$t, \kappa \in \mathbb{R}, x, \mu \in \mathbb{R}^n \ (x, \mu \ are \ a \ column \ vectors), G \in \mathbb{R}^{nXn}$

$$f(x) = -tx^{T}\mu + t\kappa x^{T}Gx - \sum_{i=1}^{n} log(x_{i}) =$$

$$-t \begin{bmatrix} x_{1} & \cdots & x_{n} \end{bmatrix} \begin{bmatrix} \mu_{1} \\ \vdots \\ \mu_{n} \end{bmatrix} + t\kappa \begin{bmatrix} x_{1} & \cdots & x_{n} \end{bmatrix} \begin{bmatrix} g_{11} & \cdots & g_{1n} \\ \vdots & \ddots & \vdots \\ g_{n1} & \cdots & g_{nn} \end{bmatrix} \begin{bmatrix} x_{1} \\ \vdots \\ x_{n} \end{bmatrix} - \sum_{i=1}^{n} log(x_{i}) =$$

$$-t(\mu_{1}x_{1} + \dots + \mu_{n}x_{n}) + t\kappa \begin{bmatrix} g_{11}x_{1} + \dots + g_{n1}x_{n} & \cdots & g_{1n}x_{1} + \dots + g_{nn}x_{n} \end{bmatrix} \begin{bmatrix} x_{1} \\ \vdots \\ x_{n} \end{bmatrix} - \sum_{i=1}^{n} log(x_{i}) =$$

$$-t(\mu_{1}x_{1} + \dots + \mu_{n}x_{n}) + t\kappa((x_{1}(g_{11}x_{1} + \dots + g_{n1}x_{n}) + \dots + x_{n}(g_{1n}x_{1} + \dots + g_{nn}x_{n})) - \sum_{i=1}^{n} log(x_{i})$$

First derivative

$$\nabla f(x) = \begin{bmatrix} \frac{\partial f}{\partial x_1} \\ \vdots \\ \frac{\partial f}{\partial x_n} \end{bmatrix} = \begin{bmatrix} -t\mu_1 + t\kappa((2g_{11}x_1 + \dots + g_{n1}x_n) + g_{12}x_2 + \dots + g_{1n}x_n) - \frac{1}{x_1} \\ \vdots \\ -t\mu_n + t\kappa(g_{n1}x_1 + g_{n1}x_2 + \dots + (g_{1n}x_1 + \dots + 2g_{nn}x_n)) - \frac{1}{x_n} \end{bmatrix}$$

Second derivative

$$\nabla^{2}f(x) = \begin{bmatrix} \frac{\partial^{2}f}{\partial x_{1}^{2}} & \frac{\partial^{2}f}{\partial x_{1}\partial x_{2}} & \cdots & \frac{\partial^{2}f}{\partial x_{1}\partial x_{n}} \\ \frac{\partial^{2}f}{\partial x_{2}\partial x_{1}} & \frac{\partial^{2}f}{\partial x_{2}\partial x} & \cdots & \frac{\partial^{2}f}{\partial x_{2}\partial x_{n}} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{\partial^{2}f}{\partial x_{n}\partial x_{1}} & \frac{\partial^{2}f}{\partial x_{n}\partial x_{2}} & \cdots & \frac{\partial^{2}f}{\partial x_{n}^{2}} \end{bmatrix} = \begin{bmatrix} 2t\kappa g_{11} + \frac{1}{x_{1}^{2}} & t\kappa g_{21} + g_{12} & \cdots & t\kappa g_{n1} + g_{1n} \\ t\kappa g_{21} + g_{12} & 2t\kappa g_{22} + \frac{1}{x_{2}^{2}} & \cdots & \frac{\partial^{2}f}{\partial x_{2}\partial x_{n}} \\ \vdots & \vdots & \ddots & \vdots \\ t\kappa g_{n1} + g_{1n} & \frac{\partial^{2}f}{\partial x_{n}\partial x_{2}} & \cdots & 2t\kappa g_{nn} + \frac{1}{x_{n}^{2}} \end{bmatrix}$$

$$(g \ is \ symmetric) = \begin{bmatrix} 2t\kappa g_{11} + \frac{1}{x_{1}^{2}} & \cdots & 2t\kappa g_{n1} \\ \vdots & \ddots & \vdots \\ 2t\kappa g_{n1} & \cdots & 2t\kappa g_{nn} + \frac{1}{x_{n}^{2}} \end{bmatrix}$$