

Tutorial 6

(1)

Name - Amenderp Singh

Course - B.Tech CSE

Section - G

Sem - 4

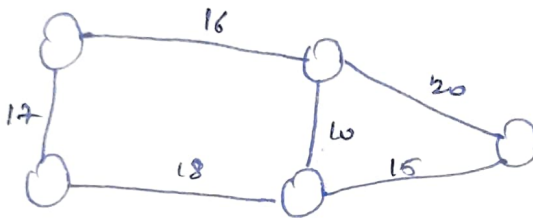
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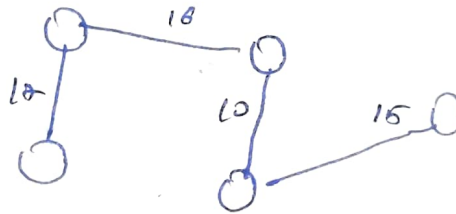
Ans 1 Minimum Spanning tree

A spanning tree of an undirect graph is a subgraph that is a tree & joined by all vertices. One of those trees which has minimum total cost would be its minimum spanning tree.

eg :-



Minimum Cost spanning tree →



* Applications of MST :-

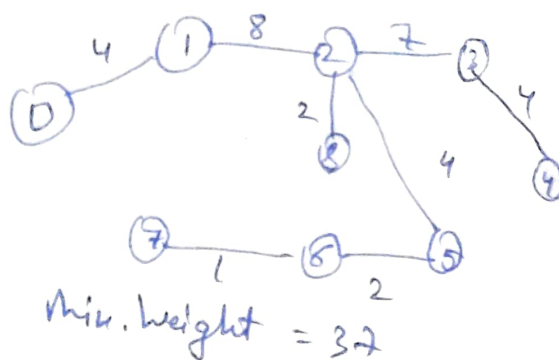
→ It has direct applications in the design of network including. computer networks, telecommunication networks, transportation networks etc.

Ans 2	Prim's Algo.	Kruskal's Algo	Dijkstra's Algo.	Bellman ford Algo
T.C.	$O(V^2)$	$O(E \log V)$	$O(V + E \log V)$	$O(VE)$
S.C.	$O(V + E)$	$O(E) + (V)$	$O(V^2)$	$O(V^2)$

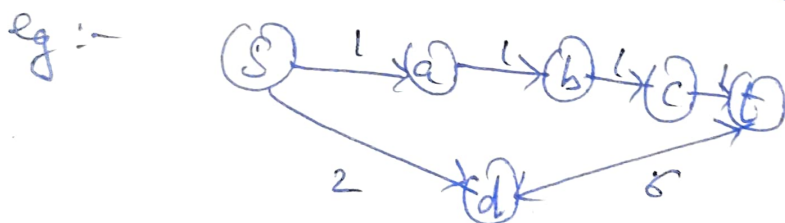
~~Kruskal~~ Kruskal's Algo :-

(3)

u	v	w
7	6	1 -
6	5	2 -
2	8	2 -
2	5	4 -
0	1	4 -
8	6	4 -
7	8	6 x
2	3	7 -
1	2	7 -
0	7	8 -
3	4	8 x
5	4	9 -
1	7	10 x
3	5	11 x
		14 x



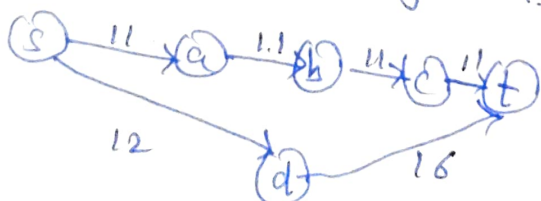
Ans 4 (i) if 10 units is added to each edge, the overall weight of the path may change.



Shortest path $\rightarrow s \rightarrow a \rightarrow b \rightarrow c \rightarrow t$

weight $1+1+1+1 \rightarrow 4$

Now if 10 unit weight is added to each edge :-

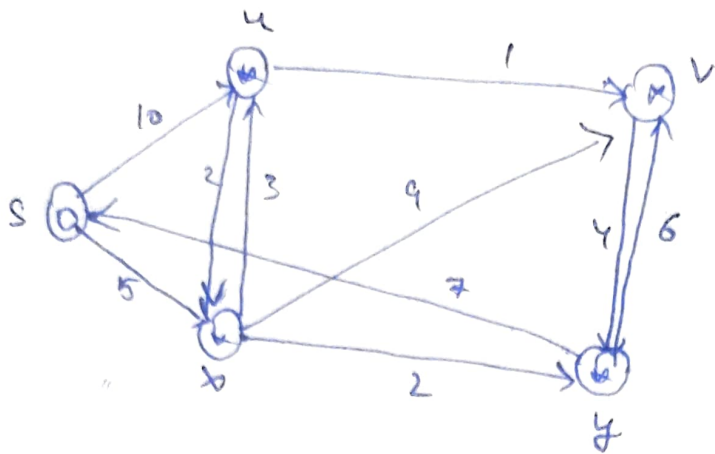


Shortest path changes $\rightarrow s \rightarrow d \rightarrow t$

weight = 28

(ii) Multiplying the weight of each edge by 10 will have no impact on the shortest path. (4)

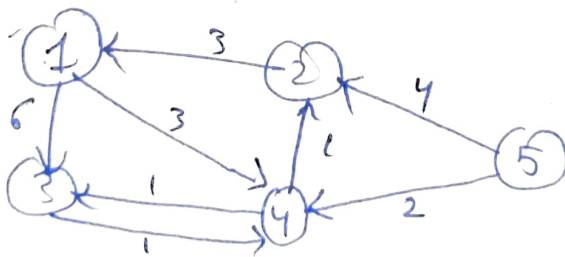
Ans 5



s	u	v	x	y
0	∞	∞	∞	∞
0	10	∞	5	∞
0	10	11	5	∞
0	16	11	5	7

Ans 6

All pair shortest path algo - floyd warshall



	1	2	3	4	5
1	0	∞	6	3	∞
2	3	0	∞	∞	∞
3	∞	∞	0	∞	∞
4	∞	1	0	2	∞
5	∞	4	∞	0	0

$$A^1 = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 & 5 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \end{matrix} & \begin{bmatrix} 0 & \infty & 6 & 3 & \infty \\ 3 & 0 & 9 & 6 & \infty \\ \infty & \infty & 0 & 2 & \infty \\ \infty & 1 & 1 & 0 & \infty \\ \infty & 4 & \infty & 2 & 0 \end{bmatrix} \end{matrix}$$

$$A^0[2,3] = \infty$$

$$A^0[2,1] + A^0[1,3] = 3 + 6 = 9$$

$$9 < \infty$$

Similarly, $A^0[2,4] = \infty$

$$A^0[2,1] + A^0[1,4] = 3 + 3 = 6$$

$$A^0[2,5] = \infty$$

$$A^0[2,1] + A^0[1,5] = 3 + \infty$$

$$A^2 = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 & 5 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \end{matrix} & \begin{bmatrix} 0 & \infty & 6 & 3 & \infty \\ 3 & 0 & 9 & 6 & \infty \\ \infty & \infty & 0 & 2 & \infty \\ \infty & 1 & 1 & 0 & \infty \\ 7 & 4 & 13 & 2 & 0 \end{bmatrix} \end{matrix}$$

$$A^1[1,3] = 6$$

$$A^1[1,2] = A^1[2,3] = \infty + 9$$

$$6 < \infty + 9$$

A³ =

$$A^3 = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 & 5 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \end{matrix} & \begin{bmatrix} 0 & \infty & 6 & 3 & \infty \\ 3 & 0 & 9 & 6 & \infty \\ \infty & \infty & 0 & 2 & \infty \\ \infty & 1 & 1 & 0 & \infty \\ 7 & 4 & 13 & 2 & 0 \end{bmatrix} \end{matrix}$$

A⁴ =

$$A^4 = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 & 5 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \end{matrix} & \begin{bmatrix} 0 & 4 & 4 & 3 & \infty \\ 3 & 0 & 7 & 6 & \infty \\ \infty & 3 & 0 & 2 & \infty \\ \infty & 1 & 1 & 0 & \infty \\ 7 & 3 & 3 & 2 & 0 \end{bmatrix} \end{matrix}$$

A⁵ =

$$A^5 = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 & 5 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \\ 5 \end{matrix} & \begin{bmatrix} 0 & 4 & 4 & 3 & \infty \\ 3 & 0 & 7 & 6 & \infty \\ \infty & 3 & 0 & 2 & \infty \\ \infty & 1 & 1 & 0 & \infty \\ 7 & 3 & 3 & 2 & 0 \end{bmatrix} \end{matrix}$$

