Inner loop optimizations in mapping single-threaded programs to hardware

Author's name Suppressed for Blind Review

Abstract—In the context of mapping high-level algorithms to hardware, we consider the basic problem of generating an efficient hardware implementation of a single threaded program. in particular, that of an inner loop. We describe a control-flow mechanism through which multiple iterations of an arbitrary inner loop can be made simultaneously active in the generated hardware, thus providing dynamic loop-pipelining capability in hardware. We study the impact of this loop-pipelining scheme in conjunction with source-level loop-unrolling. In particular, we consider some common loop kernels occurring in fast-fourier transform, matrix multiplication and inner product computations, with the resulting hardware descriptions synthesized to an FPGA target. We observe that the use of dynamic loop-pipelining mechanism alone typically results in a significant improvements in the performance of the hardware. If the loop is statically unrolled and if loop-pipelining is applied to the unrolled program, then the performance improvement is still substantial. When both optimizations are used in conjunction, the improvement in performance ranges from 6X to 20X (in terms of number of clock cycles needed for the computation) across the loop kernels that we have studied. These optimizations do have a hardware overhead, but, in spite of this, we observe that the joint use of these loop optimizations not only improves performance, but also the performance/cost ratio of the resulting hardware.

I. INTRODUCTION

A high-level-synthesis (HLS) compiler takes an algorithm described in a high-level programming language (such as C, for example) and produces a circuit description (a register-transfer-level description in a hardware description language such as VHDL, for example). High-level synthesis systems have been available for some time now (for example, [1], [2] and commercial tools such as Catapult-C¹ from Mentor Graphics C-to-Silicon² from Cadence, Synopsys HLS³ from Synopsys).

The main attraction of such a compiler is a substantial reduction in the design and verification effort. The main concern is the quality of the hardware that is produced. For the same starting point, the quality of the hardware produced may be objectively measured in terms of factors such as area, energy-consumption and performance (in the sense of time required for completion, or in terms of the rate at which the hardware finishes the computational tasks). An *internal measure* of the quality of the hardware produced is the utilization factor of the major resources in the hardware (that is, the utilization factor of expensive resources).

In our work, we have developed a set of compiler tools which take a C-description of an algorithm (with the only

important restrictions being the requirement that cycles are not present in the call graph of the source program, and the lack of support for **function** pointers, normal pointers are supported), and produces a VHDL description which is provably equivalent to the original program [3]. Results on the application of this compiler to single-threaded programs show that the circuits (when synthesized to VLSI layout) are substantially more energy efficient than a processor, but that the performance of the processor is usually better than that of the synthesized circuit [4]. If multi-threaded source programs are used as a starting point, the circuits produced are quite competitive with hand-designed RTL [5]. Quantitatively, the results in [4] and [5] indicate that the gap between the synthesized hardware and modern pipelined processors (for singlethreaded programs) and between the synthesized hardware and hand-crafted hardware (for multi-threaded programs) is of the order of 2-3X. That is, the performance of the synthesized hardware needs to improve by 2-3X in order to close the respective performance gaps.

In this paper, we consider the problem of improving the performance of hardware generated from single threaded programs; in particular, the problem of mapping loops to hardware. It is well known that most compute intensive programs spend a large fraction of their time in inner loops. Thus, the optimal implementation of such loops is of primary importance, whether the target is a processor or hardware. Such an improvement is essential if synthesized hardware is to be performance competitive with high performance processors or with hand-crafted hardware.

In the context of compilation to a pipelined processor, several loop optimizations have been considered in literature, such as loop-unrolling, loop-peeling, software-loop-pipelining etc. [6], [7], with the intent of these optimizations being the extraction of as much parallelism as possible from the single-threaded source program.

Similar loop-optimization techniques have been explored and reported in the literature related to reconfigurable hardware (for example [8], [9], [10]). For instance, in the work reported by [8], loop optimizations are done in a manner analogous to the static techniques used in software compilers, in which index expressions which depend on the induction variable are analysed to identify dependencies and schedule operations across iterations of the loop body. An explicitly timed controller is synthesized for the pipeline. Another approach which works in a similar manner is described in [9]. These approaches rely on a static analysis of the loop, and the cases to which the approach can be applied are restricted (but

¹http://www.mentor.com/products/esl/high_level_synthesis/

²http://www.cadence.com/products/sd/silicon_compiler/

³http://www.synopsys.com/Tools/SLD/HLS/

are still sufficiently general for most linear algebra and digital signal processing kernels).

In our approach, the hardware model is abstracted as a virtual circuit which consists of a data-path (a graph of operations interconnected by wires) and a control-path which is modeled as a Petri-net. The operations in the data-path are not tightly scheduled, with dependencies being taken care of by the control Petri-net (for example: operation X can start only after operations Y, Z have finished etc.). This representation allows the implementation of loop pipelining by a simple modification to the control Petri-net without altering the data-path. It is possible to pipeline any loop, even those that do not have explicit induction variables (such as while loops). We will describe this loop-pipelining mechanism in a later section in this paper.

The experimental results in this paper are based on the dynamic loop-pipelining optimization applied by itself and in conjunction with static loop-unrolling. By loop-unrolling, we mean a static source-level or compile-time optimization technique in which an inner loop is unrolled by instantiating multiple copies of the loop-body while simultaneously reducing the number of loop-iterations. For example:

```
for(i=0; i < 8; i++) {
   x += a[i]*b[i];
is transformed to
for(i=0; i < 4; i+=2) {
   int i1 = i+1; int i2 = i+2; int i3 = i+3; the mechanism of guarded (or predicated) execution.
   x += a[i]*b[i];
   x += a[i1]*b[i1];
   x += a[i2]*b[i2];
   x += a[i3]*b[i3];
}
```

This unrolling increases the size of the basic block (that is, the maximal sequence of statements without any branches), and provides the possibility of extracting more parallelism in the loop. Note that this unrolling can be done manually by the programmer, or automatically by an optimizing compiler.

In the remainder of this paper, we will first briefly describe the model of the hardware that is produced by our HLS compiler and illustrate how this model can incorporate dynamic run-time loop pipelining. The chief issues here are the hardware overhead (area, energy, delay) incurred by the need to provide this run-time support in the hardware generated by the compiler, and the corresponding improvement in performance that results from this optimization. In the results presented in this paper, the unrolling has been done manually at the source code level.

In order to address this issue, we will present a set of observations from experiments performed on representative inner loops that occur in some important applications such as the fast-fourier transform, the matrix product, vector dot-product, and a digital filtering algorithm. These observations report the hardware performance on four different loop-optimization choices: with no loop optimization, with static unrolling alone, with dynamic loop pipelining alone, and with static unrolling combined with dynamic loop pipelining. Hardware resource utilization and delays are computed by synthesizing and simulating the generated hardware for an FPGA target.

The observations indicate the following:

- The performance improvement with loop-pipelining applied alone is in the 2X-3X range.
- The performance improvement with loop-unrolling alone is in the 2X range, and with aggressive unrolling (as was tried in the matrix multiplication case), the improvement is as high as 10X.
- The combination of loop-pipelining and loop-unrolling leads to a performance improvement which is at least as high as the product of the improvements due to the individual optimizations. For matrix multiplication, this improvement is as large as 20X.
- The hardware overheads for implementing these optimizations are considerable, but the cost-to-performance ratio improves substantially in all cases.

The results indicate that loop-unrolling combined with dynamic loop-pipelining can close the performance gap noted

For the subsequent discussion, we assume that the inner loop which is being optimized consists of a single basic block, that is, there are no branching instructions in the loop body (no jumps, if constructs, switch constructs etc.). If such constructs are present, we assume that they have been eliminated using

II. A NOTE ON OUR COMPILER FLOW

We give a brief description of our compiler flow. The details are not relevant to this paper, and the interested reader can find them in [4].

Our compiler starts with a C program and produces VHDL. For the C front-end, we use the clang-2.8 compiler⁴. This compiler is used to emit LLVM byte-code⁵, which is then transformed to VHDL using the following transformations:

- 1) The LLVM byte-code is translated to an internal intermediate format, which is itself a static-single assignment centric control-flow language (named Aa) which allows the description of parallelism using fork-join structures as well as arbitrary branching [11].
- 2) The Aa description is translated to a virtual circuit (the model is described in the next section). During this translation, the following major optimizations are performed: declared storage objects are partitioned into disjoint memory spaces using pointer reference analysis, and dependency analysis is used to generate appropriate sequencing of operations in order to maximize the parallelism.
- 3) The virtual circuit is then translated to VHDL. At this point, decisions about operator sharing are taken.

⁴www.clang.org

⁵www.llvm.org

Concurrency analysis is used to determine if a shared hardware unit needs arbitration. Optimizations related to clock-frequency maximization are also carried out here. The generated VHDL uses a pre-designed library of useful operators ranging from multiplexors, arbiters to pipelined floating point arithmetic units.

The compiler flow has been characterized over a wide variety of applications [4]. The XXXX⁶ tool-chain [5] uses this compiler flow to map modular network appliances written in C++ to an FPGA platform, and achieved about half the performance possible using equivalent hand designed hardware. Thus, the flow can be applied to "real" software to produce competitive results. The optimizations indicated in this paper, should in principle, make the flow even more competitive.

III. MODEL OF THE VIRTUAL CIRCUIT GENERATED BY OUR COMPILER

The virtual circuit generated by our compiler consists of three cooperating components: the control-path, the data-path and the storage system [4].

To illustrate the model, we consider a simple example.

```
float a[1024], b[1024];
float dotp = 0.0;
for(i=0; i < 1024; i++)
{
    dotp += a[i]*b[i];
}</pre>
```

To compile this code, we use the clang-2.8 C compiler, which is used to emit LLVM byte-code. The LLVM byte-code is transformed through a series of steps by our compiler tools to produce a virtual circuit, which is depicted in Figure 1. The virtual circuit in Figure 1 has three components, described below.

A. Data-path

The data-path is a directed hyper-graph with nodes being operations and arcs being nets (shown as ovals). Each net has at most one operation which drives it. Further, most operations have a split protocol handshake with the controlpath: two pairs of request/acknowledge associations (*sr/*sa for sampling the inputs and *cr/*ca for updating the outputs). The operation samples its inputs on receiving the sr request symbol and acknowledges the completion of this action by emitting the sa acknowledge symbol. After receiving the cr symbol, the operation will update its output net using the newly computed value. The sequencing is required to be

```
sr -> sa -> cr -> ca
```

Note that an operation can be re-triggered while an earlier edition of the operation is in progress (this is important if the operation is implemented in a pipelined operator).

Some data-path operations (such as the multiplexor shown on the top and the decision operation shown at the bottom left in Figure 1) follow a simpler protocol. The multiplexor has a pair of requests and a single acknowledge, with the condition that at most one of the requests is received at any time instant. The input corresponding to the request is then sampled and stored in the output net of the multiplexor. The decision operation has a single request and two acknowledes. Upon receipt of the request symbol, the decision operation checks its input net and emits one of the two acknowledges depending on whether the input is zero/non-zero.

In Figure 1, the following data-path operations are instantiated:

```
mI, mdotP multiplexors for I, dotP.

INCR increment for I++

LA load for a[I]

LB load for b[I]

FMUL multiply for p=a[I]*b[I]

FADD add for dotP += a*b

CMP EQ compare for COND=(I==1023)

D decision COND?
```

Remark Note that the data-path only shows the operations and their interconnection. When the data-path is implemented as hardware, multiple operations may be mapped to a single operator depending on cost/performance tradeoffs. When this is done, multiplexing logic is introduced in the hardware. These decisions and manipulations are performed in the compiler stage which is responsible for transforming the virtual circuit to VHDL.

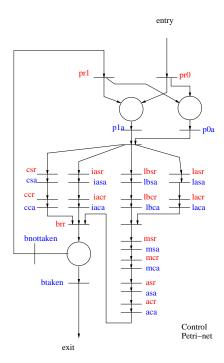
B. Storage subsystem

The load and store operations in the data-path are associated with memory subsystems. In general, there can be multiple disjoint memory subsystems inferred by our compiler. In this particular case, the arrays a[] and b[] are mapped to disjoint memories, due to which the two loads are allowed to proceed in parallel (the relaxed consistency model is enforced). In order to maintain the relaxed consistency model, the memory subsystems are designed to use a time-stamping scheme which guarantees first-come-first-served access to the same memory location.

C. Control-path

The control-path in the virtual circuit encodes all the sequencing that is necessary for correct operation of the assembly. The control-path (shown on the left in Figure 1) is modeled as a Petri-net with a unique entry point and a unique exit point. The Petri-net is constructed using a set of production rules which guarantee liveness and safeness [4]. Transitions in the Petri-net are associated with output symbols to the data-path (these can be described by the regular expressions *sr and *cr) and input symbols from the data-path (these are of the form *sa and *ca). The *sr symbols instruct an element in the data-path to sample its inputs and the *cr symbols instruct an element in the data-path to update its outputs (all outputs of data-path elements are registered).

⁶name suppressed for blind review.



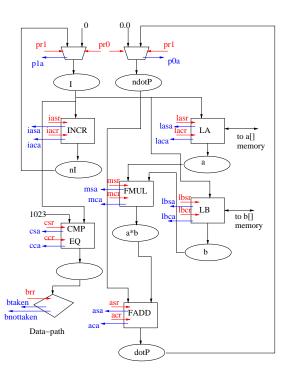


Fig. 1. Control-data-storage virtual circuit model.

The *sa and *ca symbols are acknowledgements from the datapath which indicate that the corresponding requests have been served.

The following classes of dependencies are encoded in the control Petri-net:

- Read-after-write (RAW): If the result of operator A is used as an input to operator B, the sr symbol to B can be emitted only after the ca symbol from A has been received.
- Write-after-read (WAR): If B writes to a net whose value needs to have been used by A earlier, for example as in

```
a = (b+c) -- operation A reads c
 c = (p*q) -- operation B writes to c
```

where there is a WAR dependency through c, then the cr request to B can be issued only after the sa acknowledge from A has been received.

• Load-Store ordering: If P,Q are load/store operations to the same memory subsystem, and if at least one of P,Q is a store, and if P is supposed to happen before Q, then the sr request to Q must be emitted only after the sa acknowledge from Q has been received. The memory subsystem itself guarantees that requests finish in the same order that they were initiated. This takes care of WAR, RAW and WAW memory dependencies.

The control-path in 1 shows the sequencing generated by these rules. Note that the data-path is not party to any sequencing decisions (other than responding to the request symbols).

IV. A CONTROL-FLOW MECHANISM FOR LOOP-PIPELINING

Suppose that we want to modify the control-path in order to permit the second (and maybe third etc.) iteration of a loop to begin while the first iteration is still in progress. Consider the example of the dot product. The original loop was

```
float a[1024], b[1024];
float dotp = 0.0;
for(i=0; i < 1024; i++)
{
    dotp += a[i]*b[i];
}</pre>
```

The fully unrolled version of this loop would be

```
float a[1024], b[1024];
float dotp = 0.0;
dotp += a[0]*b[0];
dotp += a[1]*b[1];
dotp += a[2]*b[2];
...
dotp += a[1023]*b[1023];
```

Let A denote the * operation and let B denote the + operation, L_a , L_b denote the loads from a and b respectively. In principle, all the loads can occur simultaneously, and all the multiplies can happen simultaneously once the loads complete. The adds would need to be ordered because of the multiply-accumulate nature of the code as it is written. Any ordering of these operations which satisfies these dependencies will be termed a fully-unrolled consistent ordering.

In our dynamic loop pipelining scheme, we use the following ordering scheme. If A is an operation in the loop body,

denote the k^{th} execution of A by A_k . Since each operation has events sr, sa, cr, ca, we denote these by $A_k.sr$, $A_k.sa$, $A_k.cr$, $A_k.ca$ respectively. We impose the following dependency rules on operations across loop iterations.

- A_k.sa → A_{k+1}.sr for all operations A: that is, the next execution of A cannot start until the current execution has finished sampling the inputs.
- $A_k.ca \rightarrow A_{k+1}.cr$ for all operations A: that is, the completion of the next execution of A can be initiated only after the current execution of A has completed.
- If A → B is a RAW dependency, then B_k.sa → A_{k+1}.cr.
 That is, until B has sampled the result of the current A, the next completion of A cannot start.
- If $A \to B$ is a WAR dependency, then $B_k.ca \to A_{k+1}.sr$. That is, the next A cannot start until the current B has completed.
- If P, Q are successive load/stores, with at least one of them being a store, then Q_k.sa → P_{k+1}.sr. That is, the next P cannot start until the current Q has acknowledged that it has started.

The mechanism for incorporating RAW and WAR dependencies is illustrated in Figure 2 for RAW and WAR dependencies within the loop body. The reverse dotted arc is a marked arc (it initially carries a single token).

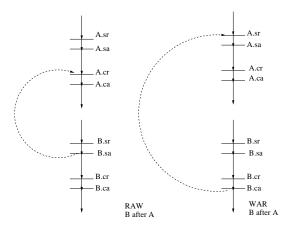


Fig. 2. Control-path mechanism for handling RAW, WAR dependencies for loop-pipelining.

It is easy to confirm that these additional dependencies ensure that the loop execution subject to these dependencies is a fully-unrolled consistent ordering. The modified control path is shown in Figure 3. The loop-terminator element has three inputs: a loop-taken transition, a loop-not-taken transition and a loop-body-exit transition. The loop-taken/not-taken pair indicates whether a new iteration is to be started or whether the loop has terminated. The loop-body-exit transition indicates that the body of the loop has finished executing an iteration. The loop-terminator initiates a new iteration as long as the number of active iterations is within a specified limit M (usually, we keep this limit to M=8). Thus, all the places in the modified control path in Figure 3 now must have a capacity of M and the cost of implementing each place in the

control path goes up by a factor of $\log M$. This is the major additional cost incurred by the pipelining mechanism.

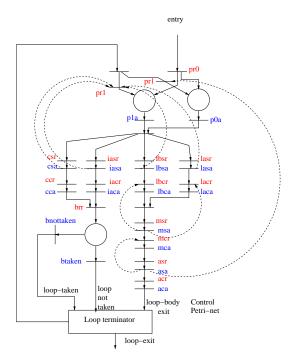


Fig. 3. Modified control-path with loop-pipeline dependencies (dotted lines).

V. EXPERIMENTAL RESULTS

We considered three examples, the dot product, the fast-fourier-transform, and matrix multiplications, each with critical inner loops. Four configurations were tested in each case: the basic code, the unrolled code, the basic code with loop-pipelining and the unrolled code with loop-pipelining. In each case, the generated VHDL code was synthesized to a Xilinx Virtex-6 FPGA and synthesis results were used to estimate the resource usage, the clock frequency and the number of cycles required by the inner loop.

VI. THE DOT PRODUCT

The basic code (a,b are arrays, dotP is the accumulated dot-product):

```
for(I=0; I < 64; I++)
{
  dotP += a[I]*b[I];
}</pre>
```

The unrolled version of the code used:

The results are shown in Table I. The number of clock-cycles needed to complete the inner loop, the number of look-up tables needed, the number of flip-flops needed and the post-synthesis clock frequency estimate are reported in the table. The last two rows correspond to the normalized performance (time needed by the plain case relative to the optimized case, higher is better), and the normalized performance/cost ratio (time/(LUTs+FF) ratio normalized with respect to the plain case, higher is better).

TABLE I
DOT-PRODUCT RESULTS WITH AND WITHOUT LOOP-OPTIMIZATIONS

	plain	pipelined	unrolled	pipelined
				+ unrolled
Cycles	4071	1874	1894	582
LUTs	4288	5195	4809	7344
FFs	3799	4345	4378	5911
Freq.(MHz)	199.7	199.7	199.7	199.7
Norm. Perf.	1	2.17	2.15	7
Norm. Perf/Cost	1	1.83	1.89	4.27

From Table I, we see

- If loop-pipelining is applied to the plain program, performance improves by about 2X relative to the nonpipelined, plain case.
- If loop-pipelining is applied to the unrolled program, performance improves by more than 3X relative to the non-pipelined, unrolled case.
- In terms of the performance/cost ratio, the pipelined-unrolled version is more than 3X better than the plain version. The normalized performance/cost ratio is 4X better when both loop optimizations are used.

VII. THE FAST-FOURIER-TRANSFORM (FFT)

A 64 point FFT program (radix two, in-place, twiddle factors computed apriori) with the following loop-structure was used:

```
for(STAGE=0; STAGE < 6; STAGE++)
{
  for(BFLY=0; BFLY < 32; BFLY++)
  {
    Butterfly(STAGE,BFLY);
  }
}</pre>
```

where the function **Butterfly** is inlined and implements the radix-two butterfly with index BFLY in stage STAGE using the precomputed twiddle factors. In the unrolled version, the inner-loop was rewritten as

```
for(BFLY=0; BFLY < 32; BFLY += 4)
{
   Butterfly(STAGE,BFLY);
   Butterfly(STAGE,BFLY+1);
   Butterfly(STAGE,BFLY+2);
   Butterfly(STAGE,BFLY+3);
}</pre>
```

The results are shown in Table II (the cycle count is for a single stage of the FFT). From Table II, we see

TABLE II FFT-results with and without loop-optimizations

	plain	pipelined	unrolled	pipelined
				+ unrolled
Cycles	4151	2885	3110	1064
LUTs	12155	23139	16032	37831
FFs	11955	18632	15299	28698
Freq.(MHz)	186.9	164.1	186.9	164.7
Norm. Perf.	1	1.26	1.33	3.42
Norm. Perf/Cost	1	0.73	1.02	1.24

- If loop-pipelining is applied to the plain program, performance improves by about 1.26X relative to the nonpipelined, plain case.
- If loop-pipelining is applied to the unrolled program, performance improves by more than 2.5X relative to the non-pipelined, unrolled case.
- In terms of the performance/cost ratio, the pipelinedunrolled version is only 1.24X better than the plain version.

The reason for the poorer results in this case is the use of the in-place algorithm. The bottleneck in this case becomes the access to the memory subsystem in which the array is stored.

VIII. MATRIX MULTIPLICATION

The plain triple loop matrix multiplication algorithm was used as a starting point.

```
float a[16]16], b[16][16], c[16][16];
for(i = 0; i < 16; i++) {
  for(j=0; j < 16; j++) {
    float v = 0.0;
    for(k = 0; k < 16; k++) {
      v += a[i][k]*b[k][j];
    }
    c[i][j] = v;
}</pre>
```

The unrolled version was aggressively generated so that the inner loop simultaneously computes 16 entries of the product at a time.

```
+ a[i+3][k+1]*b[k+1][j+3]
+ a[i+3][k+2]*b[k+2][j+3]
+ a[i+3][k+3]*b[k+3][j+3]);
}
c[i][j] = v00;
..
c[i+3][j+3] = v33;
}
```

The observations are shown in Table III. From Table II, we

TABLE III

MATRIX-MULTIPLICATION-RESULTS WITH AND WITHOUT

LOOP-OPTIMIZATIONS

	plain	pipelined	unrolled	pipelined
				+ unrolled
Cycles	161K	77K	13K	7810
LUTs	6323	9408	14891	31744
FFs	6974	8818	12041	21060
Freq.(MHz)	199.7	199.7	186.1	164.1
Norm. Perf.	1	2.09	11.5	16.9
Norm. Perf/Cost	1	1.52	5.67	4.25

see

- If loop-pipelining is applied to the plain program, performance improves by about 2X relative to the nonpipelined, plain case.
- If loop-pipelining is applied to the unrolled program, performance improves by 1.5X relative to the non-pipelined, unrolled case.
- In terms of the performance/cost ratio, the pipelinedunrolled version is only 4.25X better than the plain version.

In this instance, the aggressive loop-unrolling shows excellent performance. Loop-pipelining when combined with loop-unrolling, gives a 20X improvement in the cycle count. The normalized performance and performance/cost improvements are also substantial.

IX. CONCLUSION

We have considered the problem of optimizing inner loop implementations in an algorithm-to-hardware compilation system. Two optimizations were considered: static source-level loop unrolling and dynamic hardware supported loop-pipelining. The loop-pipelining mechanism is implemented by modifying the control-flow in the generated hardware (without disturbing the data-path).

The data obtained from three common and important inner loop kernels is encouraging. In all three cases, both loop-pipelining and loop-unrolling lead to substantial performance gains. Further, using both optimizations together results in multiplicative gains and in call cases, leads to hardware which is substantially faster and more efficient (in terms of the performance/cost ratio). The performance gain is lower if there is a bottleneck in the algorithm itself, such as in the FFT case,

in which accesses to the in-place array reduce the performance gains seen due to the loop optimizations.

Loop-unrolling is a common parallelization optimization in compilers that target pipelined processors. Our data indicates that such unrolling offers significant benefits (up to an order of magnitude) in an algorithm-to-hardware translation. Further, the use of hardware based dynamic loop-pipelining techniques seems to offer a further boost in performance in the synthesis of hardware from single-threaded programs. The performance boost provided by the dynamic loop-pipelining in hardware seems to indicate that its use, especially in conjunction with aggressive loop unrolling can offer a substantial reduction in the gap between the quality of automatically generated hardware and hand crafted hardware implementations of the same algorithm. This needs to be investigated further.

REFERENCES

- G. Venkataramani, M. Budiu, T. Chelcea, and S. Goldstein, "C to Asynchronous Dataflow Circuits: An End-to-End Toolflow," in *International Workshop on Logic & Synthesis*, Temecula, CA, June 2004, pp. 501

 508
- [2] S. Gupta, N. Dutt, R. Gupta, and A. Nicolau, "SPARK: A High-Level Synthesis Framework For Applying Parallelizing Compiler Transformations," in *International Conference on VLSI Design*, January 2003.
- [3] S. D. Sahasrabuddhe, "A competitive pathway from high-level programs to hardware." Ph.D. dissertation, IIT Bombay, 2009.
- [4] S. for Blind Review, "Suppressed for Blind Review," in Suppressed for Blind Review, Suppressed for Blind Review 2010, p. Suppressed for Blind Review
- [5] —, "Suppressed for Blind Review," in Suppressed for Blind Review, Suppressed for Blind Review 2012, p. Suppressed for Blind Review.
- [6] M. Wolfe, High Performance Compilers for Parallel Computing. Addison-Wesley, 1995.
- [7] S. S. Muchnick, Advanced Compiler Design and Implementation. Morgan Kaufmann. 1997.
- [8] M. Weinhardt and W. Luk, "Pipeline Vectorization," *IEEE Transactions on the Computer-aided Design of Integrated Circuits and Systems*, vol. 20, no. 2, pp. 234–248, 2001.
- [9] J. Cardoso, "Self Loop Pipelining and Reconfigurable Dataflow Arrays," in Computer Systems: Architecture, Modeling and Simulation, LNCS 3133. Springer Verlag, July 2004, pp. 234–243.
- [10] R. Kastner, "Synthesis techniques and optimizations for reconfigurable systems," Ph.D. dissertation, University of California, Los Angeles, 2002.
- [11] S. for Blind Review, "Suppressed for Blind Review," Suppressed for Blind Review, Suppressed for Blind Review, Tech. Rep. Suppressed for Blind Review, 2012.