

NCERT Solutions for Class 9

Mathematics

Chapter 4-Linear Equations in Two Variables

Exercise 4.1

1. Construct a linear equation in two variables to express the following statement.

The cost of a textbook is twice the cost of an exercise book.

Ans: Let the cost of a textbook be x rupees and the cost of an exercise book be y rupees.

The given statement: Cost of Notebook is twice the cost of Pen.

So, in order to form a linear equation,

the cost of the textbook $=2\times$ the cost of an exercise book.

$$\Rightarrow$$
 x=2y

$$\Rightarrow$$
 x-2y=0.

2. Determine the values of a, b, c from the following linear equations by expressing each of them in the standard form ax+by+c=0.

(i)
$$2x+3y=9.\overline{35}$$

Ans: The given linear equation is

$$2x+3y=9.\overline{35}$$

Subtracting 9.35 from both sides of the equation gives

$$2x+3y-9.\overline{35}=0$$

Now, by comparing the above equation with the standard form of the linear equation, ax+by+c=0, the values of a,b, and c are obtained as

$$a=2$$
.

$$b=3$$
, and



$$c = -9.\overline{35}$$

(ii)
$$x - \frac{y}{5} - 10 = 0$$

Ans: The given linear equation is

$$x - \frac{y}{5} - 10 = 0$$

Now, by comparing the above equation with the standard form of the linear equation, ax+by+c=0, the values of a,b, and c are obtained as

$$a = 1$$
,

$$b = -\frac{1}{5}$$
, and

$$c = -10$$
.

(iii)
$$-2x+3y=6$$

Ans: The given linear equation is

$$-2x+3y=6$$

Subtracting 6 from both sides of the equation gives

$$-2x+3y-6=0$$

Now, by comparing the above equation with the standard form of the linear equation, ax+by+c=0, the values of a,b, and c are obtained as

$$a = -2$$
,

$$b=3$$
, and

$$c = -6$$
.

$$(iv) x=3y$$

Ans: The given linear equation can be written as

$$1x = 3y$$

Subtracting 3y from both sides of the equation gives



$$1x-3y+0=0$$

Now, by comparing the above equation with the standard form of the linear equation ax+by+c=0, the values of a,b, and c are obtained as

$$a = 1$$
,

$$b = -3$$
, and

$$c = 0$$
.

(v)
$$2x = -5y$$

Ans: The given linear equation is

$$2x = -5y$$
.

Adding 5y on both sides of the equation gives

$$2x+5y+0=0$$
.

Now, by comparing the above equation with the standard form of the linear equation, ax+by+c=0, the values of a,b, and c are obtained as

$$a=2$$
,

$$b=5$$
, and

$$c = 0$$
.

(vi) 3x+2=0

Ans: The given linear equation is

$$3x+2=0$$
.

Rewriting the equation gives

$$3x+0y+2=0$$

Now, by comparing the above equation with the standard form of linear equation ax+by+c=0, the values of a,b, and c are obtained as

$$a=3$$
,

$$b=0$$
, and

$$c = 2$$
.



(vii) y-2=0

Ans: The given linear equation is

$$y-2=0$$

The equation can be expressed as

$$0x+1y-2=0$$

Now, by comparing the above equation with the standard form of the linear equation, ax+by+c=0, the values of a,b, and c are obtained as

$$a = 0$$
,

$$b=1$$
, and

$$c = -2$$
.

(viii) 5=2x

Ans: The given linear equation is

$$5=2x$$
.

The equation can be written as

$$-2x+0y+5=0$$
.

Now, by comparing the above equation with the standard form of the linear equation ax+by+c=0, the values of a,b, and c are obtained as

$$a = -2$$
,

$$b=0$$
, and

$$c = 5$$
.

Exercise 4.2

1. Complete the following statement by choosing the appropriate answer and explain why it should be chosen?

- (a) A unique solution,
- (b) Only two solutions,



(c) Infinitely many solutions.

Ans: Observe that, y = 3x+5 is a linear equation.

Now, note that, for x = 0, y = 0 + 5 = 5.

So, (0,5) is a solution of the given equation.

If x=1, then $y = 3 \times 1 + 5 = 8$.

That is, (1,8) is another solution of the equation.

Again, when y = 0, $x = -\frac{5}{3}$.

Therefore, $\left(-\frac{5}{3},0\right)$ is another solution of the equation.

Thus, it is noticed that for different values of x and y, different solutions are obtained for the given equation.

So, there are countless different solutions exist for the given linear equation in two variables. Therefore, a linear equation in two variables has infinitely many solutions.

Hence, option (c) is the correct answer.

2. Determine any four solutions for each of equations given below.

(i)
$$2x + y = 7$$
.

Ans: The given equation

2x+y=7 is a linear equation.

Solving the equation for y gives

$$y=7-2x$$
.

Now substitute x=0,1,2,3 in succession into the above equation.

For x=0,

$$2(0)+y=7$$

$$\Rightarrow$$
 y=7



So, one of the solutions obtained is (x,y)=(0,7).

For x=1,

$$2(1)+y=7$$

$$\Rightarrow$$
 y=5

Therefore, another solution obtained is (x,y)=(1,5).

For x=2,

$$2(2)+y=7$$

$$\Rightarrow$$
 y=3

That is, a solution obtained is (x,y)=(3,1).

Also, for x=3,

$$2(3)+y=7$$

$$\Rightarrow$$
 y=1

So, another one solution is (x,y)=(3,1).

Thus, four solutions obtained for the given equations are (0,7), (1,5), (2,3), (3,1).

(ii)
$$\pi x + y = 9$$
.

Ans: The given equation

$$\pi x + y = 9 \dots (a)$$

is a linear equation in two variables.

By transposing, the above equation (a) can be written as

$$y=9-\pi x$$
.

Now substitute x=0,1,2,3 in succession into the above equation.

For x=0,

$$y=9-\pi(0)$$



$$\Rightarrow$$
 y=9

Therefore, one of the solutions obtained is (x,y)=(0,9).

For x=1,

$$y = 9 - \pi(1)$$

$$\Rightarrow$$
 y = 9 - π .

So, another solution obtained is $(x,y)=(1,9-\pi)$.

For x=2,

$$y = 9 - \pi(2)$$

$$\Rightarrow$$
 y = 9 - 2 π

That is, another solution obtained is $(x,y)=(2,9-2\pi)$.

Also, for x=3,

$$y = 9 - \pi(3)$$

$$\Rightarrow$$
 y = 9 - 3 π .

Therefore, another one solution is $(x,y)=(3,9-3\pi)$.

Thus, four solutions obtained for the given equations are (0,9), $(1,9,-\pi)$, $(2,9-2\pi)$, $(3,9-3\pi)$.

(iii)
$$x = 4y$$
.

Ans: The given equation

x=4y is a linear equation in two variables.

By transposing, the above equation can be written as

$$y=\frac{x}{4}$$
.

Now substitute x=0,1,2,3 in succession into the above equation.

For x=0,



$$y = \frac{0}{4} = 0$$
.

Therefore, one of the solutions is (x,y)=(0,0).

For x = 1,

$$y = \frac{1}{4}$$
.

So, another solution of the given equation is $(x,y) = \left(1, \frac{1}{4}\right)$.

For x=2,

$$y = \frac{2}{4} = \frac{1}{2}$$
.

That is, another solution obtained is $(x,y) = \left(2, \frac{1}{2}\right)$.

Also, for x=3,

$$y = \frac{3}{4}$$
.

Therefore, another one solution is $(x,y) = (3,\frac{3}{4})$.

Thus, four solutions obtained for the given equations are (0,0), $\left(1,\frac{1}{4}\right)$, $\left(2,\frac{1}{2}\right)$, $\left(3,\frac{3}{4}\right)$.

3. Identify the actual solutions of the linear equation x-2y=4 from each of the following solutions.

(i) (0,2)

Ans: Substituting x=0 and y=2 in the Left-hand-side of the equation x-2y=4 gives



$$x-2y = 0 - 2(2)$$
$$= -4$$
$$\neq 4.$$

Therefore, Left-hand-side is not equal Right-hand-side of the given equation for (x,y)=(0,2).

Hence, (0,2) is not a solution of the equation x-2y=4.

(ii)
$$(2,0)$$

Ans: Substituting x=2 and y=0 in the Left-hand-side of the equation x-2y=4 gives

$$x-2y = 2 - 2(0)$$

$$= 2$$

$$\neq 4$$

Therefore, Left-hand-side is not equal Right-hand-side of the given equation for (x,y)=(2,0).

Hence, (2,0) is not a solution of the equation x-2y=4.

(iii)
$$(4,0)$$

Ans: Substituting x=4 and y=0 in the Left-hand-side of the equation x-2y=4 gives

$$x-2y = 4-2(0)$$

= 4.

Therefore, Left-hand-side is equal Right-hand-side of the given equation for (x,y)=(4,0).

Hence, (4,0) is a solution of the equation x-2y=4.

(iv)
$$(\sqrt{2}, 4\sqrt{2})$$

Ans: Substituting $x=\sqrt{2}$ and $y=4\sqrt{2}$ in the Left-hand-side of the equation x-2y=4 gives



$$x-2y = \sqrt{2} - 2(4\sqrt{2})$$
$$= \sqrt{2} - 8\sqrt{2}$$
$$= -7\sqrt{2}$$
$$\neq 4.$$

Therefore, Left-hand-side is not equal Right-hand-side of the given equation for $(x,y) = (\sqrt{2}, 4\sqrt{2})$.

Hence, $(\sqrt{2}, 4\sqrt{2})$ is not a solution of the equation x-2y=4.

$$(v)$$
 $(1,1)$

Ans: Substituting x = 1 and y = 1 in the Left-hand-side of the equation x-2y=4 gives

$$x-2y = 1 - 2(1)$$

$$= 1 - 2$$

$$= -1$$

$$\neq 4.$$

Therefore, Left-hand-side is not equal Right-hand-side of the given equation for (x,y)=(1,1).

Hence, (1,1) is not a solution of the equation x-2y=4.

4. If (x,y)=(2,1) is a solution of the equation 2x+3y=k, then what is the value of k?

Ans: By substituting x = 2, y = 1 and into the equation

$$2x+3y=k$$
 gives

$$2(2)+3(1)=k$$

$$\Rightarrow 4+3=k$$

 \Rightarrow k=7.

Hence, the value of k is 7.



Exercise 4.3

1. Graph each of the linear equations given below.

$$(i)$$
 $x+y=4$

Ans: The given linear equation is

$$x+y=4$$

$$\Rightarrow$$
 y=4-x (a)

Substitute x = 0 into the equation (a) gives

$$y = 4 - 0 = 4$$
.

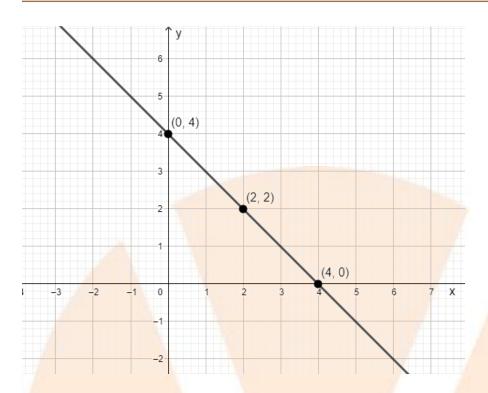
Similarly, substituting x = 2,4 in succession into the equation (a), the following table of y -values are obtained:

X	0	2	4
y	4	2	0

Now, Plot the points (0,4), (2,2) and (4,0) on a graph paper and connect the points by a straight line.

Thus, the following graph of the straight line represents the required graph of the linear equation x+y=4.





(ii)
$$x-y=2$$

Ans: The given linear equation is

$$x-y=2$$

$$\Rightarrow$$
 y = x - 2 (a)

Substitute x = 0 into the equation (a) gives

$$y = 0 - 2 = -2$$
.

Similarly, substituting x = 2,4 in succession into the equation (a), the following table of y -values are obtained:

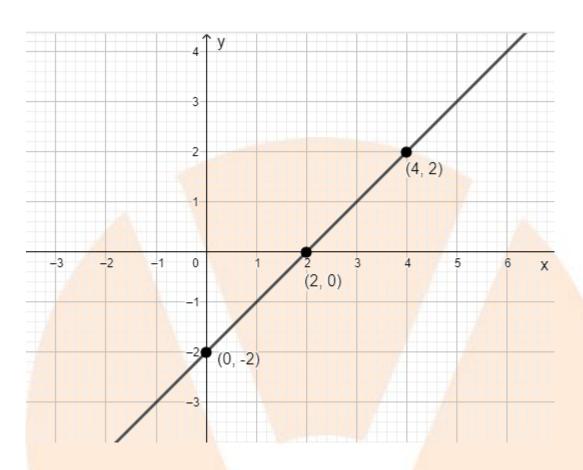
X	0	2	4
y	-2	0	2

Now, Plot the points (0,-2), (2,0) and (4,2) on a graph paper and connect the points by a straight line.

Thus, the following graph of the straight line represents the required graph of the linear equation x-y=2.



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(iii) y=3x

Ans: The given linear equation is

$$y = 3x (a)$$

Substitute x = 0 into the equation (a) gives

$$y = 3(0) = 0.$$

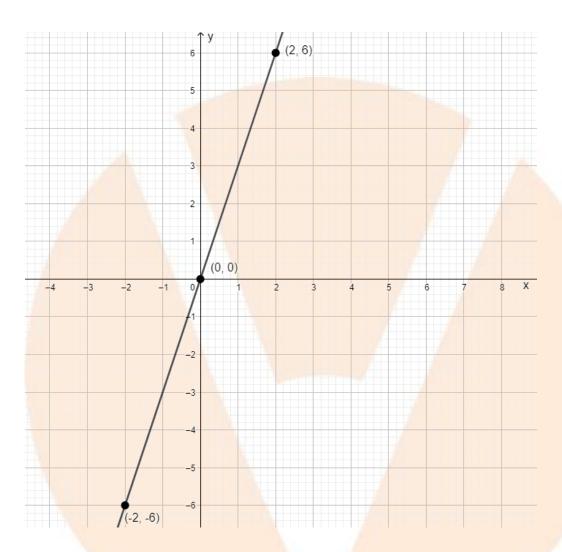
Similarly, substituting x = 2, -2 in succession into the equation (a), the following table of y -values are obtained:

X	0	2	-2
y	0	6	-6

Now, Plot the points (0,0), (2,6) and (-2,-6) on a graph paper and connect the points by a straight line.



Thus, the following graph of the straight line represents the required graph of the linear equation y = 3x.



(iv)
$$3=2x+y$$

Ans: The given linear equation is

$$3 = 2x + y$$

$$\Rightarrow$$
 y = 3 - 2x (a)

Substitute x = 0 into the equation (a) gives

$$y = 3 - 2(0) = 3$$
.

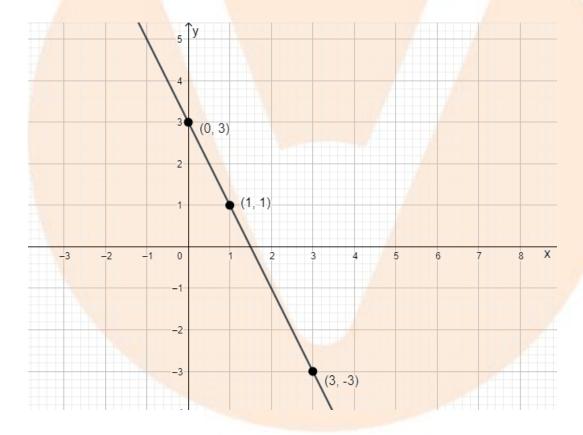


Similarly, substituting x = 1,3 in succession into the equation (a), the following table of y -values are obtained:

X	0	1	3
y	3	1	-3

Now, Plot the points (0,3), (1,1) and (3,-3) on a graph paper and connect the points by a straight line.

Thus, the following graph of the straight line represents the required graph of the linear equation 3 = 2x + y.



2. Provided that the equations of two lines passing through the point (2,14)

. Can there exist more than two equations of such type? If it is, then state the reason.

Ans: Provided that equations of two lines passing through (2,14).



It can be noted that the point (2,14) satisfies the equation 7x-y=0 and x-y+12=0.

So, the equations 7x-y=0 and x-y+12=0 represent two lines passing through point (2,14).

Now, since we know that through infinite number of lines can pass through any one point, so, there are infinite number such type of lines exist that passes through the point (2,14).

Hence, there exist more than two equations whose graph passes through the point (2,14).

3. Determine the value of a in the linear equation 3y=ax+7 if the point (3,4) lies on the graph of the equation.

Ans: Given that 3y=ax+7 is a linear equation and the point (3,4) lies on the equation.

Substituting x=3, y=4 in the equation gives

$$3y=ax+7$$

$$\Rightarrow$$
 3(4)=a(3)+7

$$\Rightarrow$$
 3a = 5

$$\Rightarrow$$
 a = $\frac{5}{3}$.

Hence, the value of a is $\frac{5}{3}$.

4. Derive a linear equation for the following situation:

For the first kilometre, a cab take rent 8 rupees and for the subsequent distances it becomes 5 rupees per kilometre. Assume the distance covered is x km and total rent is y rupees. Hence, draw the graph of the linear equation.

Ans: Let the total distance covered = x km



and the total cost for the distance travelled = y rupees.

It is given that the rent for 1st kilometre is 8 rupees and for the subsequent km, it is 5 rupees per kilometre.

Therefore, rent for the rest of the distance = (x-1)5 rupees.

Total cost for travelling x km is given by

$$y = [8 + (x-1)5]$$

$$\Rightarrow$$
 y=8+5x-5

$$\Rightarrow$$
 y=5x+3.....(1)

$$\Rightarrow$$
 5x-y+3=0,

which is the required linear equation.

Now, substituting x = 0 into the equation (1) gives

$$y = 5(0) + 3 = 3$$
.

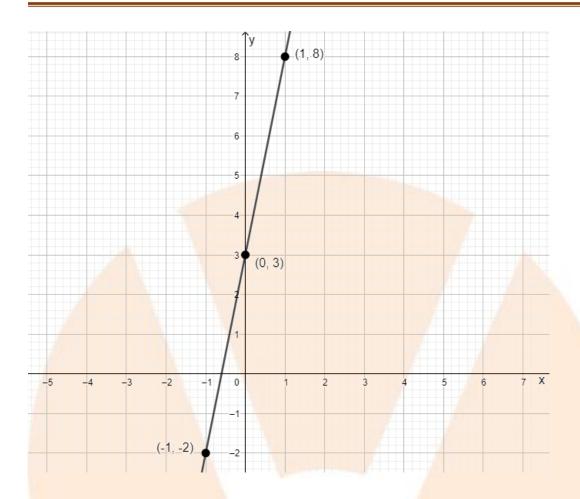
Similarly, substituting x = 1,-1 in succession into the equation (1), the following table of y -values are obtained:

X	0	1	-1
У	3	8	-2

Now, Plot the points (0,3), (1,8) and (-1,-2) on a graph paper and connect the points by a straight line.

Thus, the following graph of the straight line represents the required graph of the linear equation 5x-y+3=0.





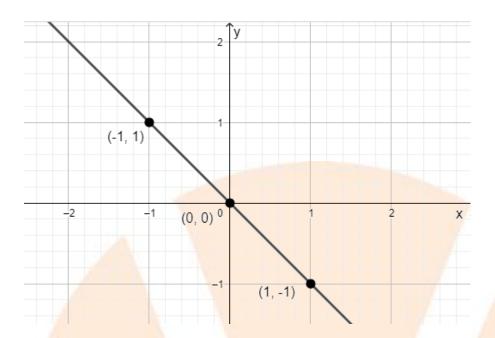
It is concluded by observing the graph of the linear equations that the variable x and y represent the distance travelled by the car and the total cost of rent for the distance respectively. Therefore, x and y are non-negative quantities.

Thus, only the first quadrant of the graph of the linear equation 5x-y+3=0 is only valid.

5. Choose the correct linear equation for the given graphs in (a) and (b).

- (a) (i) y = x
 - (ii) x + y = 0
 - (iii) y = 2x
 - (iv) 2 + 3y = 7x





Ans: It is observed in the given graph that the points (-1,1), (0,0), and (1,-1) lie on the straight line. Also, the coordinates of the points satisfy the equation x+y=0.

So, x+y=0 is the required linear equation corresponding to the given graph.

Hence, option (ii) is the correct answer

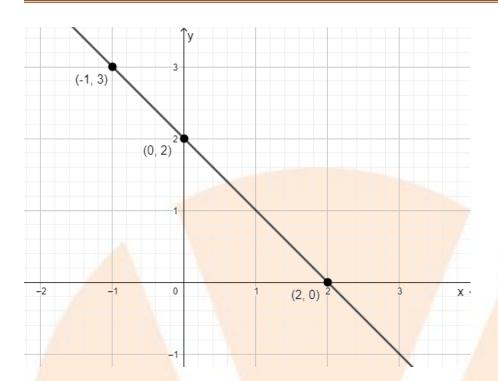
(b) (i)
$$y = x + 2$$

(ii)
$$y = x - 2$$

(iii)
$$y = -x + 2$$

$$(iv) x + 2y = 6$$





Ans: It is observed in the given graph that the points (-1,3), (0,2), and (2,0) lie on the straight line. Also, the coordinates of the points satisfy the equation y = -x+2.

So, y = -x+2 is the required linear equation corresponding to the given graph. Hence, option (iii) is the correct answer.

- 6. The work done by a body on the application of a constant force is proportional to the distance moved by the body. Formulate this relation by a linear equation and graph the same by using a constant force of five units. Hence from the graph, determine the work done when the distance moved by the body is
- (i) 2 units
- (ii) 0 unit.

Ans: Let the distance moved by the body be x units and the work done be y units.

Now, given that, work done is proportional to the distance.

Therefore, $y \propto x$.

$$\Rightarrow$$
 y = kx,..... (a)



where, k is a constant.

By considering constant force of five units, the equation (a) becomes

$$y = 5x(b)$$

Now, substituting x = 0 into the equation (b) gives

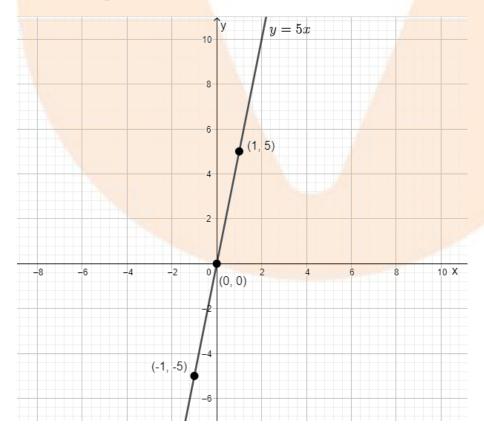
$$y = 5(0) = 0$$
.

Similarly, substituting x = 1,-1 in succession into the equation (b), gives the following table of y-values.

X	0	1	-1
У	0	5	-5

Now, Plot the points (0,0), (1,5) and (-1,-5) on a graph paper and connect the points by a straight line.

Thus, the following graph of the straight line represents the required graph of the linear equation y = 5x.





It can be concluded by observing the graph of the linear equation that the value of y corresponding to x=2 is 10. Thus, when the distance moved by the body is 2 units, then the work done by it is 10 units.

Also, the value of y corresponding to x=0 is 0. So, when the distance travelled by the body is 0 unit, then the work done by it is 0 unit.

7. Derive a linear equation that satisfies the following data and graph it. Sujata and Suhana, two students of Class X of a school, together donated 100 rupees to the Prime Minister's Relief Fund for supporting the flood victims.

Ans: Let Sujata and Suhana donated x rupees and y rupees respectively to the Prime Minister's Relief fund.

Given that, the amount donated by Sujata and Suhana together is 100 rupees.

Therefore, x+y=100.

$$\Rightarrow$$
 y = 100 - x (a)

Now, substituting x = 0 into the equation (a) gives

$$y = 100 - 0 = 100$$
.

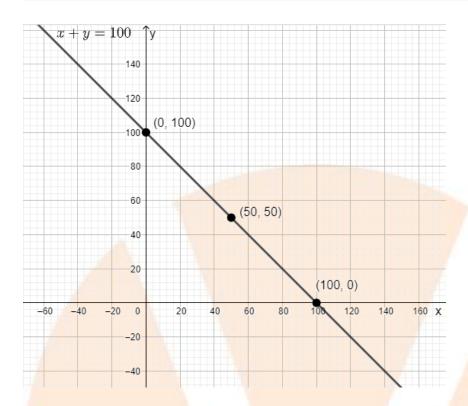
Similarly, substituting x = 50,100 in succession into the equation (a), gives the following table of y-values.

X	0	50	100
У	100	50	0

Now, Plot the points (0,100), (50,50) and (100,0) on a graph paper and connect the points by a straight line.

Thus, the following graph of the straight line represents the required graph of the linear equation x+y=100.





It is concluded by observing the graph of the linear equation that the variable x and y are showing the amount donated by Sujata and Suhana respectively and so, x and y are nonnegative quantities.

Hence, the values of x and y lying in the first quadrant will only be considered.

8. The following linear equation converts Fahrenheit to Celsius:

$$\mathbf{F} = \left(\frac{9}{5}\right)\mathbf{C} + 32,$$

where F denotes the measurement of temperature in Fahrenheit and C in Celsius unit.

Then do as directed in the following questions.

(i) Graph the linear equation given above by taking x -axis as Celsius and y -axis as Fahrenheit.

Ans: The given linear equation is

$$F = \left(\frac{9}{5}\right) C + 32 \dots (a)$$



Now, substituting C = 0 into the equation (a) gives

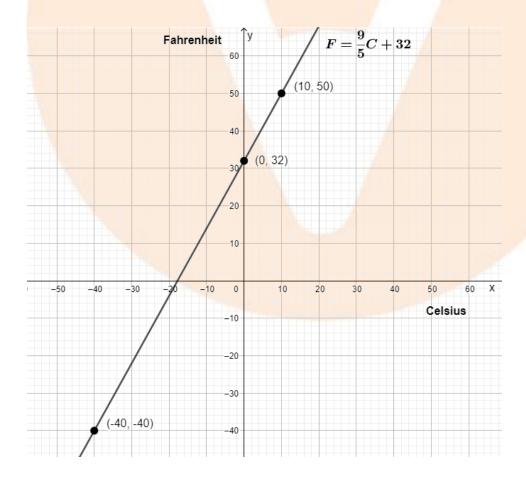
$$F = \left(\frac{9}{5}\right)(0) + 32 = 32.$$

Similarly, substituting C = -40,10 in succession into the equation (a) gives the following table of F-values.

С	0	-40	10
F	32	-40	50

Now, Plot the points (0,32), (-40,-40) and (10,50) on a graph paper and connect the points by a straight line.

Thus, the following graph of the straight line represents the required graph of the linear equation $F = \left(\frac{9}{5}\right)C + 32$.





(ii) Determine the temperature in Fahrenheit if it is 30°C in Celsius.

Ans: Given that the temperature $=30^{\circ}$ C.

Now, it is also provided that, $F = \left(\frac{9}{5}\right)C + 32$.

Substitute C = 32, in the above linear equation.

Then,

$$F = \left(\frac{9}{5}\right) 30 + 32 = 54 + 32 = 86$$
.

Hence, the temperature in Fahrenheit obtained is 86 °F.

(iii) Determine the temperature in Celsius if it is 95°F in Fahrenheit.

Ans: The given temperature $=95^{\circ}F$.

It is provided that,
$$F = \left(\frac{9}{5}\right) C + 32$$

Now, substitute F=95, into the above linear equation.

Then it gives

$$95 = \left(\frac{9}{5}\right) C + 32$$

$$\Rightarrow$$
 63= $\left(\frac{9}{5}\right)$ C

$$\Rightarrow$$
 C = 35.

Hence, the temperature in Celsius obtained is 35°C.

(iv) Calculate the temperature in Fahrenheit when it is 0°C in Celsius.

Also, determine the temperature in Celsius when it is 0°F in Fahrenheit.

Ans: It is known that,



$$F = \left(\frac{9}{5}\right) c + 32....(a)$$

Now, substituting C = 0 in the above linear equation gives,

$$F = \left(\frac{9}{5}\right)(0) + 32 = 32.$$

So, if $C = 0^{\circ}C$, then $F = 32^{\circ}F$.

Again, substituting F=0 into the equation (a) gives

$$0 = \left(\frac{9}{5}\right) C + 32$$

$$\Rightarrow \left(\frac{9}{5}\right) C = -32$$

$$\Rightarrow C = \frac{-160}{9} = -17.77$$

Hence, if $F = 0^{\circ}F$, then $C = -17.8^{\circ}C$.

(v) Does there exist a temperature that numerically gives the same value in both Fahrenheit and Celsius? If it is, then show it.

Ans: It is provided that,

$$F = \left(\frac{9}{5}\right) c + 32$$
.

Let assume that F=C.

Then,

$$F = \left(\frac{9}{5}\right)F + 32$$

$$\Rightarrow \left(\frac{9}{5} - 1\right) F + 32 = 0$$

$$\Rightarrow \left(\frac{4}{5}\right) F = -32$$



$$\Rightarrow$$
 F = -40.

Yes, there exists a temperature -40° that gives numerically the same value in both Fahrenheit and Celsius.

Exercise 4.4

1. Describe the geometric representation of y=3 as an equation

(i) in one variable

Ans: The given equation is y=3.

Note that, when y=3 is considered as an equation in one variable, then actually it represents a number in the one-dimensional number line as shown in following figure.



(ii) in two variables.

Ans: The given equation is y=3.

The above equation can be written as 0.x+y=0.

Note that when y=3 is considered in two variables, then it represents a straight line passing through point (0,3) and parallel to the x-axis. Therefore, all the points in the graph having the y-coordinate as 3, contained in the collection.

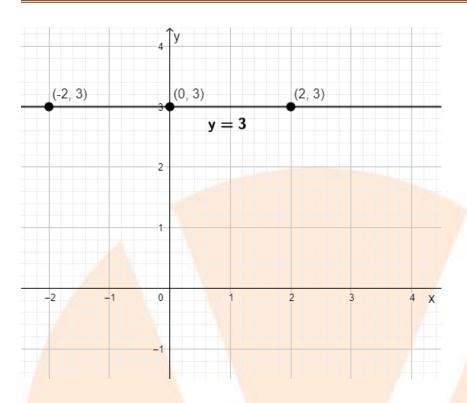
Hence, at x=0, y=3;

at
$$x=2$$
, $y=3$; and

at x = -2, y=3 are the solutions for the given equation.

Now, Plot the points (0,3), (2,3) and (-2,3) on a graph paper and connect the points by a straight line. The graphical representation is shown below:





2. Give the geometric representations of 2x+9=0 as an equation

(i) in one variable

Ans: The given equation is 2x+9=0.

Now, the equation can be written as

$$2x+9=0$$

$$\Rightarrow$$
 2x=9

$$\Rightarrow x = \frac{-9}{2} = -4.5$$

Hence, when 2x+9=0 is considered as an equation in one variable, then actually it represents a number x=-4.5 in the one-dimensional number line as shown in following figure





(ii) in two variables

Ans: The given equation is 2x+9=0.

The above equation can be written as 2x+0y=-9.

Note that when 2x+9=0 is considered in two variables, then it represents a straight line passing through point (-4.5,0) and parallel to the y-axis.

Therefore, all the points in the graph having the x-coordinate as -4.5, contained in the collection.

Hence, at y=3, x = -4.5;

at
$$y = -1$$
, $x = -4.5$; and

at y = 1, x = -4.5 are the solutions for the given equation.

Now, Plot the points (-4.5,3), (-4.5,-1) and (-4.5,1) on a graph paper and connect the points by a straight line. The graphical representation is shown below:

