

Exam.	Back	Full Marks	80
Level	BE	Pass Marks	32
Programme	All (Except B.Arch.)	Time	3 hrs.
Year / Part	II / I		

**Subject:** - Engineering Mathematics III (SH501)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.

1. Define the determinant as a function and using its properties. Show that

$$\begin{vmatrix} b+c & c+a & a+b \\ q+r & r+p & p+q \\ y+z & z+x & x+y \end{vmatrix} = 2 \begin{vmatrix} a & p & x \\ b & q & y \\ c & r & z \end{vmatrix}$$

[5]

2. If A and B are orthogonal matrices of same order, prove that the product AB is also orthogonal.

[5]

3. Test the consistency of the system  $x - 2y + 2z = 4$ ,  $3x + y + 4z = 6$  and  $x + y + z = 1$  and solve completely if found consistent.

[5]

4. For a matrix  $A = \begin{pmatrix} 5 & 4 \\ 1 & 2 \end{pmatrix}$ , find the modal matrix and the corresponding diagonal matrix.

[5]

5. Prove that line integral  $\int_A^B \vec{F} \cdot d\vec{r}$  is independent of path joining any two points A and B in the region if and only if  $\int_C \vec{F} \cdot d\vec{r} = 0$  for any simple closed curve C in the region.

[5]

6. Verify Green's theorem in the plane for  $\int_C [(3x^2 - 8y^2)dx + (4y - 6xy)dy]$  where C is region bounded by  $y = x^2$  and  $x = y^2$ .

[5]

7. Evaluate  $\iint_S \vec{F} \cdot \vec{n} ds$  where  $\vec{F} = 6z \vec{i} - 4 \vec{j} + y \vec{k}$  and S is the region of the plane  $2x + 3y + 6z = 12$  bounded in the first octant.

[5]

8. Evaluate using Gauss divergence theorem,  $\iint_S \vec{F} \cdot \vec{n} ds$  where  $\vec{F} = x^2y \vec{i} + xy^2 \vec{j} + 2xyz \vec{k}$  and S is the surface bounded by the planes  $x = 0$ ,  $y = 0$ ,  $z = 0$ ,  $x + 2y + z = 2$ .

[5]

9. Obtain the Fourier Series to represent  $f(x) = x - x^2$  from  $x = -\pi$  to  $x = \pi$  and deduce that

$$\frac{\pi^2}{12} = \frac{1}{1^2} - \frac{1}{2^2} + \frac{1}{3^2} - \frac{1}{4^2} + \dots$$

[5]

10. Obtain the half range Fourier Sine Series for  $f(x) = \pi - x$  in the range  $0 < x < \pi$ .

[5]

11. State the conditions for existence of Laplace transform. Obtain the Laplace transform of:

(i)  $e^{2t} \cos^3 2t$       (ii)  $\frac{\cos 2t - \cos 3t}{t}$

[1+2+2]

12. Find the inverse Laplace transform of:

(i)  $\frac{1}{(S-2)(S^2+1)}$

(ii)  $\cot^{-1}(S+1)$

[2.5+2.5]

13. Solve the following intial value problem by using Laplace transform:

$y'' + 4y' + 3y = e^t$ ,  $y(0) = 0$ ;  $y'(0) = 2$

[5]

14. Graphically maximize  $Z = 7x_1 + 10x_2$

Subject to constraints:

$$3x_1 + x_2 \leq 9$$

$$x_1 + 2x_2 \leq 8$$

$$x_1, x_2 \geq 0.$$

[5]

15. Solve the following linear Programming Problem by simple method:

Maximize:  $Z = 3x_1 + 5x_2$

Subject to:

$$3x_1 + 2x_2 \leq 18$$

$$x_1 \leq 4, x_2 \leq 6$$

$$x_1, x_2 \geq 0.$$

[10]

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Exam.		Regular	
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**Subject:** - Engineering Mathematics III (SH501)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
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1. If  $\begin{vmatrix} a & a^2 & a^3 - 1 \\ b & b^2 & b^3 - 1 \\ c & c^2 & c^3 - 1 \end{vmatrix} = 0$  where  $a \neq b \neq c$ ; apply properties of determinant to show  $abc = 1$ . [5]
2. If A be an  $n \times n$  matrix, prove that  $\text{Adj}(A) \cdot A = A \cdot (\text{Adj}A) = |A|I$  where I is an  $n \times n$  unit matrix. [5]
3. Find the rank of the following matrix by reducing it into normal form:  

$$\begin{pmatrix} 3 & 1 & 4 \\ 0 & 5 & 8 \\ -3 & 4 & 4 \\ 1 & 2 & 4 \end{pmatrix}$$
 [5]
4. Find the modal matrix for the matrix  

$$A = \begin{pmatrix} 2 & 1 & 1 \\ -2 & 1 & 3 \\ 2 & 1 & -1 \end{pmatrix}$$
 [5]
5. State and prove Green's theorem in plane. [5]
6. Find the total work done in moving the particle in a force field given by  $\vec{F} = \sin y \vec{i} + x(1+\cos y) \vec{j}$  over the circular path  $x^2 + y^2 = a^2$ ,  $z=0$ . [5]
7. Evaluate  $\iint_S \vec{F} \cdot d\vec{s}$  where  $\vec{F} = x \vec{i} - y \vec{j} + z \vec{k}$  and S is the surface of the cylinder  $x^2 + y^2 = a^2$ ,  $0 < z < b$ . [5]
8. Verify Stoke's theorem for  $\vec{F} = (x^2 + y^2) \vec{i} - 2xy \vec{j}$  taken round the rectangle bounded by the lines  $x = \pm a$ ,  $y = 0$ ,  $y = b$ . [5]
9. Obtain Fourier series for  $f(x) = x^3$  in the interval  $-\pi \leq x \leq \pi$ . [5]
10. Express  $f(x) = e^x$  as a half range Fourier Cosine Series in  $0 < x < 1$ . [5]
11. State existence theorem for Laplace Transform. Obtain the Laplace transform of

a)  $te^{-t} \sin t$

b) 
$$\frac{e^{-at} - e^{-bt}}{t}$$

1+2+2]

12. Find the inverse Laplace transform of:

a)  $\frac{1}{s^2 - 5s + 6}$

b)  $\tan^{-1} \frac{2}{s}$

[2+5.+2.5]

13. By using Laplace transform, solve the initial value problem:

$y'' + 2y = r(t)$ ,  $y(0) = y'(0) = 0$

Where  $r(t) = 1$ ,  $0 < t < 1$

= 0, otherwise

[5]

14. Graphically maximize  $Z = 5x_1 + 3x_2$  Subject to constraints

$x_1 + 2x_2 \leq 50$

$2x_1 + x_2 \leq 40$ .

$x_1, x_2 \geq 0$

[5]

15. Solve the following Linear Programming Problem by simple method:

Maximize :  $Z = 4x + 3y$

Subject to :  $2x + 3y \leq 6$

$-x + 2y \leq 3$

$2y \leq 5$

$2x + y \leq 4$

$x, y \geq 0$ .

[10]

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Exam.	Back		
Level	BE	Full Marks	80
Programme	ALL (Except B. Arch)	Pass Marks	32
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**Subject:** - Engineering Mathematics III (SH501)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
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- ✓ Assume suitable data if necessary.

1. Use properties of determinant to show [5]
- $$\begin{vmatrix} x^2 & x^2 - (y-z)^2 & yz \\ y^2 & y^2 - (z-x)^2 & zx \\ z^2 & z^2 - (x-y)^2 & xy \end{vmatrix} = (x-y)(y-z)(z-x)(x+y+z)(x^2 + y^2 + z^2)$$
2. Prove that every square matrix can be uniquely expressed as the sum of symmetric and a skew symmetric matrix. [5]
3. Define eigen values and eigen vectors in terms of linear transformation with matrices as operator. Find eigen values of the matrix. [2+3]
- $$\begin{pmatrix} -2 & 2 & -3 \\ 2 & 1 & -6 \\ -1 & -2 & 0 \end{pmatrix}$$
4. Test the consistency of the system  $x+y+z=3$ ,  $x+2y+3z=4$ ,  $2x+3y+4z=7$  by using rank of matrix method and solve if consistent. [5]
5. If  $\vec{F}$  is the gradient of some scalar point functions  $\phi$  i.e.  $\vec{F} = \nabla\phi$ , prove that the line integral is independent of the path joining any two points in the region and conversely. [5]
6. Evaluate  $\iint_S \vec{F} \cdot \vec{n} \, ds$ , where  $\vec{F} = xy\vec{i} - x^2\vec{j} + (x+z)\vec{k}$  and  $S$  is the region of the plane  $2x+2y+z=6$  bounded in the first quadrant. [5]
7. State and prove Green's theorem in plane. [5]
8. Apply Gauss' divergence theorem to evaluate  $\iint_S [(x^3 - yz)\vec{i} - 2x^2y\vec{j} + 2\vec{k}] \cdot \vec{n} \, ds$ , where  $S$  is the surface of the cube bounded by the planes  $x=0$ ,  $x=a$ ,  $y=0$ ,  $y=a$ ,  $z=0$ ,  $z=a$ . [5]
9. Expand  $f(x) = x \sin x$  as a Fourier series in  $-\pi \leq x \leq \pi$ . [5]
10. Obtain half range cosine series for  $f(x) = x$  in the interval  $0 \leq x \leq \pi$ . [5]
11. Find the Laplace transform of: [3+2]
- $t^2 \cos at$
  - $\frac{\sin t}{t}$

12. State convolution theorem for inverse Laplace transform and use it to find the inverse Laplace transform of  $\frac{S}{(S^2 + 4)(S^2 + 9)}$  [1+4]

13. Solve the following initial value problem by using Laplace transform: [5]

$$y'' + 2y' - 3y = \sin t, y(0) = y'(0) = 0$$

14. Graphically maximize [5]

$$Z = 7x_1 + 10x_2$$

Subject to constraints,

$$3x_1 + x_2 \leq 9$$

$$x_1 + 2x_2 \leq 8$$

$$x_1, x_2 \geq 0$$

15. Solve the following LPP by simplex method using duality of: [10]

$$\text{Minimize } Z = 20x + 50y$$

Subject to:

$$2x + 5y \geq 12$$

$$3x + 7y \geq 17$$

$$x, y \geq 0$$

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**Examination Control Division**  
**2073 Shrawan**

Exam.	New Back (2066 & Later Batch)		
Level	BE	Full Marks	80
Programme	ALL (Except B. Arch)	Pass Marks	32
Year / Part	II / I	Time	3 hrs.

**Subject:** - Engineering Mathematics II (SH501)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.

1. Use properties of determinants to prove:  $\begin{vmatrix} a^2 & bc & ac + c^2 \\ a^2 + ab & b^2 & ac \\ ab & b^2 + bc & c^2 \end{vmatrix} = 4a^2b^2c^2$  [5]

2. Prove that the necessary and sufficient condition for a square matrix A to posses an inverse is that the matrix A should be non singular. [5]

3. Find the rank of the matrix  $\begin{pmatrix} 1 & 3 & -2 & 1 \\ 1 & 1 & 1 & 1 \\ 2 & 0 & -3 & 2 \\ 3 & 3 & -3 & 3 \end{pmatrix}$  [5]

by reducing it into normal form.

4. Find the eigenvalues and eigenvectors of the matrix  $\begin{pmatrix} 2 & 1 & 1 \\ 1 & 2 & 1 \\ 0 & 0 & 1 \end{pmatrix}$  [4+1]

Give an example showing importance of eigenvectors.

5. Show that  $\vec{F} = (2x + z^2) \vec{i} + Z \vec{j} + (y + 2xz) \vec{k}$  is irrotational and find its scalar potential. [5]

6. State and prove Green's Theorem in plane. [5]

7. Evaluate  $\iint_S \vec{F} \cdot \vec{n} \, ds$ , where  $\vec{F} = yz \vec{i} + zx \vec{j} + xy \vec{k}$  and S is the surface of the sphere  $x^2 + y^2 + z^2 = 1$  in the first octant. [5]

8. Evaluate  $\int_C xy \, dx + xy^2 \, dy$  by applying stokes theorem where C is the square in xy-plane with vertices (1,0), (-1,0), (0,1), (0,-1) [5]

9. Find the Laplace transform of : [2+3]

i)  $te^{2t} \sin 3t$   
ii)  $\frac{e^{-t} \sin t}{t}$

10. Find the inverse Laplace transform of : [2+3]

i)  $\frac{s+2}{s^2 - 4s + 13}$

ii)  $\log\left(\frac{s+a}{s-a}\right)$

11. Solve the following initial value problem using Laplace transform: [5]

$$x'' + 4x' + 4x = 6e^{-t}, \quad x(0) = -2, \quad x'(0) = -8$$

12. Find the Fourier series representation of  $f(x) = |x|$  in  $[-\pi, \pi]$  [5]

13. Obtain the half range Fourier Sine Series for the function  $f(x) = x^2$  in the interval  $(0, 3)$ . [5]

14. Apply Graphical method to maximize, [5]

$$Z = 5x_1 + 3x_2$$

Subject to the constraints:

$$x_1 + 2x_2 \leq 50$$

$$2x_1 + x_2 \leq 40$$

$$x_1 \geq 0, x_2 \geq 0$$

15. Solve the following Linear Programming Problem by Simplex method: [10]

Maximize:  $Z = 15x_1 + 10x_2$

Subject to:  $x_1 + 3x_2 \leq 10$

$$2x_1 + x_2 \leq 10$$

$$x_1 \geq 0, x_2 \geq 0$$

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Exam.		Regular	
Level	BE	Full Marks	80
Programme	All (Except B. Arch)	Pass Marks	32
Year / Part	II / I	Time	3 hrs.

**Subject:** - Engineering Mathematics III (SH501)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
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- ✓ Assume suitable data if necessary.

1. Use properties of determinants to prove:

[5]

$$\begin{vmatrix} a^2 + 1 & ba & ca & da \\ ab & b^2 + 1 & cb & db \\ ac & bc & c^2 + 1 & dc \\ ad & bd & cd & d^2 + 1 \end{vmatrix} = 1 + a^2 + b^2 + c^2 + d^2$$

2. Show that every square matrix can be uniquely expressed as the sum of symmetric and Skew-Symmetric matrices.

[5]

3. Test the consistency of the system  $x+y+z=3$ ,  $x+2y+3z=4$  and  $2x+3y+4z=7$  and solve completely if found consistent.

[5]

4. State Cayley-Hamilton theorem and verify it for the matrix;  $A = \begin{pmatrix} -2 & 2 & -3 \\ 2 & 1 & -6 \\ -1 & -2 & 0 \end{pmatrix}$

[1+4]

5. Prove that " The line integral  $\int_C \vec{F} \cdot d\vec{r}$  of a continuous function  $\vec{F}$  defined in a region R is independent of path C joining any two points in R if and only if there exists a single valued scalar function  $\phi$  having first order partial derivatives such that  $\vec{F} = \nabla\phi$ ".

[5]

6. State Green's theorem and use it to find the area of astroid  $x^{2/3} + y^{2/3} = a^{2/3}$ .

[5]

7. Evaluate  $\iint_S \vec{F} \cdot \vec{n} ds$ , where  $\vec{F} = x^2 \vec{i} + y^2 \vec{j} + z^2 \vec{k}$  and 's' is the surface of the plane  $x + y + z = 1$  between the co-ordinate planes.

[5]

8. Apply Gauss' divergence theorem to evaluate  $\iint_S \vec{F} \cdot \vec{n} ds$  where

$\vec{F} = (x^3 - yz) \vec{i} - 2x^2y \vec{j} + 2z \vec{k}$  and 's' is the surface the cube bounded by the planes  $x = 0, x = a, y = 0, y = a, z = 0, z = a$ .

[5]

9. Find the Laplace transform of:

[2+3]

i)  $t \sin^2 3t$

ii)  $\frac{\sin 2t}{t}$

10. Find the inverse Laplace transform of:

[2+3]

i)  $\frac{1}{s^2 - 3s + 2}$

ii)  $\frac{1}{s(s+1)^3}$

11. Apply Laplace transform to solve the differential equation:

[5]

$$y'' + 2y' + 5y = e^{-t} \sin t, \quad x(0) = 0, x'(0) = 1$$

12. Find a Fourier series to represent  $f(x) = x - x^2$  from  $x = -\pi$  to  $x = \pi$ . Hence show that

$$\frac{1}{1^2} - \frac{1}{2^2} + \frac{1}{3^2} - \frac{1}{4^2} + \dots = \frac{\pi^2}{12}$$

[5]

13. Develop  $f(x) = \sin\left(\frac{\pi x}{l}\right)$  in half range Cosine Series in the range  $0 < x < l$ .

[5]

14. Graphically maximize,

[5]

$$Z = 7x_1 + 10x_2$$

Subject to constraints,

$$3x_1 + x_2 \leq 9$$

$$x_1 + 2x_2 \leq 8$$

$$x_1 \geq 0, x_2 \geq 0$$

15. Solve the following LPP using simplex method.

[10]

$$\text{Maximize: } P = 50x_1 + 80x_2$$

$$\text{Subject to: } x_1 + 2x_2 \leq 32$$

$$3x_1 + 4x_2 \leq 84$$

$$x_1 \geq 0, x_2 \geq 0$$

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01 TRIBHUVAN UNIVERSITY  
 INSTITUTE OF ENGINEERING  
**Examination Control Division**  
 2071 Chaitra

Exam.	Regular		
Level	BE	Full Marks	80
Programme	All (Except B.Arch.)	Pass Marks	32
Year / Part	II / I	Time	3 hrs.

**Subject:** - Engineering Mathematics III (SH501)

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1. Using the properties, evaluate the determinant:

[5]

$$\begin{vmatrix} 1 & a & a^2 & a^3 + bcd \\ 1 & b & b^2 & b^3 + cda \\ 1 & c & c^2 & c^3 + abd \\ 1 & d & d^2 & d^3 + abc \end{vmatrix}$$

2. Prove that every square matrix can uniquely be expressed as the sum of a symmetric and a skew symmetric matrix.

[5]

3. Test the consistency of the system:

[5]

$$x - 6y - z = 10, \quad 2x - 2y + 3z = 10, \quad 3x - 8y + 2z = 20$$

And solve completely, if found consistent.

4. Find the eigen values and eigenvectors of the matrix  $\begin{pmatrix} 2 & 2 & 1 \\ 1 & 3 & 1 \\ 1 & 2 & 2 \end{pmatrix}$ .

[5]

5. Using the line integral, compute the workdone by the force

[5]

$$\vec{F} = (2x - y + 2z) \vec{i} + (x + y - z) \vec{j} + (3x - 2y - 5z) \vec{k}$$

when it moves once around a circle  $x^2 + y^2 = 4; z = 0$

6. State and prove Green's Theorem in plane.

[5]

7. Verify Stoke's theorem for  $\vec{F} = (x^2 + y^2) \vec{i} - 2xy \vec{j}$  taken around the rectangle bounded by the lines  $x = \pm a, y = 0, y = b$ .

[5]

8. Evaluate  $\iint_S \vec{F} \cdot \vec{n} \, ds$  where  $\vec{F} = (2xy + z) \vec{i} + y^2 \vec{j} - (x + 3y) \vec{k}$  by Gauss divergence theorem; where S is surface of the plane  $2x + 2y + z = 6$  in the first octant bounding the volume V.

[5]

9. Find the Laplace transform of the following:

[2.5×2]

a)  $te^{-2t} \cos t$

b)  $\sin ht \cos t$

10. Find the inverse Laplace transform of :

[2.5×2]

a)  $\frac{1}{S(S+1)}$

b)  $\frac{S^2}{(S^2 + b^2)^2}$

11. Solve the differential equation  $y''+2y'+5y=e^{-t} \sin t$ ,  $y(0)=0$ ,  $y'(0)=1$ , by using Laplace transform.

[5]

12. Expand the function  $f(x)=x \sin x$  as a Fourier series in the interval  $-\pi \leq x \leq \pi$ .

[5]

13. Obtain half range sine series for the function  $f(x)=x-x^2$  for  $0 < x < 1$ .

[5]

14. Graphically maximize and minimize

[5]

$z = 9x + 40y$  subjected to the constraints

$y - x \geq 1$ ,  $y - x \leq 3$ ,  $2 \leq x \leq 5$

15. Solve the following Linear Programming Problem by Simplex method:

[10]

Maximize,  $P = 20x_2 - 5x_1$

Subjected to,  $10x_2 - 2x_1 \leq 5$

$2x_1 + 5x_2 \leq 10$  and  $x_1, x_2 \geq 0$

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01 TRIBHUVAN UNIVERSITY  
 INSTITUTE OF ENGINEERING  
**Examination Control Division**  
 2070 Chaitra

Exam.	Regular		
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Programme	All (Except B.Arch)	Pass Marks	32
Year / Part	II / I	Time	3 hrs.

**Subject:** - Mathematics III (SH501)

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1. Using the properties of determinant prove

$$\begin{vmatrix} (b+c)^2 & a^2 & a^2 \\ b^2 & (c+a)^2 & b^2 \\ c^2 & c^2 & (a+b)^2 \end{vmatrix} = 2abc(a+b+c)^3$$

2. Prove that  $(AB)^T = B^T A^T$  where A is the matrix of size  $m \times p$  and B is the matrix of size  $p \times n$

[5]

3. Find the rank of the following matrix by reducing normal form.

$$\begin{bmatrix} 1 & 3 & -2 & 1 \\ 1 & 1 & 1 & 1 \\ 2 & 0 & -3 & 2 \\ 3 & 3 & -3 & 3 \end{bmatrix}$$

[5]

4. Find the eigen values and eigen vectors of the following matrix.

$$\begin{bmatrix} 2 & 0 & 1 \\ 0 & 2 & -1 \\ 0 & 0 & 2 \end{bmatrix}$$

[5]

5. Prove that the line integral  $\int_A^B \vec{F} \cdot d\vec{r}$  is independent of the path joining any two points A and B in a region if  $\int_C \vec{F} \cdot d\vec{r} = 0$  for any simple closed curve C in the region.

[5]

6. Evaluate  $\iint_S \vec{F} \cdot \hat{n} ds$  where  $\vec{F} = x^2 \vec{i} + y^2 \vec{j} + z^2 \vec{k}$  and S is the finite plane  $x + y + z = 1$  between the coordinate planes.

[5]

**OR**

Evaluate  $\iint_S \vec{F} \cdot \hat{n} ds$  for  $\vec{F} = yz \vec{i} + zx \vec{j} + xy \vec{k}$  where S is the surface of sphere  $x^2 + y^2 + z^2 = 1$  in the first octant.

7. Evaluate,  $\iint_S \vec{F} \cdot \hat{n} ds$  for  $\vec{F} = x \vec{i} - y \vec{j} + (z^2 - 1) \vec{k}$  where S is the surface bounded by the cylinder  $x^2 + y^2 = 4$  and the planes  $z = 0$  and  $z = 1$

[5]

8. Verify the stoke's theorem for  $\vec{F} = (2x - y) \vec{i} - yz^2 \vec{j} - y^2 z \vec{k}$  where S is the upper part of the sphere  $x^2 + y^2 + z^2 = a^2$  C is its boundary. [5]
9. Find the Laplace transform of (a)  $t^2 \sin zt$  and (b)  $\frac{1-e^t}{t}$  [2.5×2]
10. Find the inverse Laplace transform of (a)  $\frac{2s+3}{s^2+5s-6}$  (b)  $\frac{s^3}{s^4-a^4}$  [2.5×2]
11. Solve the following differential equation by using Laplace transform [5]  
 $y'' + y' - 2y = x, y(0) = 1, y'(0) = 0$
12. Obtain the Fourier series for  $f(x) = x^2$  in the interval  $-\pi < x < \pi$  and hence prove that
- $$\sum \frac{1}{x^2} = \frac{1}{1^2} + \frac{1}{2^2} + \frac{1}{3^2} \dots = \frac{\pi^2}{6} \quad [5]$$
13. Obtain half range sine series for  $f(x) = \pi x - x^2$  in  $(0, \pi)$  [5]
14. Graphically minimize  $z = 4x_1 + 3x_2 + x_3$  [5]
- Subject to  $x_1 + 2x_2 + 4x_3 \geq 12$   
 $3x_1 + 2x_2 + x_3 \geq 8$  and  $x_1, x_2, x_3 \geq 0$
15. Minimize  $z = 8x_1 + 9x_2$  [10]
- Subject to  $x_1 + 3x_2 \geq 4$   
 $2x_1 + x_2 \geq 5$  with  $x_1, x_2 \geq 0$

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62. TRIBHUVAN UNIVERSITY  
INSTITUTE OF ENGINEERING  
**Examination Control Division.**  
2069 Ashad

Exam.	New Back (2066 & Later Batch)		
Level	BE	Full Marks	80
Programme	All (Except B. Arch.)	Pass Marks	32
Year / Part	II / I	Time	3 hrs.

**Subject:** - Engineering Mathematics III (SH 501)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.

1. Find the value of the determinant: [5]

$$\begin{vmatrix} 1 & a & a^2 & a^3 + bcd \\ 1 & b & b^2 & b^3 + cda \\ 1 & c & c^2 & c^3 + dab \\ 1 & d & d^2 & d^3 + abc \end{vmatrix}$$

2. Prove that every square matrix can be uniquely expressed as the sum of a symmetric and a skew-symmetric matrices. [5]

3. Find the rank of matrix:  $\begin{bmatrix} 1 & 3 & -2 & 1 \\ 1 & 1 & 1 & 1 \\ 2 & 0 & -3 & 2 \\ 3 & 3 & -3 & 3 \end{bmatrix}$  reducing to echelon form. [5]

4. Verify Cayley-Flamilton theorem for the matrix:  $\begin{bmatrix} 1 & 3 & 7 \\ 4 & 2 & 3 \\ 1 & 2 & 1 \end{bmatrix}$ . [5]

5. Find the Laplace transforms of: (a)  $te^{-t}\sin t$  (b)  $\frac{e^{at} - \cos bt}{t}$  [5]
6. If  $L[f(t)] = F(s)$ , then prove that  $L[f'(t)] = SF(s) - f(0)$ . [5]
7. Use Laplace transform to solve:  $x'' + 2x' + 5x = e^{-t} \sin t$  given  $x(0) = 0$ ;  $x'(0) = 1$ . [5]
8. Obtain the Fourier series for  $f(x) = x^3$  in the interval  $-\pi \leq x \leq \pi$ . [5]
9. Obtain half-range sine series for  $e^x$  in  $(0, 1)$ . [5]
10. Maximize  $z = 2x_1 + 3x_2$  subject to constraints  $x_1 - x_2 \leq 2$ ,  $x_1 + x_2 \geq 4$  and  $x_1, x_2 \geq 0$  graphically. [5]
11. Solve the linear programming problems by simplex method constructing the duality [10]

Minimize  $Z = 3x_1 + 2x_2$

Subject to  $2x_1 + 4x_2 \geq 10$

$4x_1 + 2x_2 \geq 10$

$x_2 \geq 4$  and  $x_1, x_2 \geq 0$

12. Prove that  $\vec{F} = (2xz^3 + 6y)\vec{i} + (6x - 2yz)\vec{j} + (3x^2z^2 - y^2)\vec{k}$  is conservative vector field and find its scalar potential function. [5]

13. Evaluate  $\iint_S \vec{F} \cdot \hat{n} ds$  where  $\vec{F} = x^2\vec{i} + y^2\vec{j} + z^2\vec{k}$  and S is the finite plane  $x+y+z=1$  between the co-ordinate planes. [5]

14. Using Green's theorem, find the area of the hypocycloid  $\frac{x^{2/3}}{a^{2/3}} + \frac{y^{2/3}}{b^{2/3}} = 1$ . [5]

15. Evaluate  $\iint_S \vec{F} \cdot \hat{n} ds$  where  $\vec{F} = 2x\vec{i} + 3y\vec{j} + 4z\vec{k}$  and S is the surface of sphere  $x^2+y^2+z^2=1$  by Gauss divergence theorem. [5]

*OR*

Verify Stoke's theorem for  $\vec{F} = 2y\vec{i} + 3x\vec{j} - z^2\vec{k}$  where S is the upper half of the sphere  $x^2+y^2+z^2=9$  and 'C' is its boundary. [5]

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Exam.	Regular		
Level	BE	Full Marks	80
Programme	All (Except B.Arch)	Pass Marks	32
Year / Part	II / I	Time	3 hrs.

**Subject:** - Engineering Mathematics III (SH501)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.

1. Find the value of the determinant  $\begin{vmatrix} a^2 & a^2 - (b-c)^2 & bc \\ b^2 & b^2 - (c-a)^2 & ca \\ c^2 & c^2 - (a-b)^2 & ab \end{vmatrix}$  [5]
2. Show that the matrix  $B^T AB$  is Hermitian or skew-Hermitian according as A is Hermitian and skew- Hermitian. [5]
3. Find the rank of the matrix  $\begin{bmatrix} 6 & 1 & 3 & 8 \\ 4 & 2 & 6 & -1 \\ 10 & 3 & 9 & 7 \\ 16 & 4 & 12 & 15 \end{bmatrix}$  reducing this into the triangular form. [5]
4. Obtain the characteristic equation of the matrix  $A = \begin{bmatrix} 1 & 0 & 2 \\ 0 & 2 & 1 \\ 2 & 0 & 3 \end{bmatrix}$  and verify that it is satisfied by A. [5]
5. Evaluate  $\int_C \vec{F} \cdot d\vec{r}$ , where  $\vec{F} = (x-y) \vec{i} + (x+y) \vec{j}$  along the closed curve C bounded by  $y^2 = x$  and  $x^2 = y$  [5]
6. Find the value of the normal surface integral  $\iint_S \vec{F} \cdot \vec{n} ds$  for  $\vec{F} = x \vec{i} - y \vec{j} + (z^2 - 1) \vec{k}$ , where S is the surface bounded by the cylinder  $x^2 + y^2 = 4$  between the planes  $Z = 0$  and  $Z = 1$ . [5]
7. Using Green's theorem, find the area of the astroid  $x^{\frac{2}{3}} + y^{\frac{2}{3}} = a^{\frac{2}{3}}$  [5]
8. Verify stoke's theorem for  $\vec{F} = 2y \vec{i} + 3x \vec{j} - z^2 \vec{k}$  where S is the upper half of the sphere  $x^2 + y^2 + z^2 = 9$  and C is its boundary. [5]

**OR**

Evaluate the volume intergral  $\iiint_V \vec{F} dv$ , where V is the region bounded by the surface  $x = 0, y = 0, y = 6, z = x^2, z = 4$  and  $\vec{F} = 2xz \vec{i} - x \vec{j} + y^2 \vec{k}$

9. Find the Laplace transforms of the following functions [2.5×2]
  - $t e^{-4t} \sin 3t$
  - $\frac{\cos at - \cos bt}{t}$

10. State and prove the second shifting theorem of the Laplace transform. [5]

11. Solve the following differential equation using Laplace transform. [5]

$$\frac{d^2y}{dx^2} + \frac{dy}{dx} - 2y = x \text{ given } y(0) = 1, y'(0) = 0$$

12. Obtain the Fourier series for  $f(x) = x^2$  in the interval  $-\pi < x < \pi$  and hence show that

$$\sum \frac{1}{n^2} = \frac{1}{1^2} + \frac{1}{2^2} + \frac{1}{3^2} + \dots = \frac{\pi^2}{6} \quad [5]$$

13. Express  $f(x) = x$  as a half-range sine series in  $0 < x < 2$  [5]

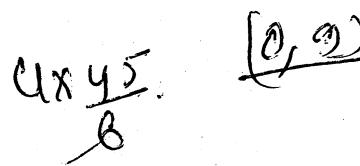
14. Maximize  $Z = 4x_1 + 5x_2$  subject to constraints [5]

$$2x_1 + 5x_2 \leq 25$$

$$6x_1 + 5x_2 \leq 45$$

$$x_1 \geq 0 \text{ and } x_2 \geq 0$$

graphically



15. Solve the following linear programming problem using the simplex method. [10]

$$\text{Maximize } P = 50x_1 + 80x_2$$

$$\text{Subject to } x_1 + 2x_2 \leq 32$$

$$3x_1 + 4x_2 \leq 84$$

$$x_1, x_2 \geq 0$$

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02 TRIBHUVAN UNIVERSITY  
INSTITUTE OF ENGINEERING  
Examination Control Division

2068 Chaitra

Exam.	Regular		
Level	BE	Full Marks	80
Programme	BCE, BEL, BEX, BCT, BME, BIE, B. AGRI.	Pass Marks	32
Year / Part	II / I	Time	3 hrs.

**Subject:** - Engineering Mathematics III (SH 501)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.

1. Prove that:  $\begin{vmatrix} a & b & c^2 \\ b & c & a \\ c & a & b \end{vmatrix} = \begin{vmatrix} 2bc - a^2 & c^2 & b^2 \\ c^2 & 2ac - b^2 & a^2 \\ b^2 & a^2 & 2ab - c^2 \end{vmatrix} = (a^3 + b^3 + c^3 - 3abc)^2$ . [5]
2. Define Hermitian and Skew Hermitian matrix. Show that every square matrix can be uniquely expressed as the sum of a Hermitian and a skew Hermitian. [5]
3. For what value of  $\lambda$  the equation  $x + y + z = 1$ ,  $x + 4y + 10z = \lambda^2$  and  $x + 2y + 4z = \lambda$  have a solution? Solve them completely in each case. [5]
4. Find the eigen values and eigen vectors of  $A = \begin{vmatrix} 3 & -4 & 4 \\ 1 & -2 & 4 \\ 1 & -1 & 3 \end{vmatrix}$ . [5]
5. Evaluate  $\int_C \vec{F} \cdot d\vec{r}$ , Where  $C: x^2 = y$  and  $y^2 = x$  and  $\vec{F} = (x-y) \vec{i} + (x+y) \vec{j}$ . [5]
6. State and prove Green theorem in a plane. [5]
7. Verify Gauss divergence theorem for  $\vec{F} = x^2 \vec{i} + 3 \vec{j} + yz \vec{k}$ . Taken over the cube bounded by  $x = 0, x = 1, y = 0, y = 1, z = 0, z = 1$ . [5]
8. Find the Laplace transform of the given function (i)  $t^2 \sin t$  (ii)  $\cos at \sin bt$ . [5]
9. Evaluate  $\iint_s \vec{F} \cdot d\vec{s}$  where  $\vec{F} = 3 \vec{i} + x \vec{j} - yz \vec{k}$  and  $s$  is the surface of the cylinder  $x^2 + y^2 = 9$  included in the first octant between the plane  $z = 0, z = 4$ . [5]
10. Find the inverse Laplace transform: (a)  $\frac{1}{(S-2)(S+4)}$  (b)  $\log\left(\frac{s^2 + a^2}{s^2}\right)$  [5]
11. Solve the equation using Laplace transform  $y'' + 4y' + 3y = t$ ,  $t > 0$   $y(0) = 0$ ,  $y'(0) = 1$ . [5]

12. Obtain a Fourier series to represent the function  $f(x) = |x|$  for  $-\pi \leq x \leq \pi$  and hence.

$$\text{deduce } \frac{\pi^2}{8} = \frac{1}{1^2} + \frac{1}{3^2} + \frac{1}{5^2} + \dots \quad [5]$$

13. Obtain the half Range Sine Series  $f(x) = ex$  in  $0 < x < 1$ . [5]

*OR*

Obtain the Fourier series for  $f(x) = x - x^2$  where  $-1 < x < 1$  as a Fourier series of period 2.

14. Solve the following by using the simplex method: [7.5]

Maximize  $P = 15x_1 + 10x_2$ ,

Subject to

$$2x_1 + x_2 \leq 10,$$

$$x_1 + 3x_2 \leq 10,$$

$$x_1, x_2 \geq 0.$$

15. Solve by using the dual method: [7.5]

Minimize  $C = 21x_1 + 50x_2$ ,

Subject to  $2x_1 + 5x_2 \leq 12$ ,

$$3x_1 + 7x_2 \leq 17,$$

$$x_1, x_2 \geq 0.$$

*OR*

Solve the following LPP by using the big M-method:

Maximize  $P = 2x_1 + x_2$ ,

Subject to

$$x_1 + x_2 \leq 10,$$

$$-x_1 + x_2 \geq 2,$$

$$x_1, x_2 \geq 0.$$

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02 TRIBHUVAN UNIVERSITY  
 INSTITUTE OF ENGINEERING  
**Examination Control Division**  
 2068 Baishakh

Exam.	Regular / Back.		
Level	BE	Full Marks	80
Programme	All (Except B.Arch.)	Pass Marks	32
Year / Part	II / I	Time	3 hrs.

**Subject:** - Engineering Mathematics III

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.

1. Using the properties of determinant prove that:

[5]

$$\begin{vmatrix} x & 1 & y & 1 \\ 1 & y & 1 & x \\ 1 & x & 1 & y \\ y & 1 & x & 1 \end{vmatrix} = (x+y+2)(x-y)^2(x+y-2)$$

2. If A and B are two non singular matrices of the same order, prove that  $(AB)^{-1} = B^{-1} \cdot A^{-1}$ .

[5]

3. Find the rank of the following matrix reducing to normal form

$$\begin{bmatrix} 1 & 2 & 1 & 2 \\ 1 & 3 & 2 & 2 \\ 2 & 4 & 3 & 4 \\ 3 & 7 & 4 & 6 \end{bmatrix}$$

[5]

4. Find the eigen values and eigen vectors of the matrix  $\begin{bmatrix} 2 & -2 & 2 \\ 1 & 1 & 1 \\ 1 & 3 & -1 \end{bmatrix}$ .

[5]

5. Find the Laplace transform of the following functions:

[5]

a)  $te^{-3t} \cos 2t$       b)  $\frac{e^{at} - \cos 6t}{t}$

6. Find the inverse Laplace transform of the following functions:

[5]

a)  $\frac{1}{(s-2)(s+2)^2}$       b)  $\frac{1}{s^2(s+2)}$

7. Solve using Laplace transform  $(D^2 + 4D + 3)x = e^{-t}$ , where  $x(0) = x'(0) = 1$ .

[5]

8. Obtain a Fourier series for  $f(x) = x^3$  in the interval  $-\pi \leq x \leq \pi$ .

[5]

9. Find the half range sine series for the function  $f(x) = x - x^2$  in the interval  $0 < x < 1$ .

[5]

10. Maximize  $Z = x_1 + 1.5 x_2$  subject to constraints

[5]

$2x_1 + 2x_2 \leq 160$

$x_1 + 2x_2 \leq 120$

$4x_1 + 2x_2 \leq 280$

$x_1 \geq 0$  and  $x_2 \geq 0$  graphically.

11. Solve the following linear programming problems by simplex method [10]

Maximize  $Z = 15x_1 + 10x_2$

Subject to  $2x_1 + 2x_2 \leq 10$

$x_1 + 3x_2 \leq 10$  and  $x_1, x_2 \geq 0$

12. Show that the vector field  $\vec{F} = (x^2 - yz)\hat{i} + (y^2 - zx)\hat{j} + (z^2 - xy)\hat{k}$  is irrotational. Find the scalar function  $\phi(x, y, z)$  such that  $\vec{F} = \nabla\phi$ . [5]

13. If S be the part of the surface  $Z = 9 - x^2 - y^2$  with  $Z \geq 0$  and  $\vec{F} = 3x\hat{i} + 3y\hat{j} + Z\hat{k}$ , find the flux of F through S. [5]

14. State and prove that Green's theorem in the plane. [5]

15. Evaluate by Stoke's theorem: [5]

$$\int_C (e^x dx + 2y dy - dz)$$

Where C is the curve:  $x^2 + y^2 = 4$ ,  $z = 2$ .

*OR*

Verify Gauss divergence theorem for the vector function  $\vec{F} = x^2\hat{i} + z\hat{j} + yz\hat{k}$ , taken over the unit cube bounded by the planes:  $x = 0, x = 1, y = 0, y = 1, z = 0, z = 1$ .

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05 TRIBHUVAN UNIVERSITY  
 INSTITUTE OF ENGINEERING  
**Examination Control Division**  
 2067 Ashadh

Exam.	Regular/Back		
Level	BE	Full Marks	80
Programme	All (Except B.Arch.)	Pass Marks	32
Year / Part	II / I	Time	3 hrs.

**Subject:** - Mathematics III

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ All questions carry equal marks.
- ✓ Assume suitable data if necessary.

1. Using the properties of determinant prove:

$$\begin{vmatrix} a^2 + 1 & ba & ca & da \\ ab & b^2 + 1 & cb & db \\ ac & bc & c^2 + 1 & dc \\ ad & bd & cd & d^2 + 1 \end{vmatrix} = a^2 + b^2 + c^2 + d^2 + 1$$

2. Show that every square matrix can be uniquely expressed as the sum of hermitian and a skew-hermitian matrix.

3. Reduce to normal form and find the rank of the matrix:

$$\begin{bmatrix} 2 & -2 & 0 & 6 \\ 4 & 2 & 0 & 2 \\ 1 & -1 & 0 & 3 \\ 1 & -2 & 1 & 2 \end{bmatrix}$$

4. Find the eigen values and eigenvectors of the matrix

$$\begin{bmatrix} 2 & 2 & 1 \\ 1 & 3 & 1 \\ 1 & 2 & 2 \end{bmatrix}$$

5. Find the Laplace transform of:

a)  $\cosh at \sin at$

b)  $\frac{\cos 2t - \cos 3t}{t}$

6. Find the inverse Laplace transform of:

a)  $\frac{1}{s^2(s^2 + a^2)}$

b)  $\log \frac{s+1}{s-1}$

7. State and prove the integral theorem of the Laplace transform.

8. Solve the following differential equation using the Laplace transform.

$y''' + 2y'' - y' - 2y = 0$  where  $y(0) = y'(0) = 0$  and  $y''(0) = 6$

9. Find a Fourier series to represent  $x - x^2$  for  $-\pi < x < \pi$ . Hence show that

$$\frac{\pi^2}{12} = \frac{1}{1^2} - \frac{1}{2^2} + \frac{1}{3^2} - \frac{1}{4^2} + \dots$$

10. Express  $f(x) = x$  as a cosine half range series in  $0 < x < 2$ .

11. The acceleration of a moving particle at any time  $t$  is given by

$\frac{d^2 \vec{r}}{dt^2} = 12 \cos 2t \hat{i} - 8 \sin 2t \hat{j} + 16t \hat{k}$ . Find the velocity  $\vec{v}$  and displacement  $\vec{r}$  at anytime  $t$  if

$$t = 0, \vec{v} = 0 \text{ and } \vec{r} = 0.$$

12. Find the angle between the normals to the surface  $xy = z^2$  at the points  $(1,4,2)$  and  $(-3,-3,3)$

13. Find the work done in moving a particle once round the circle  $x^2 + y^2 = 9, z = 0$  under the force field  $\vec{F}$  given by  $\vec{F} = (2x - y + z) \hat{i} + (x + y - z^2) \hat{j} + (3x - 2y + 4z) \hat{k}$ .

14. Evaluate  $\iint_S \vec{F} \cdot \vec{n} ds$  where  $s$  is the upper side of triangle with vertices  $(1,0,0), (0,1,0), (0,0,1)$  where  $\vec{F} = (x - 2z) \hat{i} + (x + 3y + z) \hat{j} + (5x + y) \hat{k}$ .

15. State Green's theorem in a plane. Using Green's theorem find the area of  $x^{2/3} + y^{2/3} = a^{2/3}$ .

16. Verify Stoke's theorem for  $\vec{F} = (2x - y) \hat{i} - yz^2 \hat{j} - y^2 z \hat{k}$  where  $s$  is the upper part of the sphere  $x^2 + y^2 + z^2 = a^2$  and  $c$  is its boundary.

**OR**

Verify Gauss theorem for  $\vec{F} = y \hat{i} + x \hat{j} + z^2 \hat{k}$  over the region bounded by  $x^2 + y^2 = a^2, z = 0$  and  $z = h$ .

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04 TRIBHUVAN UNIVERSITY  
 INSTITUTE OF ENGINEERING  
**Examination Control Division**  
 2067 Magh

Exam.	Back		
Level	BE	Full Marks	80
Programme	All (Except B.Arch.)	Pass Marks	32
Year / Part	II / I	Time	3 hrs.

**Subject:** - Mathematics III

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ All questions carry equal marks.
- ✓ Assume suitable data if necessary.

1. Show that  $\begin{vmatrix} a & b & b & b \\ a & b & a & a \\ a & a & b & a \\ b & b & b & a \end{vmatrix} = -(b-a)^4$ .

2. If P and Q are two orthogonal matrices of the same order, prove that their product is also orthogonal.

3. Reducing to normal form, find the rank of matrix  $\begin{vmatrix} 1 & -1 & 2 & -3 \\ 4 & 1 & 0 & 2 \\ 0 & 3 & 0 & 4 \\ 0 & 1 & 0 & 2 \end{vmatrix}$ .

4. Find the eigen values and eigen vectors of the matrix  $\begin{vmatrix} 2 & -2 & 2 \\ 1 & 1 & 1 \\ 1 & 3 & -1 \end{vmatrix}$ .

5. Find a Fourier series for  $f(x) = x^3$ ,  $-\pi < x < \pi$ .
6. Find the half range sine series for the function  $f(x) = e^x$  for  $0 < x < \pi$ .

7. Find the Laplace transform of

a)  $t^2 \cos at$   
 b)  $t^3 e^{-3t}$

8. Find the Inverse Laplace transform of

a)  $\frac{s}{(s-3)(s^2+4)}$

b)  $\log \frac{s(s+1)}{(s^2+4)}$

9. If  $L\{f(t)\} = F(s)$ , then prove  $L\{e^{at} f(t)\} = F(s-a)$ .

10. Use the Laplace transform to solve  $\frac{d^2y}{dt^2} + 4\frac{dy}{dt} + 3y = e^{-t}$ ,  $y(0) = y'(0) = 1$ .

11. The position vector of a moving particle at any time  $t$  is given by  $\vec{r} = (t^2 + 1)\vec{i} + (4t - 3)\vec{j} + (2t^2 - 6)\vec{k}$ . Find the velocity and acceleration at  $t = 1$ . Also find their magnitudes.

12. Define divergence and curl of  $\vec{V}$ . Prove that  $\text{div}(\text{curl } \vec{V}) = 0$ .

13. Evaluate  $\int_C \vec{F} \cdot d\vec{r}$  where  $\vec{F} = Z\vec{i} + x\vec{j} + y\vec{k}$  and  $C$  is the arc of curve,  $x = t^2 + 1$ ,  $y = 2t^2$ ,  $z = t^3$  from  $t = 1$  to  $t = 2$ .

14. Evaluate  $\iint_S \vec{F} \cdot \vec{n} ds$  where  $\vec{F} = x\vec{i} + y\vec{j} + z\vec{k}$  and  $S$  is the outside of the lateral surface of circular cylinder,  $x^2 + y^2 = a^2$  between planes  $z = 0$  and  $z = 4$ .

15. Use Green's theorem to find the area of ellipse,  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ .

16. Verify Stoke's theorem for  $\vec{F} = x\vec{i} + z^2\vec{j} + y^2\vec{k}$  over the plane surface  $x + y + z = 1$  lying in first octant.

*OR*

Verify Gauss's theorem for  $\vec{F} = 4x\vec{i} - 2y^2\vec{j} + z^2\vec{k}$  taken over the region bounded by  $x^2 + y^2 = 4$ ,  $z = 0$  and  $z = 3$ .

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