

Design and Analysis of Algorithms

ASSIGNMENT-21

Group-2 Section-C

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Problem:

The longest Zig-Zag subsequence problem is to find length of the longest subsequence of given sequence such that all elements of this are alternating.



01

Approach

Basic

ALGORITHM-1

- During recursion, we will determine the state of the problem if,
State is 0 then we want an element smaller than it as subsequence is already been started
State is 1 then t we want an element greater than it as subsequence is already been started
State is 2 then we can take any element as subsequence is yet to be started.

Then in the Base case, when we have no further elements left. ($n==0$).

- After knowing the state, either discard the number or include the number in the current sequence if the previous element is smaller with state = 1 or previous element is greater with state = 0 and if state =2 we take all of the possibilities.

Pseudo Code :

```
HELPER(arr,n,prev,state)
{
    if n = 0 then
        return 0
    if state < 0 then
    {
        a = b = INT_MIN
        a = HELPER(arr,n - 1, prev, state)
        if arr[n - 1] > prev then
            b = 1 + HELPER(arr,n - 1, arr[n - 1], 1)
        return max(a, b)
    }
}
```

```
else if state > 0
{
    a = b = INT_MIN
    a = HELPER(arr,n - 1, prev, state)
    if arr[n - 1] < prev then
        b = 1 + solve(arr,n - 1, arr[n - 1], -1)
    return max(a, b)
}
else
{
    a = b = c = INT_MIN
    a = HELPER(arr,n - 1, prev, state)
    b = 1 + solve(arr,n - 1, arr[n - 1], -1)
    c = 1 + solve(arr,n - 1, arr[n - 1], 1)
    return max(a, max(b, c))
}
```

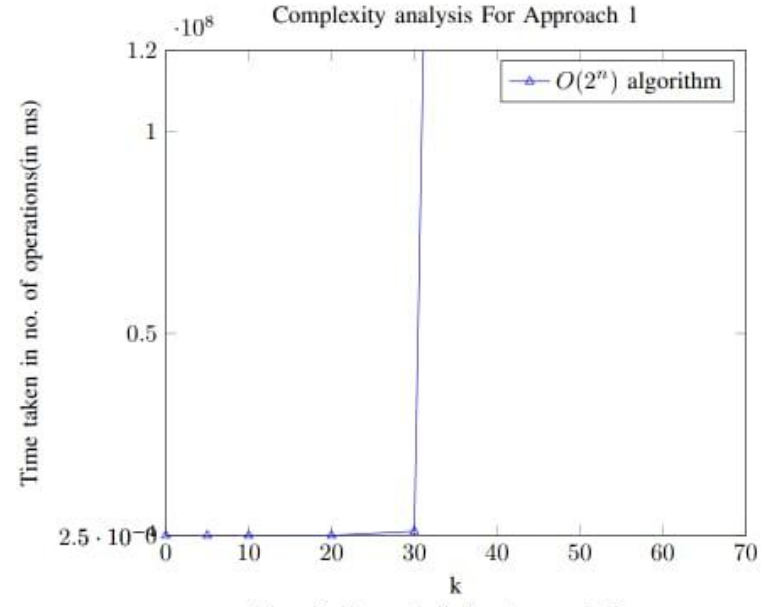
Time Complexity and Space Complexity Analysis

Time Complexity Analysis

The time complexity will be $O(2^n)$ because it checks out all the possibilities by recursing.

Space Complexity Analysis

The space complexity is $O(n)$, for storing the input array.





02

Approach

Using DP

ALGORITHM-2

- At start, we get to know about the state of the problem whether it is 0, 1 or 2.
- To store the values of each element, there is a two dimensional matrix of size $n \times 3$ ($dp[n][3]$).
- 2D matrix will store each element's state in best possible way.
- If the value of $dp[i][state]$ is precalculated then directly pass on it for further calculation, else calculate $dp[i][state]$ and store it for further use.
- Finally we return the length of the subsequence.

Pseudo Code :

```
int HELPER(n,prev,state,dp[][],arr)
{
    if n=0 then
        return 0
    if dp[n][state] != -1 then
        return dp[n][state]

    if state = 0
    {
        a=b=INT_MIN
        a = HELPER(n-1,prev,state,dp,arr)
        if arr[n-1]>prev then
            b = 1+ HELPER(n-1, arr[n-1] , 1,dp,arr)

        return dp[n][state] = max(a,b)
    }
}
```

```
else if state = 1 then
{
    a=b=INT_MIN
    a = HELPER(n-1, prev , state,dp,arr)
    if arr[n-1]<prev then
        b = 1+ HELPER(n-1, arr[n-1] , 0,dp,arr)

    return dp[n][state] = max(a,b)
}
else
{
    a=b=c= INT_MIN;
    a = HELPER(n-1, prev , state,dp,arr)
    b = 1+HELPER(n-1, arr[n-1] , 0,dp,arr)
    c = 1+HELPER(n-1, arr[n-1] , 1,dp,arr)
    return dp[n][state] = max(a,max(b,c))
}
```

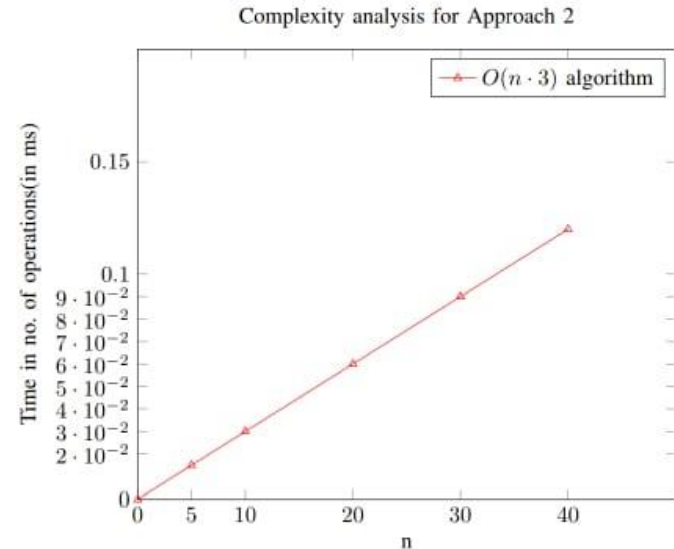
Time Complexity and Space Complexity Analysis

Time Complexity Analysis

The time complexity will be $O(n \cdot 3)$ because we are in a way doing memoization our approach 1 code and saving time by using values of the precalculated subproblems.

Space Complexity Analysis

The space complexity will be $O(n)$ for input array and $O(n \cdot 3)$ for storing the values of each condition by dynamic programming.



CONCLUSION

Above two methods have different time and space complexities and meet to fulfill the problem statement. The order in which they are good can be listed as:

I. Approach 2

II. Approach 1

Based on the time complexities and space complexities.

REFERENCES

Utkarsh Trivedi, '[Longest Zig-Zag Subsequence](#)', [GeeksforGeeks](#), 2018. [Online].
[Accessed: 27-Mar-2021]