

U3

Pumping Lemma for CFL -

$$z = uvwx^i y$$

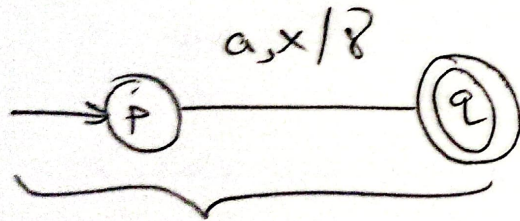
$$i) |vx| \geq 1$$

$$ii) |vwx| \leq n$$

$$iii) \text{ for all } i \geq 0, uv^iwx^i y \in L.$$

PDA - (7 components)

$$* P = (Q, \Sigma, \Gamma, \delta, q_0, Z_0, F)$$



$$\delta(p, a, x) = (q, \delta)$$

$$a \rightarrow \text{input symbol}$$

$$x \rightarrow \text{old top stack symbol}$$

$$\delta \rightarrow \text{new " " " "}$$

$Q \rightarrow$ finite set of states

$\Sigma \rightarrow$ " " " symbols

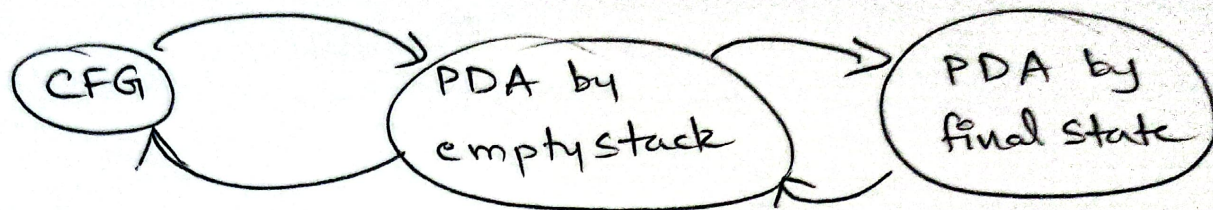
$\Gamma \rightarrow$ a finite stack alphabet

$\delta \rightarrow$ transition function

$q_0 \rightarrow$ initial state

$Z_0 \rightarrow$ starting symbol of stack

$F \rightarrow$ final state



PDA \rightarrow CFG:

* grammar $G = \{V, T, P, S\}$ and $V = \{S, [q_i, z, q_j]\}$

where $q_i, q_j \in Q$ and z is the stack element.

Rule 1 \rightarrow start symbol production $\Rightarrow S \rightarrow [q_0, z_0, q_f], q_f \in Q$.

Rule 2 $\xrightarrow{\text{if}}$ mapping function of PDA $\Rightarrow \delta(q_i, a, z) = (q_j, \epsilon), q_i, q_j \in Q$.

then production $\Rightarrow [q_i, z, q_j] \rightarrow a$

Rule 3 $\xrightarrow{\text{if}}$ mapping function of PDA $\Rightarrow \delta(q_i, a, z) = (q_j, AB), q_i, q_j \in Q$.

then production $\Rightarrow [q_i, z, q_k] \rightarrow a [q_i, A, q_k] [q_k, B, q_j]$

Rule 4 \rightarrow for $\delta(q_i, a, z) = (q_j, A)$

then production $\Rightarrow [q_i, z, q_k] \rightarrow a [q_j, A, q_k]$