

SET - I

Branch: BTech CSBS
Year/Sem: II/III

Marks: 50

Part - A (10 X 1 = 10 marks)
Answer all the questions

- Which one of the following languages over $\Sigma = \{a, b\}$ is NOT context-free?
 - $\{wwR | w \in \{a, b\}^*\}$
 - $\{wanbnwR | w \in \{a, b\}^*, n \geq 0\}$
 - $\{wanwRbn | w \in \{a, b\}^*, n \geq 0\}$
 - $\{anbi | i \in \{n, 3n, 5n\}, n \geq 0\}$
- Automaton accepting the regular expression of any number of a's is
 - a^*
 - ab^*
 - $(a/b)^*$
 - a^*b^*c
- Consider the following context-free grammar over the alphabet $\Sigma = \{a, b, c\}$ with S as the start symbol: $S \rightarrow abScT | abcTT \rightarrow bT | b$ Which one of the following represents the language generated by the above grammar?
 - $\{(ab)^n(cb)^n | n \geq 1\}$
 - $\{(ab)^n cbm^1 cbm^2\}$
 - $\{cbmn | n, m^1, m^2, mn \geq 1\}$
 - $\{(ab)^n (cbm)^n | m, n \geq 1\}$
- Assume the statements S1 and S2 given as: S1: Given a context free grammar, there exists an algorithm for determining whether $L(G)$ is infinite. S2: There exists an algorithm to determine whether two context free grammars generate the same language. Which of the following is true?
 - S1 is correct and S2 is not correct
 - Both S1 and S2 are correct
 - Both S1 and S2 are not correct
 - S1 is not correct and S2 is correct
- A student wrote two context-free grammars G1 and G2 for generating a single C-like array declaration. The dimension of the array is at least one. For example, `int a[10][3];` The grammars use D as the start symbol, and use six terminal symbols `int ; id [] num.` Grammar G1 Grammar

G2 $D \rightarrow \text{int}L$; $D \rightarrow \text{int}L$; $L \rightarrow \text{id}[E L \rightarrow \text{id}EE \rightarrow \text{num}] E \rightarrow E[\text{num}]E \rightarrow \text{num}][E E \rightarrow [\text{num}]$ Which of the grammars correctly generate the declaration mentioned above?

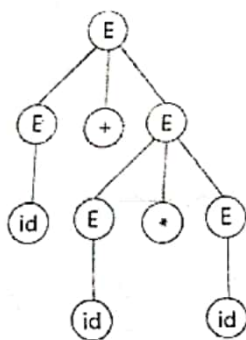
- A. Both G1 and G2
- B. Only G1
- C. Only G2
- D. Neither G1 nor G2

6. For any two languages $L1$ and $L2$ such that $L1$ is context-free and $L2$ is recursively enumerable but not recursive, which of the following is/are necessarily true?

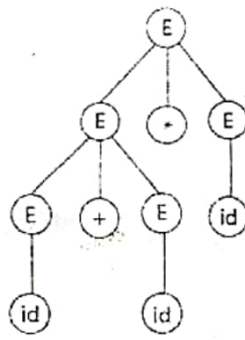
- I. $L1$ (complement of $L1$) is recursive
- II. $L2$ (complement of $L2$) is recursive
- III. $L1$ is context-free
- IV. $L1 \cup L2$ is recursively enumerable *

- A. I
- B. III
- C. III and IV
- D. I and IV

7. Consider $E \rightarrow E + E$ $E \rightarrow E * E$ $E \rightarrow \text{id} *$



Parse tree 1



Parse tree 2

- A. $E \rightarrow E + T, T \rightarrow T * F, F \rightarrow \text{id}$
- B. $E \rightarrow E + T, T \rightarrow F$
- C. $E \rightarrow E + T, E \rightarrow T, T \rightarrow T * F, T \rightarrow F$
- D. $E \rightarrow E + T, E \rightarrow T$

8. Push down automata accepts _____ languages.

- A. Type 3
- B. Type 2
- C. Type 1
- D. Type 0

9. A push down automaton with only symbol allowed on the stack along with fixed symbol.

- A. Embedded PDA
- B. Nested Stack automata
- C. DPDA
- D. Counter Automaton

10. Which of the following option resembles the given PDA?

- A. $\{0^n 1^n | n \geq 0\}$
- B. $\{0^n 1^{2n} | n \geq 0\}$
- C. $\{0^{2n} 1^n | n \geq 0\}$
- D. $\{0^{21^n} | n \geq 0\}$

PART-B (4 X 4 = 16 marks)

- 11. Define CFG.
- 12. Construct a CFG over $\{a, b\}$ generating a language consisting of equal number of a's and b's.
- 13. Eliminate all unit production $S \rightarrow Aa | B; B \rightarrow A | bb; A \rightarrow a | bc | B$.
- 14. Define Push Down Automata.
- 15. Is it true that non-deterministic PDA is more Powerful than that of deterministic PDA? Justify your answer.
- 16. Construct a PDA to accept a language $\{(ab)^n | n \geq 1\}$ by empty stack.

Part - C (2*12 = 24 marks)

17. a. Convert to Chomsky Normal Form $S \rightarrow ASA | aB, A \rightarrow B | S, B \rightarrow b | \epsilon$
OR

17. b. Consider the grammar,
 $S \rightarrow iCtS, S \rightarrow iCtSeS, S \rightarrow a, C \rightarrow b$

- 1) Construct leftmost derivation for the sentence $W = libtibtaea$.
- 2) Show the corresponding Parse tree for the above sentence.
- 3) Is the above grammar ambiguous? If so prove it.

18. a. Design a PDA for $L = \{WCW^R | W \text{ in } (0+1)^*\}$
OR

18. b. Obtain CFG for the PDA as given below

- $\delta(q_0, 0, Z) = (q_0, AZ)$
- $\delta(q_0, 0, A) = (q_0, AA)$
- $\delta(q_0, 1, A) = (q_0, \epsilon)$
- $\delta(q_1, 1, A) = (q_1, \epsilon)$
- $\delta(q_0, \epsilon, A) = (q_1, \epsilon)$
- $\delta(q_0, \epsilon, Z) = (q_1, \epsilon)$

HOD/SE
17/11/21

Adel
17/11/21