

**SRM INSTITUTE OF SCIENCE AND TECHNOLOGY**  
**DEPARTMENT OF MATHEMATICS**  
**18MAB101T-CALCULUS AND LINEAR ALGEBRA**  
**ASSIGNMENT-II (UNIT-II & III) MARKS: 5\*12=60**  
DATE 29/10/2021

1. Solve  $x^2 \frac{d^2 y}{dx^2} + x \frac{dy}{dx} + y = \log x \sin(\log x)$  .
2. Solve by the method of variation of parameters,  $\frac{d^2 y}{dx^2} - y = \frac{2}{1+e^x}$  .
3. Expand  $\tan^{-1}\left(\frac{y}{x}\right)$  about (1,1) upto second-degree term using Taylor's theorem.
4. If  $g(x, y) = \psi(u, v)$  , where  $u = x^2 - y^2$  and  $v = 2xy$  then prove that
$$\frac{\partial^2 g}{\partial x^2} + \frac{\partial^2 g}{\partial y^2} = 4(x^2 + y^2) \left( \frac{\partial^2 \psi}{\partial u^2} + \frac{\partial^2 \psi}{\partial v^2} \right)$$
5. Find the shortest and longest distance between from the point (1,2,-1) to the sphere  $x^2 + y^2 + z^2 = 24$  , using Lagrange's method of constrained maxima and minima.