Benchmarking Local Robustness of High-Accuracy Binary Neural Networks for Enhanced Traffic Sign Recognition

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Overview

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- ▶ isolating the traffic sign in a bounding box
- ► classifying the sign into a specific traffic class.

Well-know problem of the classifiers: the lack of robustness¹ ².

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guence of physical road signs under different conditions





Physical road signs with adversarial





Video sequences taken under

different driving speeds



Modified from https://deepdrive.berkelev.edu



Different types of physical adversarial examples

Cropping, Resizing Stop Sign → Speed Limit Sign



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Solution:

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- ▶ logical methods: recently explored, scalability issues ~> this presentation, our long time goal

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These models should have high accuracy while amenable for formal verification.

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Characteristics that count in machine learning and formal verification:

► Layers' type: convolution (Conv), sign (Sgn), max pooling (MP), batch normalization (BN), fully connected (FC)

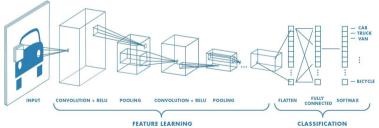
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From https://saturncloud.io/blog/a-comprehensive-guide-to-convolutional-neural-networks-the-eli5-way/

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Given a trained model and a property to be verified, does the model satisfy that property?

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Challenges:

- ► NP-complete problem⁴
- ► How to formalize the property to be verified

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Data collection



Training:

- GTSRB (German) traffic sign dataset.
 - Classes: 43,
 - Size: from 25 × 25 to 243 × 225, and not all of them are square.
 - Each class: 210 2250 images
 - 39209 images used for training and validation with ratio 80:20

Testing:

- GTSRB (German) traffic sign dataset.
 - ▶ 12630 images used for testing
- Belgium traffic sign dataset.
 - ► Number of images = 4533.
 - Only 23 classes match the one from GTSRB.
- Chinese traffic sign dataset.
 - ► Number of images = 1818.
 - ▶ Only 15 classes match the one from GTSRB.



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Difference between Belgium (left) and GTSRB (right) dataset



Difference between Chinese (left) and GTSRB (right) dataset

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BNNs Architectures with Best Accuracy⁵

The architectures below were obtained by a bottom-up approach, starting with simple layers (fully connected) and stacking new more complicated ones for higher accuracy.

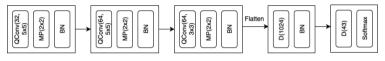


Figure: Architecture with Best Accuracy for GTSRB (96.45%) and Belgium (88.17%) dataset. Input: $64 \text{ px} \times 64 \text{ px}$

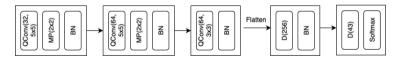


Figure: Architecture with Best Accuracy (83.9%) for Chinese dataset. Input: 48 px x 48 px

⁵More details in: A. Postovan, M, Erașcu. Architecturing binarized neural networks for traffic sign recognition. to appear in ICANN 2023

XNOR Architecture

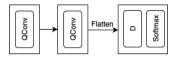


Figure: XNOR(QConv) architecture

Table: XNOR(QConv) architecture. Image size: $30px \times 30px$. Dataset for train and test: GTSRB.

Model description	Acc	#Binary	Model Size (in KiB)	
Woder description	Acc	Params	Binary	Float-32
$QConv(16, 3\times3), QConv(32, 2\times2), D(43)$	81.54	1005584	122.75	3932.16

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Local robustness ensures that for a given input x from a set χ , the neural network F remains unchanged within a specified perturbation radius ϵ , implying that small variations in the input space do not result in different outputs. The output for the input x is represented by its label I_x . We consider L_∞ norm defined as $||x||_\infty = \sup |x_n|$.

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Definition of local robustness useful in a computational setting. A network is ϵ -locally robust in the input x if for every x', such that $||x-x'||_{\infty} \leq \epsilon$, the network assigns the same label to x and x'.

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- 3. bounding constraints for the input variables: local robustness definition is used for generating the property taking into account that vector x (its elements are the values of the pixels of the image) and ε (perturbation) are known.

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4. constraints involving the output variables assessing the value of the output label.

```
(assert (or (>= Y_0 Y_38)
...
(>= Y_37 Y_38)
(>= Y_39 Y_38)
...
(>= Y 42 Y 38)))
```

Model Representation: Open Neural Network Exchange (ONNX)

- storage and organization of large amounts of data, including the parameters and architecture of machine learning models
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- ► ONNX representation of the neural network is transformed into a constraint satisfaction problem in the VNN-LIB format

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Randomly selected 3 distinct images from the test set of the GTSRB dataset for each model and have generated the VNN-LIB files for each epsilon in the set, in the way we ended up having 45 VNN-LIB files in total.

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Our benchmark was used for scoring the competing tools but different images were chosen in order to avoid tuning of the solvers for precise instances.



Experimental Results of the VNN-COMP 2023

Table: VNN-COMP 2023 Results for Traffic Signs Recognition Benchmark

#	Tool	Verified	Falsified	Fastest	Penalty	Score	Percent
1	Marabou	0	18	0	1	30	100%
2	PyRAT	0	7	0	1	-80	0%
3	NeuralSAT	0	31	0	4	-290	0%
4	alpha-beta-CROWN	0	39	0	3	-60	0%

- Verified is number of instances that were UNSAT (no counterexample) and proven by the tool.
- ▶ Falsified is number that were SAT (counterexample was found) and reported by the tool.
- ▶ **Fastest** is the number where the tool was fastest (this did not impact the scoring in this year competition). Penalty is the number where the tool gave the incorrect result or did not produce a valid counterexample.
- **Score** is the sum of scores (10 points for each correct answer and -150 for incorrect ones).
- ▶ **Percent** is the score of the tool divided by the best score for the benchmark (so the tool with the highest score for each benchmark gets 100) and was used to determine final scores across all benchmarks.

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- ▶ Investigate for which architectures the previous results were obtained.
- Investigate the potential for solving more instances by extending the time limit (currently set at 8 minutes).
- Understand the factors contributing to incorrect outputs from the tools on specific benchmark tasks.