

Cross-Entropy ($ce(y, \hat{y})$)

$$ce(y, \hat{y}) = - \sum_{i=0}^n y_i \log(\hat{y}_i)$$

- n : number of classes
- y : actual output
- \hat{y} : predicted output

$$\frac{\partial ce(y, \hat{y})}{\partial y_k} = \frac{\partial}{\partial y_k} \sum_{i=0}^n y_i \log(\hat{y}_i) =$$

$$= \frac{\partial}{\partial y_k} y_k \log(\hat{y}_k) = y_k \cdot \frac{1}{\hat{y}_k}$$

$$\frac{\partial ce(y, \hat{y})}{\partial y_k} = \frac{y_k}{\hat{y}_k}$$

MSE ($\text{mse}(y, \hat{y})$)

$$\text{mse}(y, \hat{y}) = - \sum_{i=0}^n (\hat{y} - y)^2$$

- n : number of classes
- y : actual output
- \hat{y} : predicted output

$$\frac{\partial \text{mse}(y, \hat{y})}{\partial y_k} = \frac{\partial}{\partial y_k} \sum_{i=0}^n (\hat{y}_k - y_k)^2 =$$

$$= \frac{\partial (\hat{y}_k - y_k)^2}{\partial y_k} =$$

$$= 2 \cdot (\hat{y}_k - y_k) \cdot \frac{\partial (\hat{y}_k - y_k)}{\partial y_k} =$$

$$= 2 \cdot (\hat{y}_k - y_k) \cdot (-1)$$

$$\frac{\partial \text{mse}(y, \hat{y})}{\partial y_k} = 2(y_k - \hat{y}_k)$$