

PAPER

Salmon: Combining Inference Modes

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Abstract

Salmon provides a fast and accurate way to estimate transcript abundance. This method uses a dual-phase inference algorithm and takes into account fragment biases for transcript verification. However, there are some areas where Salmon could improve. The inference algorithms used—EM and VBEM—are only point estimates and cannot be checked if there is no ground truth available. Furthermore, the choice of prior when using the VBEM algorithm can affect the accuracy of the results. In this work, we test how averaging the inference model predictions affect the accuracy of the inference estimation during Salmon’s offline phase.

Key words: Salmon, VBEM, Inference, EM, RNA Transcription

Introduction

A key characteristic of many newly-formed eukaryotic RNA sequences is the inclusion of non-coding and coding regions, which are often referred to as introns and exons. Prior to translation, transcript maturation must occur via splicing, a process that revolves around the displacement of introns from the mRNA sequence. However, depending on environmental conditions and sequence variations, some exons are often removed from the mRNA as well, eventually resulting in the creation of a different protein isoform. Unfortunately, the many factors related to alternative splicing are still poorly understood for most eukaryotic proteins, hence the reasoning behind the continuation of transcriptome projects.

One essential facet to transcriptomics is the sequencing techniques used to generate transcript fragments for data analysis. Prior approaches to transcriptome quantification involved the use of microarrays, which has important limitations such as relatively high risks of cross-hybridization, low range of detection, and complicated normalization methods for differential expression analysis [11]. RNA-Seq, on the other hand, does not face such limitations and retains microarrays’ advantage over classical sequencing such as high-throughput capabilities and the use of inexpensive technology. It has been revolutionary in furthering the field of transcriptomics, specifically with regards to eukaryotic cell transcriptomes. In particular, recent RNA-seq experiments yielded meaningful results in quantifying expression difference across different tissues [4], distinguishing host-pathogen interactions [10], and identifying the effect of structural variants on splicing regulators [8].

Equally important to transcriptomics is abundance quantification. Estimations can be done through an alignment to a reference transcriptome sequence; nevertheless, a constant struggle with quantifying eukaryotic samples is to map read fragments back to the original transcript as opposed to

the original gene. Although the detection of protein family abundances can be useful on its own, oftentimes researchers are more so interested in transcript abundances. Since isoforms of the same protein will retain common exons, identifying the source of each read is a tedious process that requires complex statistical methods.

In the past, Salmon was developed to address this particular issue. Given a known transcript and a set of sequenced fragments, it quantifies the relative abundance of each transcript in the sample using a dual-phase inference procedure. Salmon improves accuracy compared to other models, because it takes into account sample-specific biases to improve accuracy. When these biases are not accounted for, calculations like the false discovery rate cannot be controlled for. Using multiple inference steps, Salmon improves its abundance estimates using either the VBEM or EM inference algorithms. However, both methods have drawbacks. Both algorithms return point estimates of abundances, and we are uncertain about the returned estimates without ground truth. Further, the choice of Bayesian priors used in the VBEM algorithm also has considerations. A small prior leads to sparser results than EM. However, a larger prior may result in more estimated non-zero abundance than EM. Prior simulated tests [2] show that VBEM with a small prior can lead to more accurate estimates. However, there has been much research into improving the results of these algorithms such as model averaging [5].

Given the trade offs of the two algorithms, we sought to know if the averaged prediction for EM and VBEM inference is better than one algorithm or another. Further, if this ensemble estimate is better, could it be improved by varying the Bayesian priors. We find that a naive average of these outputs does not result in conclusive results. We saw that using the average is very similar to EM when used with a lower prior and more similar to the VBEM output when used with a higher prior. In

light of these results we have also included a section on future work.

Salmon

Salmon uses a dual-phase inference procedure to provide fast and accurate estimates. In an online and offline step, Salmon is able to calculate and improve the abundance estimates for a transcript based on fragment GC-content and positional biases. Salmon initially utilizes raw reads in a quasi-mapping phase where it performs direct quantification instead of enacting a traditional alignment. Salmon then moves to an online inference phase. Here, Salmon uses a variant of stochastic, collapsed variational Bayesian inference to solve a variation Bayesian inference problem. In this phase, Salmon estimates the initial expression levels, auxiliary parameters, the ‘foreground’ bias models, and fragment equivalence classes. In the offline phase, Salmon improves the estimates it calculated in the online phase. Here, the user can specify the inference algorithm of EM or VBEM. The chosen algorithm runs to convergence on this data, outputting an optimized array of abundances. Optionally, using the converged abundances and fragment equivalence classes, Salmon can also draw and save estimates from the posterior distribution using Gibbs or bootstrap sampling.

EM & VBEM

The Expectation Maximization (EM) algorithm optimizes the likelihood of the parameters given the data. This algorithm returns a point estimate of the abundances. This algorithm was previously the default of Salmon, but preliminary results demonstrated that VBEM-inferred estimates tended to be more accurate [2]

The Variational Bayesian Expectation Maximization (VBEM) algorithm accounts for the sparsity of the data. It takes a Bayesian nucleotide prior that controls for the sparsity of the data. The default prior for Salmon was 1×10^{-2} .

Each transcriptome \mathcal{T} is composed of transcripts t . Each transcript is a nucleotide sequence which can be described through its length l , effective length \tilde{l} , and its count c —which is the number of times that t occurs in a given sample. There are M transcripts in a given transcriptome.

The probability that a given fragment originates from a transcript t depends on the length of that transcript relative to all other transcripts in the transcriptome. We define this nucleotide fraction η for a given transcript t as

$$\eta_i = \frac{c_i \cdot \tilde{l}_i}{\sum_{j=1}^M c_j \cdot \tilde{l}_j}$$

We obtain a transcript fraction τ for a given transcript t by normalizing its nucleotide fraction against the effective length of all transcripts.

$$\eta_i = \frac{c_i \cdot \tilde{l}_i}{\sum_{j=1}^M c_j \cdot \tilde{l}_j}$$

Let’s say that the true nucleotide fraction for a transcript t is η . We can describe the probability of observing a set of sequenced fragments \mathcal{F} as a

$$\begin{aligned} \Pr(\mathcal{F}|\boldsymbol{\eta}, Z, \mathcal{T}) &= \prod_{j=1}^N \Pr(f_j|\boldsymbol{\eta}, Z, \mathcal{T}) \\ &= \prod_{j=1}^N \sum_{i=1}^M \Pr(t_i|\boldsymbol{\eta} \cdot \Pr(f_j|t_i, z_{ij} = 1)) \end{aligned}$$

where N is the number of fragments in \mathcal{F} , Z is a relationship matrix where $z_{ij} = 1$ when fragment f_j is derived from t_i .

We want to obtain $\boldsymbol{\alpha}$, which is the estimated number of reads from each transcript. We describe the maximum likelihood estimates as:

$$\mathcal{L}(\boldsymbol{\alpha}|\mathcal{F}, Z, \mathcal{T}) = \prod_{j=1}^N \sum_{i=1}^M \hat{\eta}_i \Pr(f_j|t_i)$$

Written in terms of equivalence classes \mathcal{C}

$$\mathcal{L}(\boldsymbol{\alpha}|\mathcal{F}, Z, \mathcal{T}) = \prod_{\mathcal{C}^j \in \mathcal{C}} \left(\sum_{t_i \in \mathcal{C}^j} \hat{\eta}_i w_t^j \right)^{d^j}$$

The abundances $\hat{\eta}$ are computed directly from $\boldsymbol{\alpha}$

$$\hat{\eta}_i = \frac{\alpha_i}{\sum_j \alpha_j}$$

Then we apply an update function

$$\alpha_i^{u+1} = \sum_{\mathcal{C}^j \in \mathcal{C}} d^j \left(\frac{\alpha_i^u w_i^j}{\sum_{t_k \in \mathcal{C}^j} \alpha_k^u w_k^j} \right)$$

Until the maximum relative difference in $\boldsymbol{\alpha}$ is

$$\Delta(\alpha^u, \alpha^{u+1}) = \max_i \frac{|\alpha_i^u - \alpha_i^{u+1}|}{\alpha_i^{u+1}} < 1 \times 10^{-2}$$

for all $\alpha_i^{u+1} > 1 \times 10^{-8}$, at which point we derive the estimated nucleotide fraction

$$\hat{\eta}_i = \frac{\alpha'_i}{\sum_j \alpha'_j}$$

Variational Bayes Optimization

Optionally, the we can apply variational bayeseian optimization where the update function is

$$\alpha_i^{u+1} = \sum_{\mathcal{C}^j \in \mathcal{C}} d^j \left(\frac{e^{\gamma_i^u} e_i^j}{\sum_{t_k \in \mathcal{C}^j} j e^{\gamma_k^u} w_k^j} \right)$$

where

$$\gamma_i^u = \Psi \left(\sum_{k=1}^M \alpha_k^0 + \alpha^u + \alpha_k \right)$$

where Ψ is the digamma function and the expected value of nucleotide fractions can be expressed as

$$\begin{aligned} \mathbb{E}(\eta_i) &= \frac{\alpha_i^0 + \alpha'_i}{\sum_j \alpha_j^0 + \alpha'_j} = \frac{\alpha_i^0 + \alpha'_i}{\hat{\alpha}^0 + N} \\ \hat{\alpha}^0 &= \sum_{i=1}^M \alpha_i^0 \end{aligned}$$

```

salmon quant -i human_index -l IU -1 sample_1.fa.gz -2 sample_2.fa.gz -p 6 --gcBias --useEM \
--validateMappings -o sample
salmon quant -i human_index -l IU -1 sample_1.fa.gz -2 sample_2.fa.gz -p 6 --gcBias --vbPrior \
1e{from -5 to 1} --validateMappings -o sample
salmon quant -i human_index -l IU -1 sample_1.fa.gz -2 sample_2.fa.gz -p 6 --gcBias --useBoth \
--vbPrior 1e{from -5 to 1} --validateMappings -o sample

```

Fig. 1. Commands used for the quantification of each sample using EM, VBEM, or both inference strategies, respectively.

Methods

Combining the traditional EM algorithm with the VBEM algorithm

Since we are only interested in optimizing abundance estimation in the offline phase, we opted to directly change Salmon v1.10.3's source code. We introduce a new flag, `useBoth`, which forces the program to run the offline phase twice: once with the traditional EM algorithm and once with the VBEM algorithm. The program then computes the average of the two different estimates for the α vector before computing its final prediction for η .

Running the new implementation on the polyester dataset

The commands used for the quantification of each sample using EM, VBEM, or both inference strategies, are provided in Fig 1.

Quantification was run on the 24 samples through a slurm batch script. For each run, 5GB of memory was allocated on the CBCB's Nexus partition. In total, every sample had 15 runs, each with different specifications for the inference method (1 EM, 7 VBEM, and 7 combo) and the prior value if applicable (10^{-5} to 10^1). All other parameters were kept the same among the 360 total runs:

1. We kept the selective alignment feature on for this experiment. This strategy is currently the default for the pipeline, and it allows Salmon to adopt a more sensitive approach during quasi-mapping.
2. In recent versions of Salmon, the library type can be automatically detected. Nevertheless, we elected to specify the library type for all the runs.
3. The `--gcBias` flag was passed to the pipeline as well, which allows Salmon to identify and remedy for GC biases. This extra step is essential for the analysis of our synthetic data since they were simulated from an already existing GC bias profile [7].

Statistical Evaluation

The statistical evaluation of the different inference algorithms was performed with R. Because only the original simulated read counts were made available to, we conducted our comparisons on the estimated number of reads given by Salmon. We chose two statistical metrics for our analysis: The mean absolute relative difference, or MARD, was already introduced in the original Salmon publication. It is the average of the absolute relative difference ARD for each transcript i , where x_i is the original simulated read count, and y_i is the read count reported

by Salmon.

$$\text{ARD}_i = \begin{cases} 0 & \text{if } x_i = y_i = 0 \\ \frac{|x_i - y_i|}{x_i + y_i} & \text{otherwise} \end{cases}$$

$$\text{MARD} = \frac{1}{M} \sum_{i=1}^M \text{ARD}_i$$

The Spearman correlation, also described in the original publication, calculates the relationship between the rank for our results and the rank for the simulated data. It was computed through the `core.test` function where we indicated a two sided alternative hypothesis.

$$\rho = 1 - \frac{6 \sum d_i^2}{n(n^2 - 1)}$$

Additionally, we were also required to measure the differences between the three inference algorithms. We used the Mann-Whitney test (also known as the Wilcoxon test) to calculate the p value for such analysis, and computations were also performed in R with the `wilcox.test` function

Datasets

We used the same synthetic dataset from Love's 2018 method article on DTU analysis, which consists of 24 sets of unstranded inward pair-ended reads [7]. This data was generated using polyester 1.16.0 and alpine version 1.6.0. [3] We also utilized the *Homo sapiens* GRCh37 version 28 sequence as our human transcriptome reference, which was the same reference used for the generation of the simulated read. [1]

Results

We encountered different results depending on the prior selected. Overall, we can separate the outcome of combining both inference algorithms into two categories. The first of such categories includes runs with a prior between 10^{-5} and 10^1 , inclusive. As shown in figures 2 and 3, both the MARD values and the Spearman correlation values are lower for estimates inferred from VBEM than for estimates inferred from both methods (Mann-Whitney U test, $P \leq 1.436 \cdot 10^{-7}$ for MARD, $P < 6.202 \cdot 10^{-14}$ for Spearman). However, MARD values tended to be similar between estimates inferred from EM and estimates inferred from both methods (Mann-Whitney U test, $P \geq 0.4803$), whereas the Spearman correlation values were slightly higher for EM (Mann-Whitney U test, $P \leq 0.03941$). Because the MARD metrics are negatively impacted by false discovery rates [9], we hypothesize that the results gathered from running both inference algorithms is affected by EM's tendency to collect more non-zero abundances than VBEM at low prior values.

This can also be concluded from the analysis of our second category, which includes runs with a prior of 1 or 10. Unlike with the first category, the MARD and the Spearman correlation values are strikingly lower for the estimates inferred from EM (Mann-Whitney U test, $P < 6.202 \cdot 10^{-14}$ for MARD, $P < 6.202 \cdot 10^{-14}$ for Spearman), whereas the difference in MARD between VBEM and the combination of both methods was insignificant for runs with a prior of 1 (Mann-Whitney U test, $P = 0.8944$). The difference between the Spearman correlation values and between the MARD values for runs with a prior of 10 was still significant (Mann-Whitney U test, $P = 5.675 \cdot 10^{-11}$ for MARD, $P < 6.202 \cdot 10^{-14}$ for Spearman). From those observations, we predict that for high prior values, the negative impact from false discovery rates by the VBEM algorithm is offsetted by the more accurate abundance estimates from the EM algorithm.

Discussion

We were unable to definitively say whether our method improved on Salmon. The output of using the average of the EM and VBEM results produced similar results to just EM or VBEM by themselves. A lower prior, 10^{-5} to 10^{-1} , resulted in similar results to EM while priors greater than 10^0 resulted in similar results to VBEM. At no point does it appear that using the average of both methods significantly improved the output, but it also did not significantly harm the results. This is likely attributed to our method of combining EM and VBEM. Even though we did not find conclusive results, there are next steps to further this work.

Future Work

In our results we saw that using the average of both VBEM and EM is very similar to EM when used with a lower prior and more similar to the VBEM output when used with a higher prior. We have hypothesized this is because we were taking the average even when one of the results was a zero. In future work, we would like to prioritize zero abundances over non-zero abundances. Instead of taking the average between value and zero, we want to record the value as zero. If neither result is a zero, we wish to take the average of those values. We believe this could improve our estimates.

In the current timeframe, we were unable to expand on our project, but in future work, we would like to expand upon ways to best combine the results of the EM and VBEM algorithms. Currently, our code is only taking the mean of the two results. However, we would also like to experiment with the weighted average or the Bayesian model average of these two algorithms also taking into account various prior sizes. We hypothesize that this would further improve Salmon's results [9]. Additionally, we also would like to test our approach on real life data. Although we picked out a dataset consisting of sequencing reads from NK cells, T cells, and tumor collected from matched soft tissue sarcoma and peripheral blood [6], we were pressed for time and resources, and therefore we had to abandon this portion of our project.

We would also like to verify the time it takes to run our combined approach. It would be beneficial to run multiple trials to gain an idea of the time it takes to run Salmon using our solution. We would like to verify that running this approach will not greatly impact the runtime of Salmon. The runtime is expected to increase, since we are running both the EM and

VBEM algorithms. However, we would like to verify that it is not detrimental to the use of Salmon.

In future work, it would be useful to measure the uncertainty of our trials. We were unable to run this during our initial experiments. However, we would like to know if there is a level of uncertainty with our results when we use the average of the EM and VBEM algorithms. We would like to know if this uncertainty increases or decreases, and if so, whether the change in uncertainty is significant. Salmon already supports this analysis through the use of a flag.

References

1. Homo_sapiens - Ensembl genome browser 112.
2. Salmon 1.10.2 documentation.
3. Alyssa C Frazee, Andrew E Jaffe, Ben Langmead, and Jeffrey T Leek. Polyester: simulating rna-seq datasets with differential transcript expression. *Bioinformatics*, 31(17):2778–2784, 2015.
4. Dafni A. Glinos, Garrett Garborcauskas, Paul Hoffman, Nava Ehsan, Lihua Jiang, Alper Gokden, Xiaoguang Dai, François Aguet, Kathleen L. Brown, Kiran Garimella, and et al. Transcriptome variation in human tissues revealed by long-read sequencing. *Nature*, 608(7922):353–359, Aug 2022.
5. Jennifer A. Hoeting, David Madigan, Adrian E. Raftery, and Chris T. Volinsky. Bayesian model averaging: a tutorial (with comments by M. Clyde, David Draper and E. I. George, and a rejoinder by the authors. *Statistical Science*, 14(4):382–417, November 1999.
6. Sean J. Judge, Joshua D. Bloomstein, Cyrus J. Sholevar, Morgan A. Darrow, Kevin M. Stoffel, Logan V. Vick, Cordelia Dunai, Sylvia M. Cruz, Aryana M. Razmara, Arta M. Monjazeb, Robert B. Rebhun, William J. Murphy, and Robert J. Canter. Transcriptome Analysis of Tumor-Infiltrating Lymphocytes Identifies NK Cell Gene Signatures Associated With Lymphocyte Infiltration and Survival in Soft Tissue Sarcomas. *Frontiers in Immunology*, 13:893177, 2022.
7. Michael I. Love, Charlotte Soneson, and Rob Patro. Swimming downstream: statistical analysis of differential transcript usage following Salmon quantification. *F1000Research*, 7:952, October 2018.
8. Corina Pascal, Jonathan Zonszain, Ofir Hameiri, Chen Gargi-Levi, Galit Lev-Maor, Luna Tammer, Tamar Levy, Anan Tarabeih, Vanessa Rachel Roy, Stav Ben-Salmon, and et al. Human histone h1 variants impact splicing outcome by controlling rna polymerase ii elongation. *Molecular Cell*, 83(21), Nov 2023.
9. Rob Patro, Geet Duggal, Michael I. Love, Rafael A. Irizarry, and Carl Kingsford. Salmon provides fast and bias-aware quantification of transcript expression. *Nature Methods*, 14(4):417–419, April 2017.
10. Davide Pisu, Lu Huang, Jennifer K. Grenier, and David G. Russell. Dual rna-seq of mtb-infected macrophages in vivo reveals ontologically distinct host-pathogen interactions. *Cell Reports*, 30(2), Jan 2020.
11. Zhong Wang, Mark Gerstein, and Michael Snyder. Rna-seq: A revolutionary tool for transcriptomics. *Nature Reviews Genetics*, 10(1):57–63, Jan 2009.

Table 1. Spearman correlation table for first four samples and their subsamples.

	Sample 1 ₀₁	Sample 1 ₀₂	Sample 2 ₀₁	Sample 2 ₀₂	Sample 3 ₀₁	Sample 3 ₀₂	Sample 4 ₀₁	Sample 4 ₀₂
EM	0.932	0.932	0.933	0.932	0.937	0.936	0.934	0.933
both - 10^{-5}	0.933	0.933	0.934	0.933	0.939	0.938	0.935	0.934
VBEM - 10^{-5}	0.952	0.951	0.953	0.951	0.957	0.956	0.954	0.952
both - 10^{-4}	0.933	0.933	0.934	0.933	0.939	0.938	0.935	0.934
VBEM - 10^{-4}	0.952	0.951	0.953	0.951	0.957	0.956	0.954	0.952
both - 10^{-3}	0.933	0.933	0.934	0.933	0.939	0.938	0.935	0.934
VBEM - 10^{-3}	0.952	0.951	0.953	0.951	0.957	0.956	0.954	0.952
both - 10^{-2}	0.933	0.933	0.934	0.933	0.939	0.938	0.935	0.934
VBEM - 10^{-2}	0.952	0.951	0.953	0.952	0.957	0.956	0.954	0.952
both - 10^{-1}	0.933	0.933	0.934	0.933	0.939	0.937	0.935	0.934
VBEM - 10^{-1}	0.951	0.950	0.953	0.951	0.957	0.955	0.954	0.951
both - 10^0	0.755	0.754	0.755	0.754	0.755	0.755	0.755	0.754
VBEM - 10^0	0.751	0.751	0.751	0.751	0.752	0.752	0.751	0.751
both - 10^1	0.736	0.735	0.736	0.736	0.738	0.737	0.736	0.736
VBEM - 10^1	0.715	0.715	0.715	0.716	0.717	0.717	0.715	0.715

Table 2. MARD table for first four samples and their subsamples.

	Sample 1 ₀₁	Sample 1 ₀₂	Sample 2 ₀₁	Sample 2 ₀₂	Sample 3 ₀₁	Sample 3 ₀₂	Sample 4 ₀₁	Sample 4 ₀₂
EM	0.284	0.285	0.273	0.276	0.243	0.245	0.277	0.278
both - 10^{-5}	0.287	0.287	0.275	0.278	0.245	0.247	0.279	0.280
VBEM - 10^{-5}	0.241	0.243	0.229	0.232	0.199	0.201	0.233	0.235
both - 10^{-4}	0.287	0.287	0.275	0.278	0.245	0.247	0.279	0.280
VBEM - 10^{-4}	0.241	0.243	0.229	0.232	0.199	0.201	0.233	0.235
both - 10^{-3}	0.287	0.287	0.275	0.278	0.245	0.247	0.279	0.280
VBEM - 10^{-3}	0.241	0.243	0.229	0.232	0.199	0.201	0.232	0.235
both - 10^{-2}	0.287	0.287	0.275	0.278	0.244	0.247	0.279	0.280
VBEM - 10^{-2}	0.241	0.243	0.229	0.232	0.198	0.201	0.232	0.235
both - 10^{-1}	0.286	0.287	0.274	0.277	0.244	0.246	0.278	0.280
VBEM - 10^{-1}	0.241	0.243	0.229	0.232	0.199	0.201	0.233	0.235
both - 10^0	0.663	0.662	0.658	0.658	0.647	0.647	0.660	0.660
VBEM - 10^0	0.662	0.662	0.658	0.658	0.647	0.647	0.660	0.659
both - 10^1	0.663	0.663	0.660	0.659	0.651	0.650	0.662	0.660
VBEM - 10^1	0.678	0.678	0.675	0.674	0.667	0.666	0.677	0.675

Supplementary

Min, Median, and Max MARD

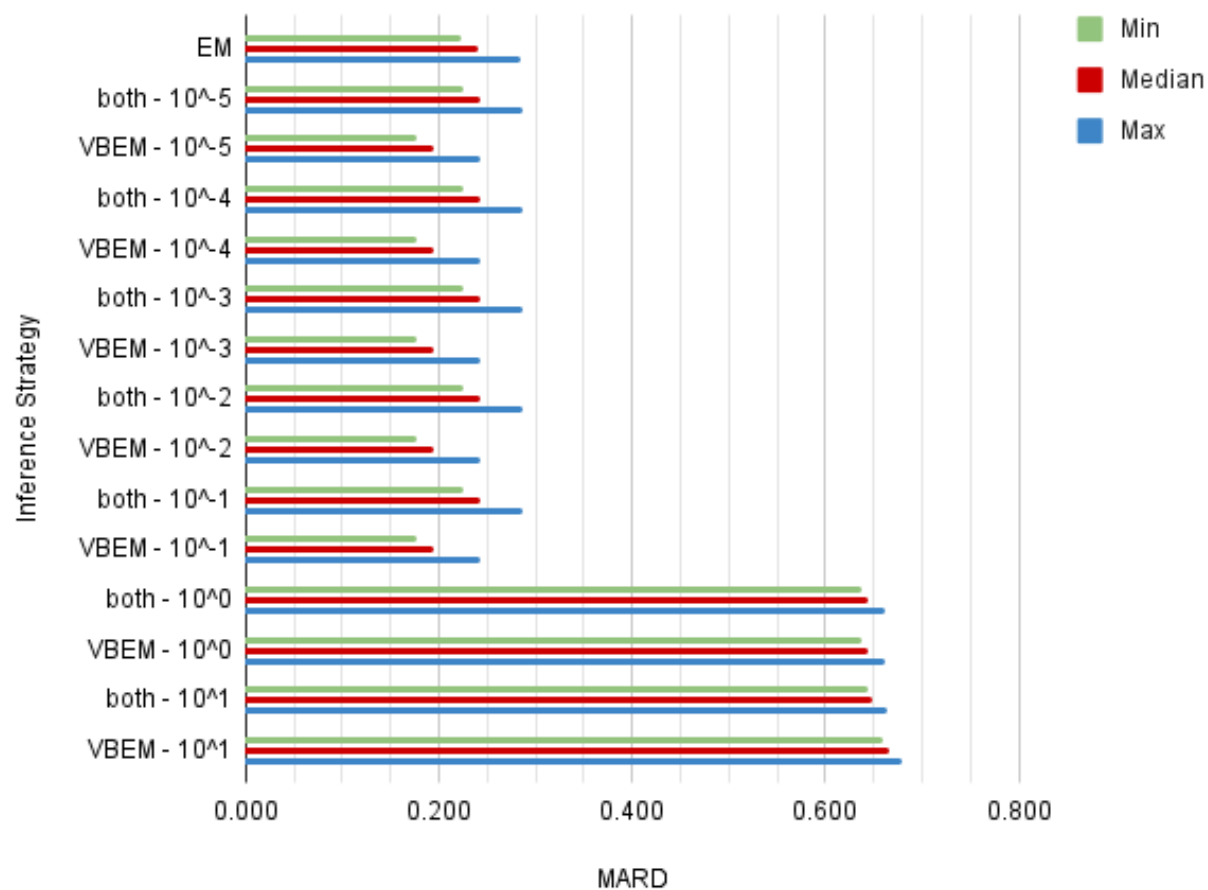


Fig. 2. Min, Median, and Max MARD

Min, Median, and Max Spearman Correlation

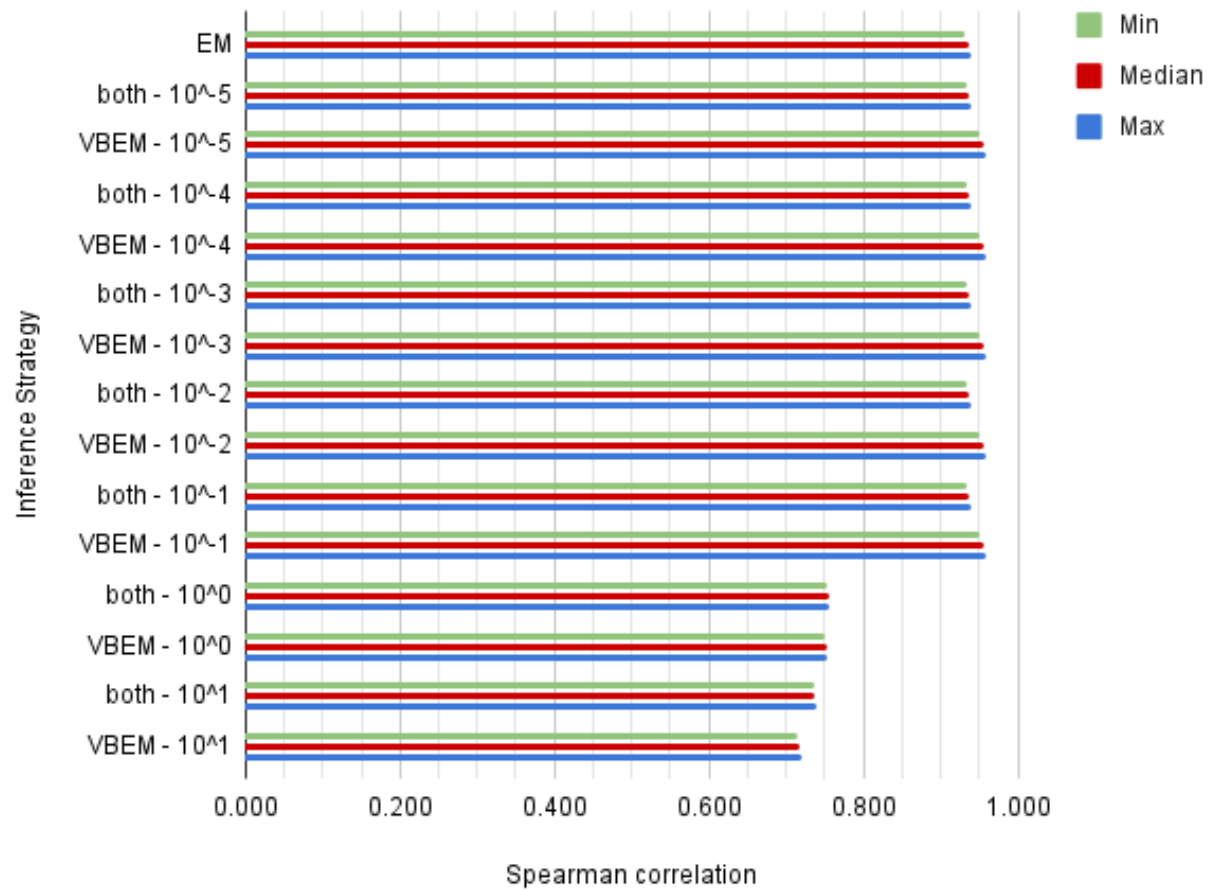


Fig. 3. Min, Median, and Max Spearman Correlation