):
8      return img.size
9
10 # returns the number of pixels of each intensity level
11 def populateCountArray(img):
12     countArray = [0] * 256
13
14     # load the pixels
15     pix = img.load()
16
17     # M is the width and N is the height of the image
18     M, N = imageProperties(img)
19
20     # iterate through the pixels
21     for x in range(M):
22         for y in range(N):
23             # add 1 to the countArray whenever a particular intensity pixel is found
24             countArray[pix[x, y]] += 1
25
26     return countArray
27
```

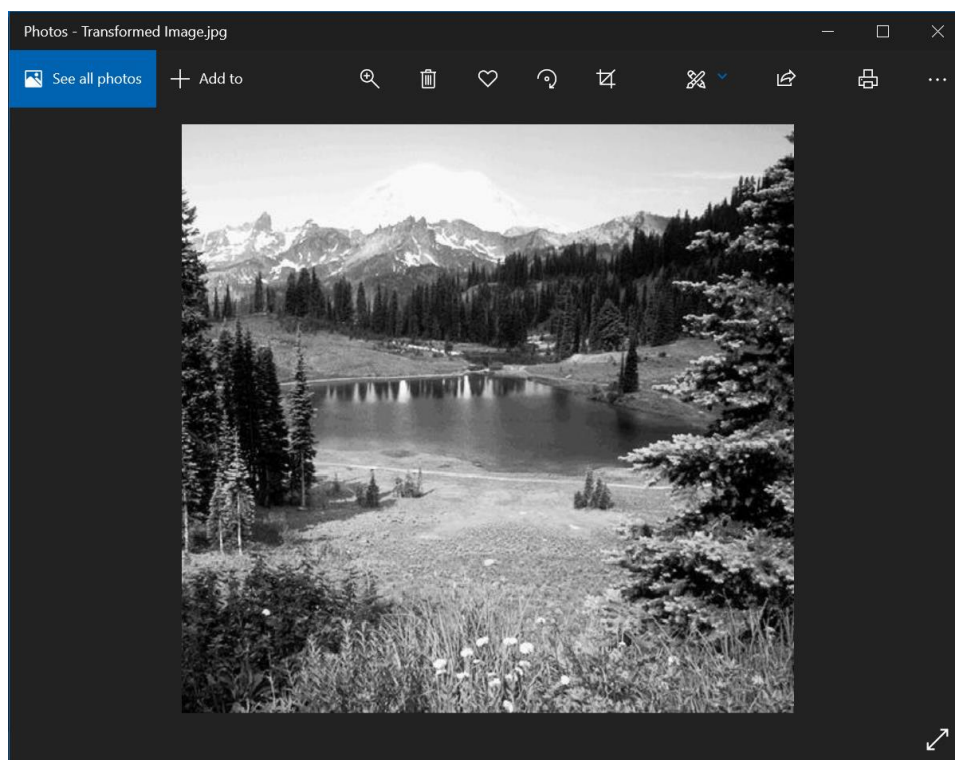


```
28 # probability distribution function
29 def pdf(array, img):
30     pdfArray = [0] * 256
31     M, N = imageProperties(img)
32
33     # pdf = frequency / total no. of pixels
34     for i in range(len(array)):
35         # M * N is the total no. of pixels
36         pdfArray[i] = array[i] / (M * N)
37
38     return pdfArray
39 # cumulative frequency distribution function
40 def cdf(array):
41     cdfArray = [0] * 256
42
43     # at every index, find the sum of current and all previous pdfs
44     for i in range(len(array)):
45         for j in range(i):
46             cdfArray[i] += array[j]
47     return cdfArray
48
```

```
49 # map cdf to intensity values
50 def transformation(array):
51     transformed = [0] * 256
52     for i in range(len(array)):
53         transformed[i] = round(array[i] * (L - 1))
54     return transformed
55
56 # plot the histogram
57 def showAndSaveHistogram(array, string):
58     plt.title("Intensity Histogram")
59     plt.xlabel("Intensity")
60     plt.ylabel("Frequency")
61     plt.bar([i for i in range(256)], array)
62     plt.savefig(string + " histogram")
63     plt.show()
64
65 # apply histogram equalization to the input image
66 def outputImage(array, img):
67     pix = img.load()
68     M, N = imageProperties(img)
69
70     # iterate the pixels
71     for x in range(M):
72         for y in range(N):
73             # change the intensity of the pixel to the transformed one
74             pix[x, y] = array[pix[x, y]]
75
76     return img
```



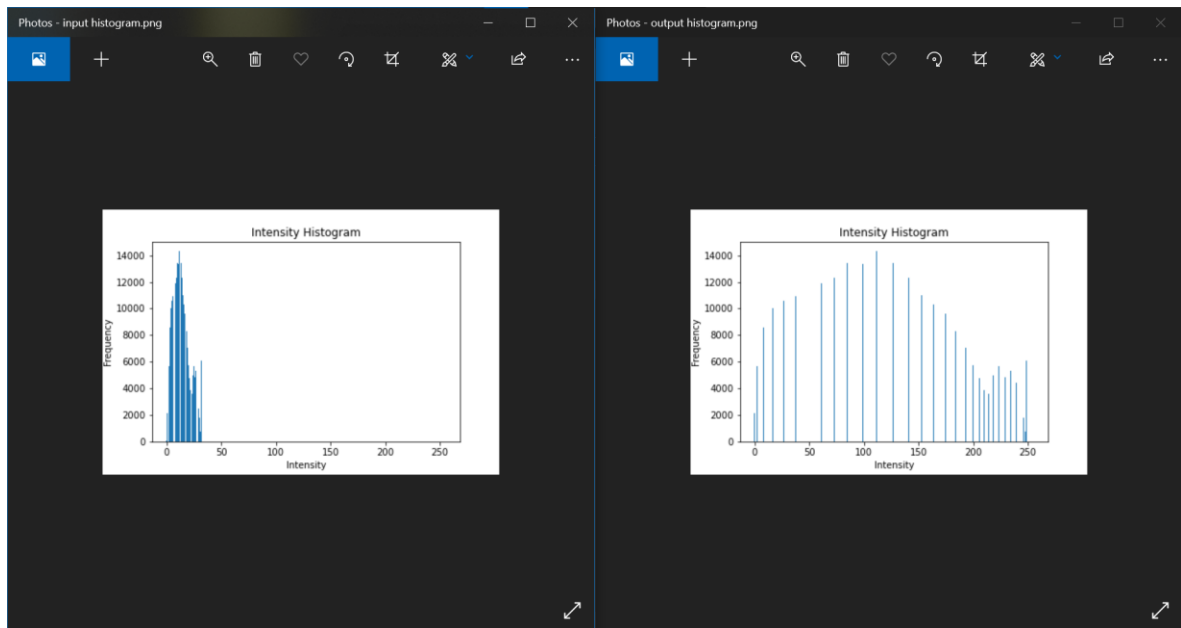
```
77
78
79 # open image
80 image = Image.open("Lab07_img.png").convert('L')
81 histArray = populateCountArray(image)
82 pdfArray = pdf(histArray, image)
83 cdfArray = cdf(pdfArray)
84 transformed = transformation(cdfArray)
85 # save and show the histogram for the input image
86 showAndSaveHistogram(histArray, "input")
87 # get output image
88 output = outputImage(transformed, image)
89 histOutput = populateCountArray(image)
90 # save and show the histogram for the output image
91 showAndSaveHistogram(histOutput, "output")
92 # save output image
93 output.save("Transformed Image.jpg")
```



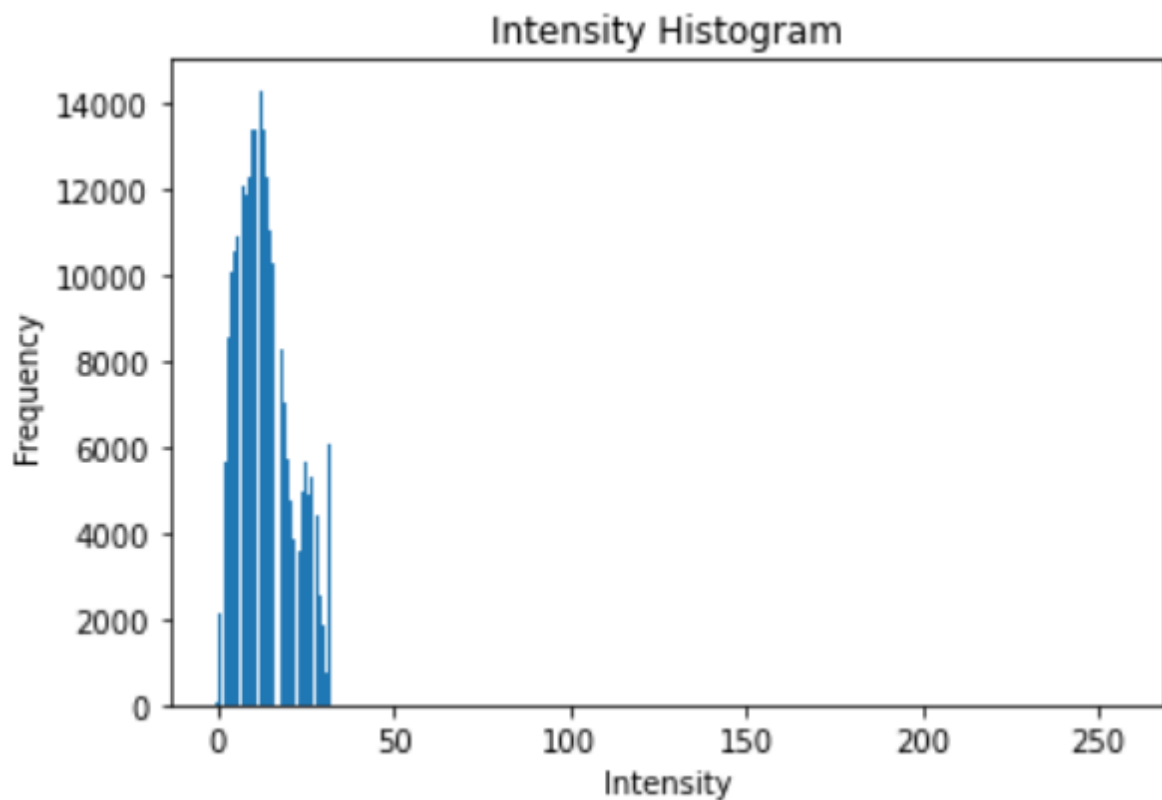


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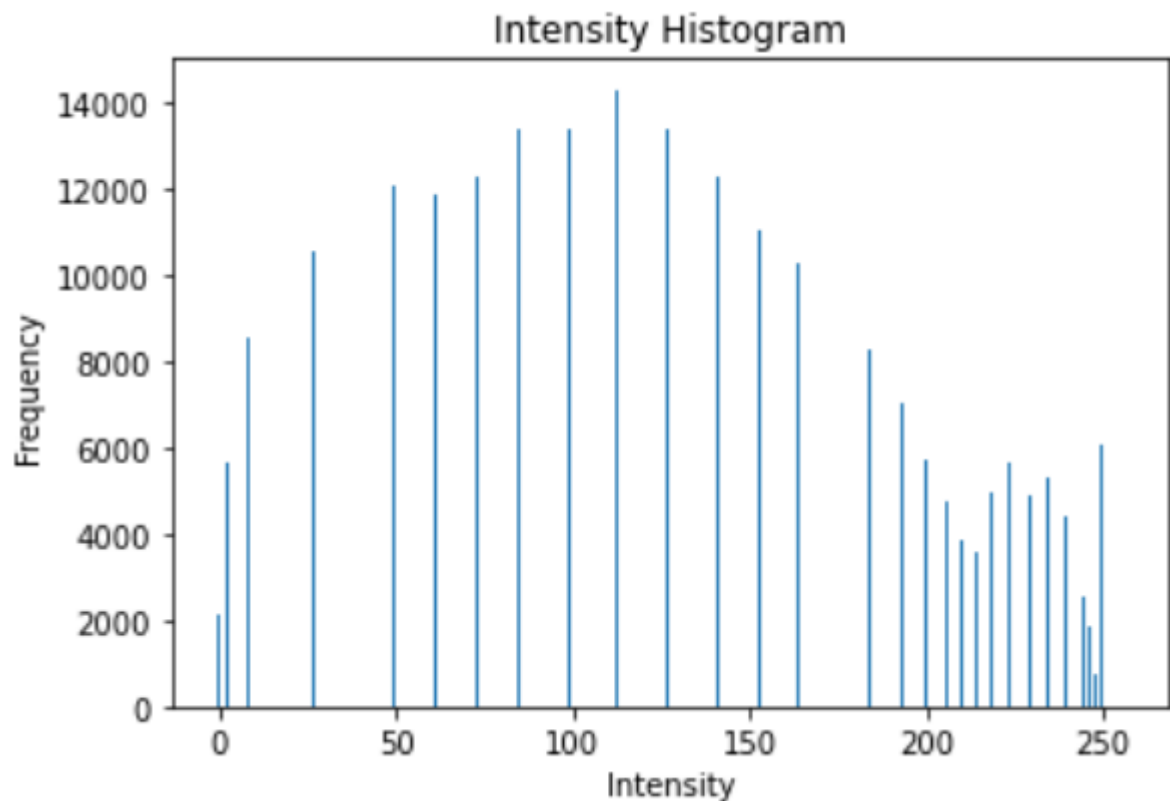
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Before:



After:



Task 2

Local Histogram Equalization

Tiling

CODE

```
from PIL import Image
from matplotlib import pyplot as plt

L = 256

# returns the width and height of the image
def imageProperties(img):
    return img.size
```



```
# returns the number of pixels of each intensity level
def populateCountArray(img,startX,startY,endX,endY):
    countArray = [0] * 256

    # load the pixels
    pix = img.load()

    # iterate through the pixels
    for x in range(startX,endX):
        for y in range(startY,endY):
            # add 1 to the countArray whenever a particular intensity pixel is found
            countArray[pix[x, y]] += 1

    return countArray

# probability distribution function
def pdf(array, width, height):
    pdfArray = [0] * 256

    # pdf = frequency / total no. of pixels
    for i in range(len(array)):
        # width * height is the total no. of pixels in the tile
        pdfArray[i] = array[i] / (width*height)

    return pdfArray

# cumulative frequency distribution function
def cdf(array):
    cdfArray = [0] * 256
```



```
# at every index, find the sum of current and all previous pdfs
for i in range(len(array)):
    for j in range(i):
        cdfArray[i] += array[j]
return cdfArray

# map cdf to intensity values
def transformation(array):
    transformed = [0]*256
    for i in range(len(array)):
        transformed[i] = round(array[i] * (L - 1))
    return transformed

# plot the histogram
def showAndSaveHistogram(array, string, tileNo):
    plt.title("Intensity Histogram")
    plt.xlabel("Intensity")
    plt.ylabel("Frequency")
    plt.bar([i for i in range(256)], array)
    plt.savefig(string + "- tile " + str(tileNo) + "histogram")
    plt.show()

# apply histogram equalization to the input image
def outputImage(array, img, startX,startY,endX,endY):
    pix = img.load()

    # iterate the pixels
    for x in range(startX,endX):
```



```
for y in range(startY,endY):

    # change the intensity of the pixel to the transformed one

    pix[x, y] = array[pix[x, y]]

return img

# open image
image = Image.open("lab07_img.png").convert('L')
M, N = image.size

currentTile = 0

for i in range(2):
    for j in range(2):
        # histogram of input tile
        tile = populateCountArray(image, j*int(M/2), i*int(N/2), (j+1)*int(M/2), (i+1)*int(N/2))
        pdfArray = pdf(tile,M/2,N/2)
        cdfArray = cdf(pdfArray)
        transformed = transformation(cdfArray)
        # for naming reasons
        currentTile += 1

        # showing and saving the input tile's histogram
        showAndSaveHistogram(tile, "input", currentTile)

        # map the transformed array to an output image of that tile
        output = outputImage(transformed, image, j*int(M/2), i*int(N/2), (j+1)*int(M/2),
        (i+1)*int(N/2))

        # histogram of output tile
        outputHist = populateCountArray(output, j*int(M/2), i*int(N/2), (j+1)*int(M/2),
        (i+1)*int(N/2))
```



```
# showing and saving the output tile's histogram
```

```
showAndSaveHistogram(outputHist, "output", currentTile)
```

```
output.save("Task2.png")
```

```
1  from PIL import Image
2  from matplotlib import pyplot as plt
3
4  L = 256
5
6  # returns the width and height of the image
7  def imageProperties(img):
8      return img.size
9
10 # returns the number of pixels of each intensity level
11 def populateCountArray(img, startX, startY, endX, endY):
12     countArray = [0] * 256
13
14     # load the pixels
15     pix = img.load()
16
17     # iterate through the pixels
18     for x in range(startX, endX):
19         for y in range(startY, endY):
20             # add 1 to the countArray whenever a particular intensity pixel is found
21             countArray[pix[x, y]] += 1
22
23     return countArray
24
```

```
25 # probability distribution function
26 def pdf(array, width, height):
27     pdfArray = [0] * 256
28
29     # pdf = frequency / total no. of pixels
30     for i in range(len(array)):
31         # width * height is the total no. of pixels in the tile
32         pdfArray[i] = array[i] / (width*height)
33
34     return pdfArray
35
36 # cumulative frequency distribution function
37 def cdf(array):
38     cdfArray = [0] * 256
39
40     # at every index, find the sum of current and all previous pdfs
41     for i in range(len(array)):
42         for j in range(i):
43             cdfArray[i] += array[j]
44     return cdfArray
```



```
45
46 # map cdf to intensity values
47 def transformation(array):
48     transformed = [0]*256
49     for i in range(len(array)):
50         transformed[i] = round(array[i] * (L - 1))
51     return transformed
52
53 # plot the histogram
54 def showAndSaveHistogram(array, string, tileNo):
55     plt.title("Intensity Histogram")
56     plt.xlabel("Intensity")
57     plt.ylabel("Frequency")
58     plt.bar([i for i in range(256)], array)
59     plt.savefig(string + "- tile " + str(tileNo) + "histogram")
60     plt.show()
61
62 # apply histogram equalization to the input image
63 def outputImage(array, img, startX,startY,endX,endY):
64     pix = img.load()
65
66     # iterate the pixels
67     for x in range(startX,endX):
68         for y in range(startY,endY):
69             # change the intensity of the pixel to the transformed one
70             pix[x, y] = array[pix[x, y]]
71
72     return img
```

```
73
74
75 # open image
76 image = Image.open("Lab07_img.png").convert('L')
77 M, N = image.size
78
79 currentTile = 0
80
81 for i in range(2):
82     for j in range(2):
83         # histogram of input tile
84         tile = populateCountArray(image, j*int(M/2), i*int(N/2), (j+1)*int(M/2), (i+1)*int(N/2))
85         pdfArray = pdf(tile,M/2,N/2)
86         cdfArray = cdf(pdfArray)
87         transformed = transformation(cdfArray)
88         # for naming reasons
89         currentTile += 1
90         # showing and saving the input tile's histogram
91         showAndSaveHistogram(tile, "input", currentTile)
92         # map the transformed array to an output image of that tile
93         output = outputImage(transformed, image, j*int(M/2), i*int(N/2), (j+1)*int(M/2), (i+1)*int(N/2))
94         # histogram of output tile
95         outputHist = populateCountArray(output, j*int(M/2), i*int(N/2), (j+1)*int(M/2), (i+1)*int(N/2))
96         # showing and saving the output tile's histogram
97         showAndSaveHistogram(outputHist, "output", currentTile)
98
99     output.save("Task2.png")
```

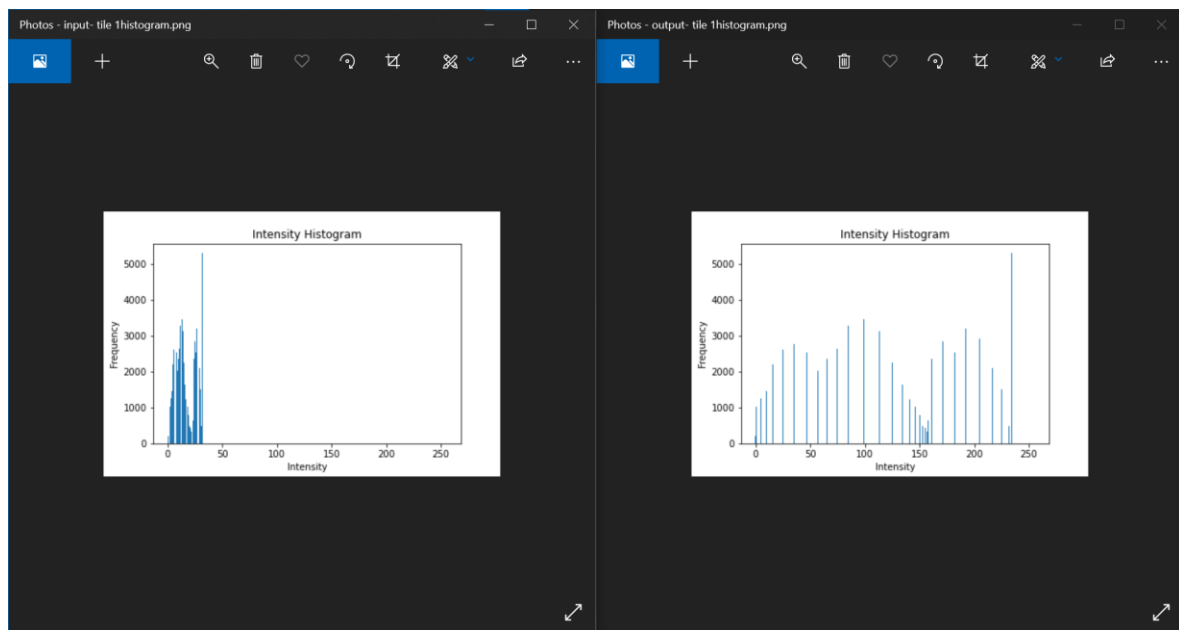
HISTOGRAMS

Tile 1

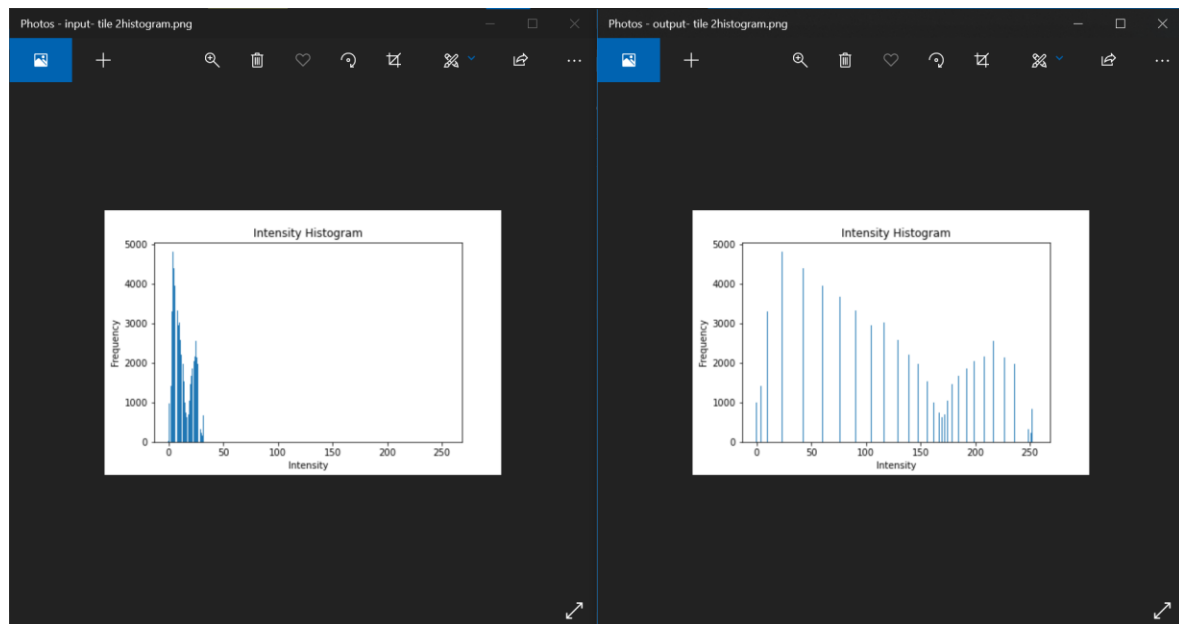


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Tile 2

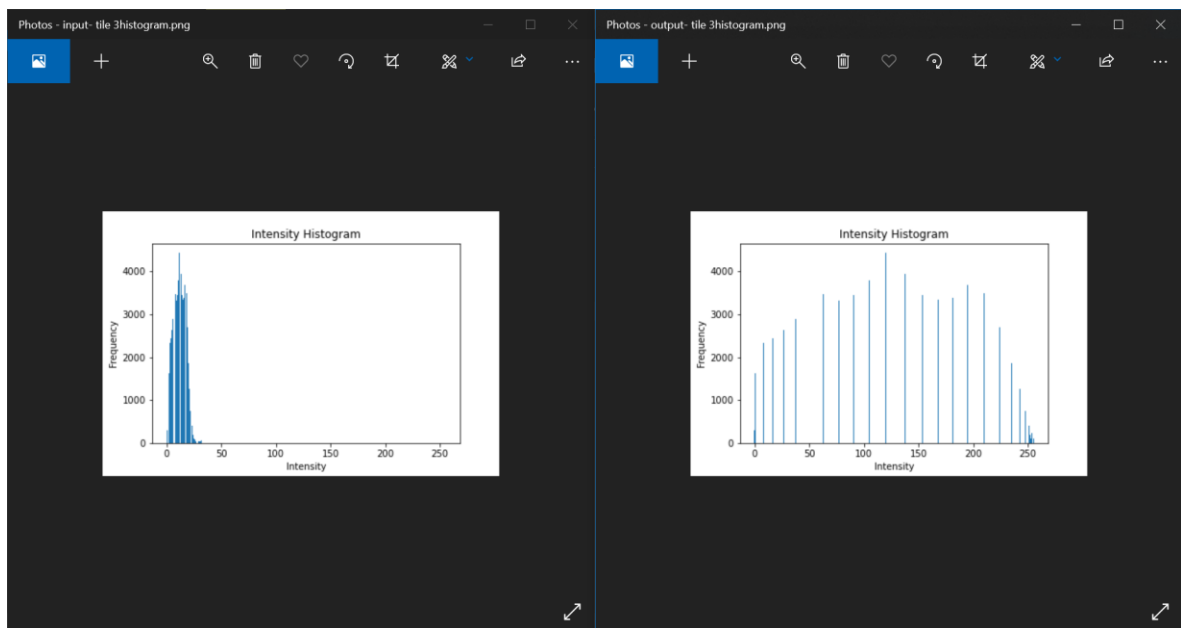


Tile 3

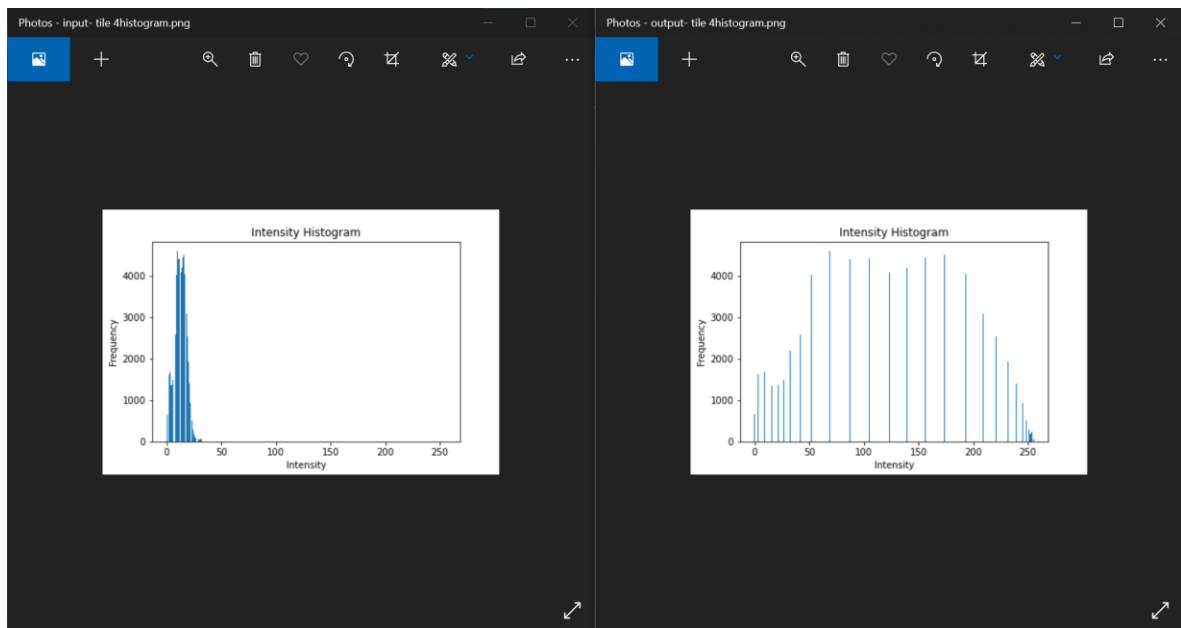


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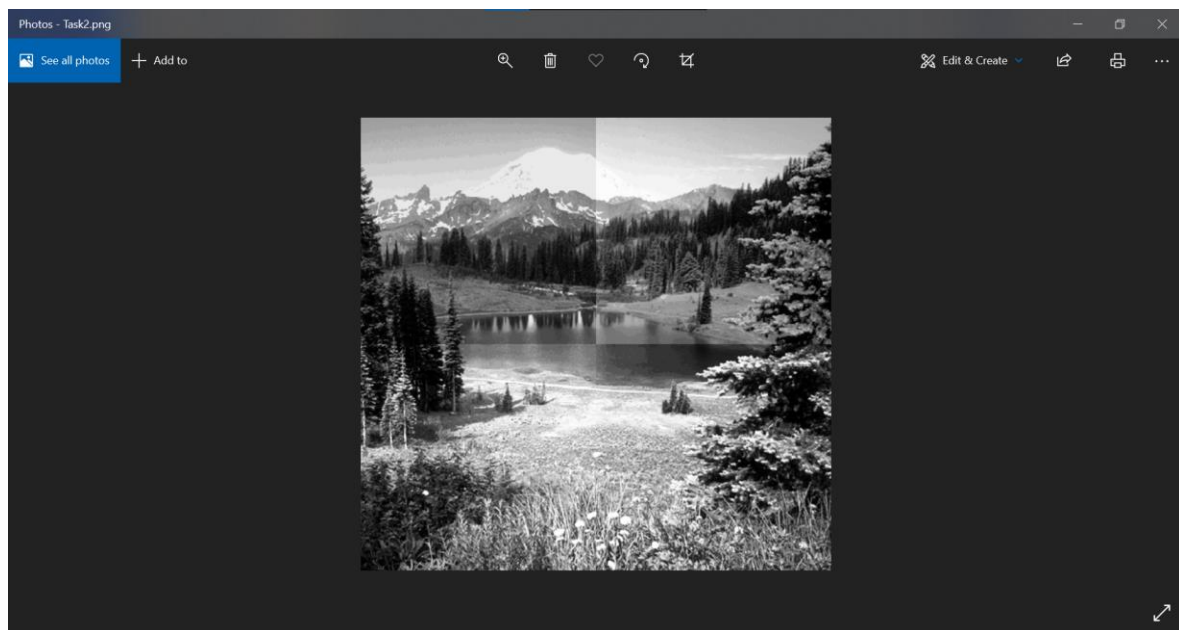
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Tile 4



OUTPUT



Sliding Window

Saving and showing histograms for so many windows takes a lot of time. So we resized the image and saved and showed the histograms for the windows. For the larger image, we displayed two histograms, one at the start and one at the end.

CODE (to save and show histogram for every window)

```
from PIL import Image
from matplotlib import pyplot as plt
import numpy as np

L = 256

# returns the width and height of the image
def imageProperties(img):
    return img.size

# returns the number of pixels of each intensity level
def populateCountArray(img, startXpixel, endXpixel, startYpixel, endYpixel):
    countArray = [0] * 256
```



```
# load the pixels
```

```
pix = image.load()
```

```
# iterate through the pixels
```

```
for x in range(startXpixel, endXpixel):
```

```
    for y in range(startYpixel, endYpixel):
```

```
        # add 1 to the countArray whenever a particular intensity pixel is found
```

```
        countArray[pix[x, y]] += 1
```

```
return countArray
```

```
# probability distribution function
```

```
def pdf(array, width, height):
```

```
    pdfArray = [0] * 256
```

```
    # pdf = frequency / total no. of pixels
```

```
    for i in range(len(array)):
```

```
        # width * height is the total no. of pixels in that window
```

```
        pdfArray[i] = array[i] / (width * height)
```

```
    return pdfArray
```

```
# cummulative frequency distribution function
```

```
def cdf(array):
```

```
    cdfArray = [0] * 256
```

```
    # at every index, find the sum of current and all previous pdfs
```

```
    for i in range(len(array)):
```



```
    for j in range(i):
        cdfArray[i] += array[j]
    return cdfArray

# map cdf to intensity values
def transformation(array):
    transformed = [0] * 256
    for i in range(len(array)):
        transformed[i] = round(array[i] * (L - 1))
    return transformed

# plot the histogram
def showAndSaveHistogram(array, string):
    plt.title("Intensity Histogram")
    plt.xlabel("Intensity")
    plt.ylabel("Frequency")
    plt.bar([i for i in range(256)], array)
    plt.savefig(string + " histogram")
    plt.show()

# apply histogram equalization to the input image
def outputImage(array, img, startX,startY,endX,endY):
    pix = img.load()

    # iterate the pixels
    for x in range(startX,endX):
        for y in range(startY,endY):
            # change the intensity of the pixel to the transformed one
            pix[x, y] = array[pix[x, y]]
```



```
return img

def histogramFromArray(new_arr):
    new_img = Image.fromarray(new_arr)
    countArray = [0] * 256

    # load the pixels
    pix = new_img.load()
    (M,N) = new_img.size

    # iterate through the pixels
    for x in range(M):
        for y in range(N):
            # add 1 to the countArray whenever a particular intensity pixel is found
            countArray[pix[x, y]] += 1
    return countArray

# open image
image = Image.open("lab07_img_resized.png").convert('L')
M, N = image.size

pix = image.load()
new_arr = np.asarray(image).copy()

for i in range(int(M/2)):
    for j in range(int(N/2)):
```



```
histArray = populateCountArray(image, i, i + int(M/2), j, j + int(N/2))

pdfArray = pdf(histArray, int(M/2), int(N/2))

cdfArray = cdf(pdfArray)

transformed = transformation(cdfArray)

# save and show the histogram for the input image

showAndSaveHistogram(histArray, "input")


# get output image

output = outputImage(transformed, image, i, j, i + int(M/2), j + int(N/2))

histOutput = populateCountArray(output, i, i + int(M/2), j, j + int(N/2))

showAndSaveHistogram(histOutput, "output")


for x in range(i,i+int(M/2)):
    for y in range(j,j+int(N/2)):
        pix_val=pix[x,y]
        transform_val=transformed[pix_val]
        new_arr[y][x]=transform_val


image = Image.open("lab07_img_resized.png").convert('L')


arr2 = histogramFromArray(new_arr)

showAndSaveHistogram(arr2, "full_image")


Image.fromarray(new_arr).show()
```



```
1  from PIL import Image
2  from matplotlib import pyplot as plt
3  import numpy as np
4  L = 256
5
6  # returns the width and height of the image
7  def imageProperties(img):
8      return img.size
9
10 # returns the number of pixels of each intensity level
11 def populateCountArray(img, startXpixel, endXpixel, startYpixel, endYpixel):
12     countArray = [0] * 256
13
14     # load the pixels
15     pix = image.load()
16
17     # iterate through the pixels
18     for x in range(startXpixel, endXpixel):
19         for y in range(startYpixel, endYpixel):
20             # add 1 to the countArray whenever a particular intensity pixel is found
21             countArray[pix[x, y]] += 1
22
23     return countArray
```

```
24
25 # probability distribution function
26 def pdf(array, width, height):
27     pdfArray = [0] * 256
28
29     # pdf = frequency / total no. of pixels
30     for i in range(len(array)):
31         # width * height is the total no. of pixels in that window
32         pdfArray[i] = array[i] / (width * height)
33
34     return pdfArray
35
36 # cumulative frequency distribution function
37 def cdf(array):
38     cdfArray = [0] * 256
39
40     # at every index, find the sum of current and all previous pdfs
41     for i in range(len(array)):
42         for j in range(i):
43             cdfArray[i] += array[j]
44     return cdfArray
45
46 # map cdf to intensity values
47 def transformation(array):
48     transformed = [0] * 256
49     for i in range(len(array)):
50         transformed[i] = round(array[i] * (L - 1))
51     return transformed
52
```



```
53 # plot the histogram
54 def showAndSaveHistogram(array, string):
55     plt.title("Intensity Histogram")
56     plt.xlabel("Intensity")
57     plt.ylabel("Frequency")
58     plt.bar([i for i in range(256)], array)
59     plt.savefig(string + " histogram")
60     plt.show()
61
62 # apply histogram equalization to the input image
63 def outputImage(array, img, startX, startY, endX, endY):
64     pix = img.load()
65
66     # iterate the pixels
67     for x in range(startX, endX):
68         for y in range(startY, endY):
69             # change the intensity of the pixel to the transformed one
70             pix[x, y] = array[pix[x, y]]
71
72     return img
73
74 def histogramFromArray(new_arr):
75     new_img = Image.fromarray(new_arr)
76     countArray = [0] * 256
77
78     # load the pixels
79     pix = new_img.load()
80     (M, N) = new_img.size
81
82     # iterate through the pixels
83     for x in range(M):
84         for y in range(N):
85             # add 1 to the countArray whenever a particular intensity pixel is found
86             countArray[pix[x, y]] += 1
87     return countArray
```

```
88
89
90 # open image
91 image = Image.open("Lab07_img_resized.png").convert('L')
92 M, N = image.size
93
94
95 pix = image.load()
96 new_arr = np.asarray(image).copy()
97
```

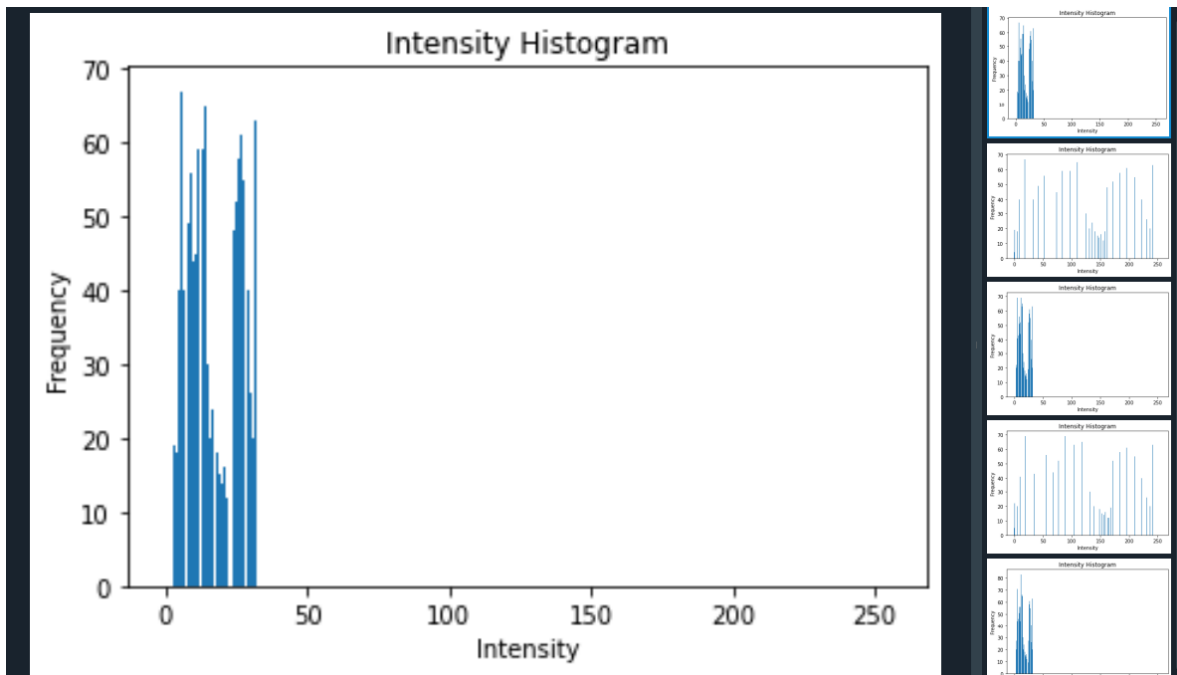


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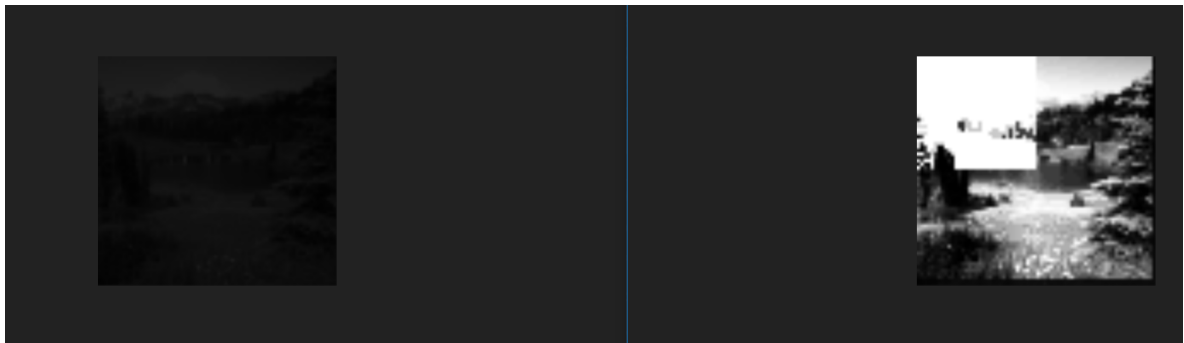
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```
98 for i in range(int(M/2)):
99     for j in range(int(N/2)):
100         histArray = populateCountArray(image, i, i + int(M/2), j, j + int(N/2))
101         pdfArray = pdf(histArray, int(M/2), int(N/2))
102         cdfArray = cdf(pdfArray)
103         transformed = transformation(cdfArray)
104         # save and show the histogram for the input image
105         showAndSaveHistogram(histArray, "input")
106
107         # get output image
108         output = outputImage(transformed, image, i, j, i + int(M/2), j + int(N/2))
109         histOutput = populateCountArray(output, i, i + int(M/2), j, j + int(N/2))
110         showAndSaveHistogram(histOutput, "output")
111
112     for x in range(i, i+int(M/2)):
113         for y in range(j, j+int(N/2)):
114             pix_val=pix[x,y]
115             transform_val=transformed[pix_val]
116             new_arr[y][x]=transform_val
117
118     image = Image.open("Lab07_img_resized.png").convert('L')
119
120 arr2 = histogramFromArray(new_arr)
121 showAndSaveHistogram(arr2, "full_image")
122
123 Image.fromarray(new_arr).show()
```

SOME OF THE HISTOGRAMS (can see on the right)



OUTPUT



CODE (to save and show histogram only at the start and end)

```
from PIL import Image
from matplotlib import pyplot as plt
import numpy as np
L = 256

# returns the width and height of the image
def imageProperties(img):
    return img.size

# returns the number of pixels of each intensity level
def populateCountArray(img, startXpixel, endXpixel, startYpixel, endYpixel):
    countArray = [0] * 256

    # load the pixels
    pix = image.load()

    # iterate through the pixels
    for x in range(startXpixel, endXpixel):
        for y in range(startYpixel, endYpixel):
            # add 1 to the countArray whenever a particular intensity pixel is found
            countArray[pix[x, y]] += 1
```



```
return countArray

# probability distribution function
def pdf(array, width, height):
    pdfArray = [0] * 256

    # pdf = frequency / total no. of pixels
    for i in range(len(array)):
        # width * height is the total no. of pixels in that window
        pdfArray[i] = array[i] / (width * height)

    return pdfArray

# cumulative frequency distribution function
def cdf(array):
    cdfArray = [0] * 256

    # at every index, find the sum of current and all previous pdfs
    for i in range(len(array)):
        for j in range(i):
            cdfArray[i] += array[j]
    return cdfArray

# map cdf to intensity values
def transformation(array):
    transformed = [0] * 256
    for i in range(len(array)):
        transformed[i] = round(array[i] * (L - 1))
```



```
return transformed

# plot the histogram
def showAndSaveHistogram(array, string):
    plt.title("Intensity Histogram")
    plt.xlabel("Intensity")
    plt.ylabel("Frequency")
    plt.bar([i for i in range(256)], array)
    plt.savefig(string + " histogram")
    plt.show()

# apply histogram equalization to the input image
def outputImage(array, img, startX,startY,endX,endY):
    pix = img.load()

    # iterate the pixels
    for x in range(startX,endX):
        for y in range(startY,endY):
            # change the intensity of the pixel to the transformed one
            pix[x, y] = array[pix[x, y]]

    return img

def histogramFromArray(new_arr):
    new_img = Image.fromarray(new_arr)
    countArray = [0] * 256

    # load the pixels
    pix = new_img.load()
```



```
(M,N) = new_img.size
```

```
# iterate through the pixels
```

```
for x in range(M):
```

```
    for y in range(N):
```

```
        # add 1 to the countArray whenever a particular intensity pixel is found
```

```
        countArray[pix[x, y]] += 1
```

```
return countArray
```

```
# open image
```

```
image = Image.open("lab07_img.png").convert('L')
```

```
M, N = image.size
```

```
# histogram before equalization
```

```
inputHistArray = populateCountArray(image, 0, M, 0, N)
```

```
showAndSaveHistogram(inputHistArray, "input")
```

```
pix = image.load()
```

```
new_arr = np.asarray(image).copy()
```

```
for i in range(int(M/2)):
```

```
    for j in range(int(N/2)):
```

```
        histArray = populateCountArray(image, i, i + int(M/2), j, j + int(N/2))
```

```
        pdfArray = pdf(histArray, int(M/2), int(N/2))
```

```
        cdfArray = cdf(pdfArray)
```

```
        transformed = transformation(cdfArray)
```

```
        for x in range(i,i+int(M/2)):
```



```
for y in range(j,j+int(N/2)):  
    pix_val=pix[x,y]  
    transform_val=transformed[pix_val]  
    new_arr[y][x]=transform_val
```

histogram after equalization

```
arr2 = histogramFromArray(new_arr)
```

```
showAndSaveHistogram(arr2, "full_image")
```

```
Image.fromarray(new_arr).show()
```

```
1  from PIL import Image  
2  from matplotlib import pyplot as plt  
3  import numpy as np  
4  L = 256  
5  
6  # returns the width and height of the image  
7  def imageProperties(img):  
8      return img.size  
9  
10 # returns the number of pixels of each intensity level  
11 def populateCountArray(img, startXpixel, endXpixel, startYpixel, endYpixel):  
12     countArray = [0] * 256  
13  
14     # load the pixels  
15     pix = image.load()  
16  
17     # iterate through the pixels  
18     for x in range(startXpixel, endXpixel):  
19         for y in range(startYpixel, endYpixel):  
20             # add 1 to the countArray whenever a particular intensity pixel is found  
21             countArray[pix[x, y]] += 1  
22  
23     return countArray
```



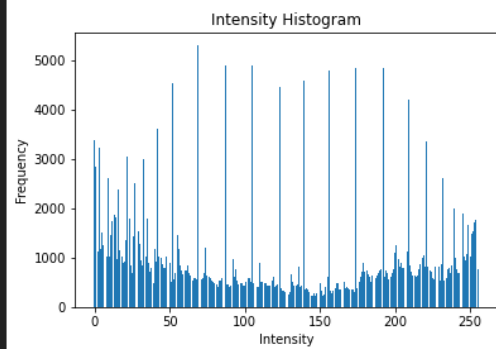
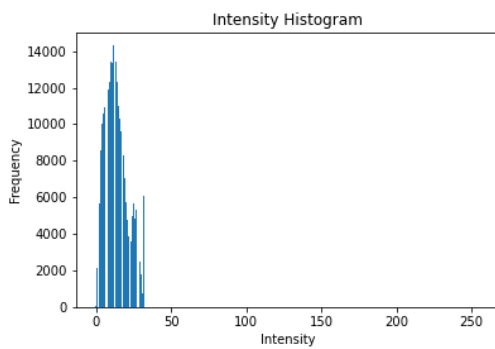
```
24
25 # probability distribution function
26 def pdf(array, width, height):
27     pdfArray = [0] * 256
28
29     # pdf = frequency / total no. of pixels
30     for i in range(len(array)):
31         # width * height is the total no. of pixels in that window
32         pdfArray[i] = array[i] / (width * height)
33
34     return pdfArray
35
36 # cumulative frequency distribution function
37 def cdf(array):
38     cdfArray = [0] * 256
39
40     # at every index, find the sum of current and all previous pdfs
41     for i in range(len(array)):
42         for j in range(i):
43             cdfArray[i] += array[j]
44     return cdfArray
45
46 # map cdf to intensity values
47 def transformation(array):
48     transformed = [0] * 256
49     for i in range(len(array)):
50         transformed[i] = round(array[i] * (L - 1))
51     return transformed
52
53 # plot the histogram
54 def showAndSaveHistogram(array, string):
55     plt.title("Intensity Histogram")
56     plt.xlabel("Intensity")
57     plt.ylabel("Frequency")
58     plt.bar([i for i in range(256)], array)
59     plt.savefig(string + " histogram")
60     plt.show()
61
62 # apply histogram equalization to the input image
63 def outputImage(array, img, startX, startY, endX, endY):
64     pix = img.load()
65
66     # iterate the pixels
67     for x in range(startX, endX):
68         for y in range(startY, endY):
69             # change the intensity of the pixel to the transformed one
70             pix[x, y] = array[pix[x, y]]
71
72     return img
```



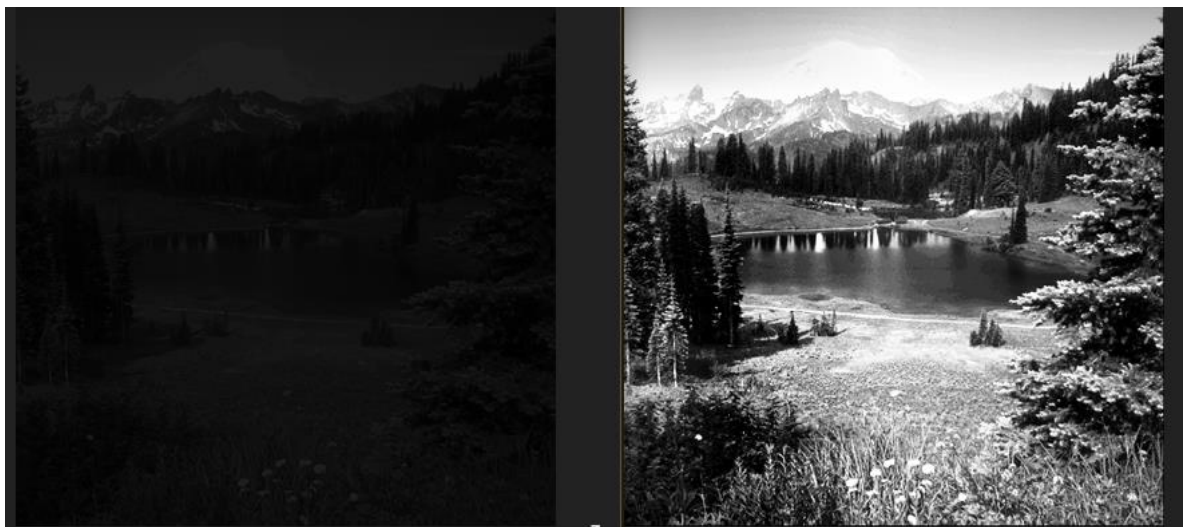
```
73
74 def histogramFromArray(new_arr):
75     new_img = Image.fromarray(new_arr)
76     countArray = [0] * 256
77
78     # load the pixels
79     pix = new_img.load()
80     (M,N) = new_img.size
81
82     # iterate through the pixels
83     for x in range(M):
84         for y in range(N):
85             # add 1 to the countArray whenever a particular intensity pixel is found
86             countArray[pix[x, y]] += 1
87     return countArray
88
89
90 # open image
91 image = Image.open("Lab07_img.png").convert('L')
92 M, N = image.size
93
94 # histogram before equalization
95 inputHistArray = populateCountArray(image, 0, M, 0, N)
96 showAndSaveHistogram(inputHistArray, "input")
97
98 pix = image.load()
99 new_arr = np.asarray(image).copy()
```

```
100
101 for i in range(int(M/2)):
102     for j in range(int(N/2)):
103         histArray = populateCountArray(image, i, i + int(M/2), j, j + int(N/2))
104         pdfArray = pdf(histArray, int(M/2), int(N/2))
105         cdfArray = cdf(pdfArray)
106         transformed = transformation(cdfArray)
107
108         for x in range(i,i+int(M/2)):
109             for y in range(j,j+int(N/2)):
110                 pix_val=pix[x,y]
111                 transform_val=transformed[pix_val]
112                 new_arr[y][x]=transform_val
113
114 # histogram after equalization
115 arr2 = histogramFromArray(new_arr)
116 showAndSaveHistogram(arr2, "full_image")
117
118 Image.fromarray(new_arr).show()
```

HISTOGRAMS



OUTPUT



Artifacts/ effects are observed when applying equalization at different levels in an image:

Using global histogram equalization, showed a result with good contrast.

In tiled histogram equalization, the edges/boundaries of the tiles are clearly visible making the image look like it's divided into 4 tiles.

In sliding window histogram equalization, the image is clearer than with the global histogram equalization. Unlike tiled histogram equalization, windows cannot be seen using sliding window method.