

## SRM Institute of Science and Technology College of Engineering and Technology

## **Department of Mathematics**

SRM Nagar, Kattankulathur – 603203, Chengalpattu District, Tamilnadu

Academic Year: 2023-2024(ODD)

**Tutorial sheet - 1** 

Date:16/10/2023

## Course Code &Title:18MAB302T-Discrete Mathematics for Engineers Year & Sem:III/V

| Q. No | Questions  | Answer Keys |
|-------|--|-------------|
| 1     | Give an example of a non-abelian group.  |             |
| 2     | Examine whether the function $\phi: (Z, +) \to (Z, +)$ defined as $\phi(x) = x + 1$ is a homomorphism or not.  | No          |
| 3     | Compute $\alpha\beta$ , $\beta\alpha$ and $\alpha^{-1}$ if $\alpha = \begin{pmatrix} 1 & 2 & 3 & 4 \\ 2 & 4 & 1 & 3 \end{pmatrix} \text{ and } \beta = \begin{pmatrix} 1 & 2 & 3 & 4 \\ 3 & 4 & 1 & 2 \end{pmatrix}$ |             |
| 4.    | Let $G = \{f_1, f_2, f_3, f_4\}$ where $f_1(x) = x, f_2(x) = -x,$<br>$f_3(x) = 1/x, f_4(x) = -1/x$ and $\circ$ be the composition of function, prove that $(G, \circ)$ is a group.                                   |             |
| 5.    | Prove that every cyclic group is abelian.  |             |
| 6.    | If $(G,*)$ is a group then prove that G is abelian if and only if $(a*b)^2 = a^2*b^2$ .  |             |
| 7.    | Prove that the subgroup of a cyclic group is cyclic.   |             |
| 8.    | Prove that the set {1,3,7,9} is an abelian group under multiplication modulo 10.   |             |
| 9.    | State and prove the necessary and sufficient condition for a non-<br>empty subset H of a group G to be a subgroup of G.  |             |
| 10.   | Show that the intersection of two subgroups of a group is a subgroup.  |             |