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1. $A = \begin{vmatrix} 1 & a & 0 \\ 0 & 1 & 1 \\ 0 & -1 & 1 \end{vmatrix} \begin{vmatrix} 1 & 0 \\ 0 & 1 \\ 0 & -1 \end{vmatrix}$ $\rightarrow \text{Det } A = 1 - (-1) = 2$

$0 + (-1) + 0 = -1$

$1 + 0 + 0 = 1$

$B = \begin{vmatrix} 1 & 0 & 0 & 3 \\ 0 & 1 & -1 & 4 \\ 0 & 0 & 0 & 3 \\ 0 & 1 & 1 & 4 \end{vmatrix}$ $\frac{1}{2} \cdot \text{cof}(B_{21})$ $\frac{1}{2} \cdot \text{cof}(B_{41})$

$1 + 1 = 2$

Par \rightarrow permanecer o sinal

\rightarrow escolhida

$\frac{1}{2} \cdot \text{cof}(B_{21})$ $\frac{1}{2} \cdot \text{cof}(B_{41})$ $\frac{1}{2} \cdot \text{cof}(B_{21})$ $\frac{1}{2} \cdot \text{cof}(B_{41})$

\downarrow \downarrow \downarrow \downarrow

$0 + 3 + 0 = 3$ $\text{sempre da } 0$

$\begin{vmatrix} 1 & -1 & 4 \\ 0 & 0 & 3 \\ 1 & 1 & 4 \end{vmatrix} \begin{vmatrix} 1 & -1 \\ 0 & 0 \\ 1 & 1 \end{vmatrix}$ $\rightarrow 3 - (-3) = -6$

$0 + (-3) + 0 = -3$ $1 \cdot (-6) = -6$

$$2 \cdot \text{cof}(B_{21})$$

$$\downarrow \quad 0+0+0=0$$

0	0	3	0	0	
0	0	3	0	0	$\rightarrow 0 \cdot 0 = 0$
1	1	4	1	1	

$$0+0+0=0$$

$$1 \cdot \text{cof}(B_{41}) + 2 \cdot \text{cof}(B_{21})$$

$$1 \cdot (-6) + 2 \cdot 0$$

$$R: -6$$

$$2. A = \begin{vmatrix} x^2 & 0 & x & -\frac{1}{10} \\ 7,5 & 0 & 5 & 2 \\ 10 & 0 & 4 & 2 \\ 1 & 1 & 1 & 1 \end{vmatrix} = 0$$

↳ escolhido

S. cof(A₄₂)

$$\begin{vmatrix} x^2 & x & -\frac{1}{10} \\ 7,5 & 5 & 2 \\ 10 & 4 & 2 \end{vmatrix} \begin{matrix} \nearrow \\ \nearrow \\ \searrow \end{matrix}$$

$-5 + 8x^2 + 15x$

$$\begin{vmatrix} x^2 & x \\ 7,5 & 5 \end{vmatrix} = 0$$

$10x^2 + 20x - 3$

Det. A = $10x^2 + 20x - 3 - 8x^2 - 15 + 5 = 2x^2 + 5x + 2$

$$2x^2 + 5x + 2 = 0$$

$$\Delta = b^2 - 4ac$$

$$x = \frac{-b \pm \sqrt{\Delta}}{2a}$$

$$\Delta = 5^2 - 4 \cdot 2 \cdot 2$$

$$\Delta = 25 - 16$$

$$\Delta = 9$$

$$x = \frac{-5 \pm 3}{4}$$

$$x' = \frac{-5 + 3}{4}$$

$$x'' = \frac{-5 - 3}{4}$$

$$x' = \frac{-2}{4} = -\frac{1}{2} \quad x'' = \frac{-8}{4} = -2$$

~~Wolfram~~

$$3. A = \begin{pmatrix} x & 0 & 0 & 3 \\ -1 & x & 0 & 0 \\ 0 & -1 & x & 1 \\ 0 & 0 & -1 & -2 \end{pmatrix}$$

Wolfram

$$x \cdot \det(A) = 0 \rightarrow x \cdot (-x^3 - x^2 - x - 2) = 0$$

$$\begin{array}{c|c} \begin{matrix} x & 0 & 0 & 3 \\ -1 & x & 0 & 0 \\ 0 & -1 & x & 1 \\ 0 & 0 & -1 & -2 \end{matrix} & \begin{matrix} x & 0 \\ -1 & x \\ 0 & -1 \\ 0 & 0 \end{matrix} \end{array} \rightarrow \begin{array}{l} 0 - x + 0 = -x \\ -2x^2 - (-x) = -2x^2 + x \\ -2x^2 + 0 + 0 = -2x^2 \end{array}$$

$$x \cdot (2x^2 + x)$$

$$-2x^2 + x^3$$

$$-1 \cdot \text{cof}(a_{11})$$

$$2 \cdot 1 = 3 \text{ (Impar = Inverte o sinal)}$$

$$0 + 0 + 0 = 0$$

$$\begin{array}{c|cc} 0 & 0 & 3 \\ \hline -1 & 1 & -1 \\ 0 & -1 & 2 \end{array} \begin{array}{c|cc} 0 & 1 & 0 \\ \hline -1 & 1 & -1 \\ 0 & -1 & 2 \end{array} \rightarrow 3 - 0 = 3$$

$$0 + 0 + 3 = 3$$

$$-1 \cdot (-3)$$

$$3$$

$$(x \cdot \text{cof}(a_{11})) + (-1 \cdot \text{cof}(a_{21}))$$

$$-2x^3 + x^2 + 3$$

$$R = A$$

$$4. \begin{array}{c|ccccc} x & 1 & 0 & 0 & 0 \\ \hline 0 & x & 3 & 0 & 0 \\ 0 & 0 & x & 1 & 0 \\ 0 & 0 & 0 & x & k \\ 0 & 0 & 0 & 1 & x \end{array} \rightarrow x \cdot \text{cof}(A_{11})$$

$$A = \begin{array}{c|ccccc} x & 1 & 0 & 0 & 0 \\ \hline 0 & x & 3 & 0 & 0 \\ 0 & 0 & x & 1 & 0 \\ 0 & 0 & 0 & x & k \\ 0 & 0 & 0 & 1 & x \end{array} \quad B = \begin{array}{c|ccccc} x & 3 & 0 & 0 & 0 \\ \hline 0 & x & 1 & 0 & 0 \\ 0 & 0 & x & k & 0 \\ 0 & 0 & 1 & x & 0 \\ 0 & 1 & x & 0 & x \end{array} \rightarrow x \cdot \text{cof}(B_{11})$$

↙ escalado ↘

$$0 = Kx + 0 = Kx$$

$$\begin{array}{c|cc} x & 3 & 0 \\ \hline 0 & x & k \\ 0 & 1 & x \end{array} \begin{array}{c|cc} x & 3 \\ \hline 0 & x \\ 0 & 1 \end{array} \rightarrow \text{Det } C = x^3 - (Kx) = x^3 - ixk$$

$$x^3 + 0 + 0 = x^3$$

$$f(x) = \text{Det } A \rightarrow f(-2) = 8$$

$$x \cdot \text{cof}(A_{11}) \rightarrow x^5 - x^3 K$$

$$x \cdot \text{cof}(B_{11}) \rightarrow x^5 - x^3 K$$

$$x \cdot \text{cof}(C_{11}) = x^3 - x K$$

$$\text{Det } A = x \cdot \text{cof}(A_{11})$$

$$8 = x^5 - x^3 K$$

$$8 = (-2)^5 - (-2)^3 K$$

$$8 = -32 + 8K$$

$$8K = 8 + 32$$

$$8K = 40$$

$$K = \frac{40}{8}$$

$$K = 5$$