

The Frogs Game

- Given
 - \circ n pairwise disjoint sets of size δ
- Task
 - Merging consecutive pairs of sets until there is only one set left
 - Every time cost is the sum of the sizes of K consecutive sets, left or right, whatever turns out cheaper
- Prove
 - \circ The total cost an adversary can generate here is $O(\delta \kappa n \log n)$



The Frogs Game

Algorithm

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- Iteratively merge adjacent sets, choosing pairs where the minimum sum of k left/right neighbors exists
- Calculate merge cost as the minimum between left k elements before or right k elements after the merge position
- Repeat greedily until one set remains, accumulating minimal total merging cost
- Pre-Compute left sum and right sum for each index to reduce the time complexity