



**INDIAN INSTITUTE OF INFORMATION TECHNOLOGY  
DESIGN AND MANUFACTURING KANCHEEPURAM**

LAB ASSIGNMENT 3 - REPORT  
ON  
ADDITION OF N NUMBERS AND VECTOR DOT PRODUCT  
USING REDUCTION AND CRITICAL SECTION FOR BOTH

SUBMITTED BY  
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TO  
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## **Specifications : -**

Cpu processor - Intel core i5-7200 CPU @ 2.50GHz

L1d cache:	64 KiB
L1i cache:	64 KiB
L2 cache:	512 KiB
L3 cache:	3 MiB

Thread(s) per core: 2

Core(s) per socket: 2

Socket(s): 1

So number of physical cores =  $2 * 1 = 2$

And number of logical cores =  $2 * 2 * 1 = 4$

## **Observation : -**

For all the questions, i have taken number of iterations as  $10^7$  and **question1a** and **question1b** was taking around 1-2 minutes while **question2a** and **question2b** was taking around 3-4 minutes.

These time includes the generation of random numbers as well

# ADDITION OF N NUMBERS

(USING REDUCTION)

## Strategy

In my program for addition of n numbers, the instruction which is running in parallel is **asum = asum + a[i]**

Here i am using reduction method to add these n numbers otherwise it should lead to racing conditions and thus should give wrong results. Due to reduction, the value of asum is not shared by all the threads and thus it gives the right result.

For example - suppose thread1 has to execute for iteration 1 to 10, then asum is only shared with iteration 1 to 10 not others. Also it is not shared with other threads to avoid racing conditions.

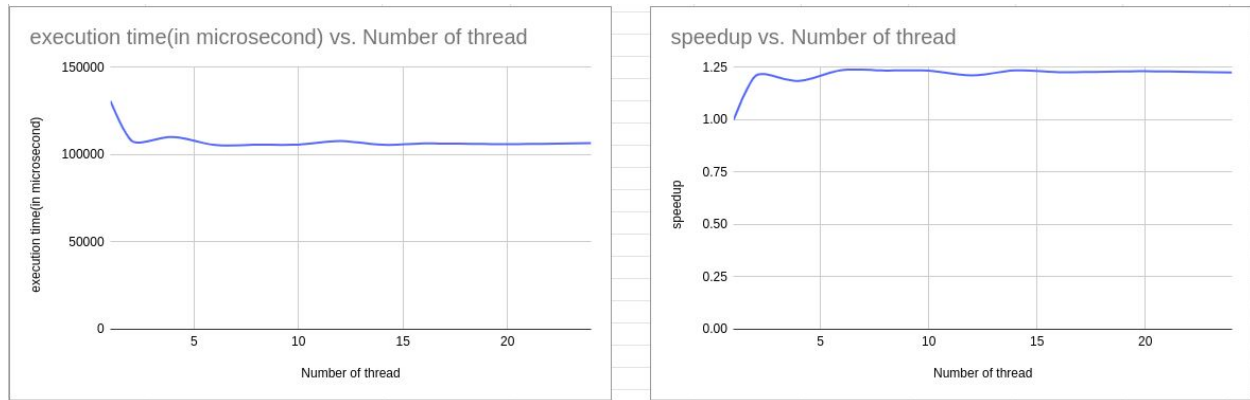
Instead of running the program serially, we can distribute the task of adding n elements among the threads so that my program could run parallelly and in turn save the execution time.

Therefore , in #pragma omp parallel block , for loop consists of these granular instructions. We also have shared a,b and c to run the program in parallel.

## Graph and tables

<https://docs.google.com/spreadsheets/d/1XfX1qzk0ZGUGZaxF76MaZQ9xRs8rBuHHTQx2Kb8HnT8/edit#gid=0>

Number of iterations = 10 <sup>7</sup>				
Number of thread	execution time(in microsecond)	speedup	parallelization fraction(f)	
1	130564	1	0	
2	107992	1.209015483	0.3457614656	
4	110177	1.18503862	0.2081941934	
6	105536	1.237151304	0.2300297172	
8	105724	1.234951383	0.2174303133	
10	105783	1.234262594	0.2108884872	
12	107782	1.211371101	0.1903517885	
14	105646	1.235863166	0.2055296194	
16	106415	1.226932293	0.1972897072	
20	106029	1.231398957	0.1978057948	
24	106576	1.225078817	0.1917140753	



## Calculation of parallelization fraction

$T(1) = 130564$  microseconds

Here , for  $P = 6$  the execution time is minimum

$T(P) = 105536$  microseconds

$$\text{Speedup} = \frac{T(1)}{T(P)} = \frac{130564}{105536} = 1.237151304.$$

From Amdahl's Law,

$$\text{Speedup} = \frac{1}{(f/P) + (1-f)} \text{ Where , } f = \text{Parallelization factor } P = \text{Thread Number}$$

$$\text{So, } f = \frac{(1-T(P)/T(1))}{(1-(1/P))}$$

Therefore,  $f = 0.2300297172$  which means that approx. 23% of the program is parallelizable.

# ADDITION OF N NUMBERS

(USING CRITICAL SECTION)

## Strategy

In my program for addition of n numbers, the instruction which is running in parallel is  
**psum = psum + a[i]**

and **asum = asum + psum** is in critical section.

Here i am using critical section method to add these n numbers otherwise it should lead to racing conditions and thus should give wrong results. Due to critical section, the value of psum is not shared by all the threads and it is used in critical section for finding total psum which is equal to asum and thus it gives the right result.

For example - suppose thread1 has to execute for iteration 1 to 10, then psum is only shared with iteration 1 to 10 not others. Also it is not shared with other threads to avoid racing conditions.

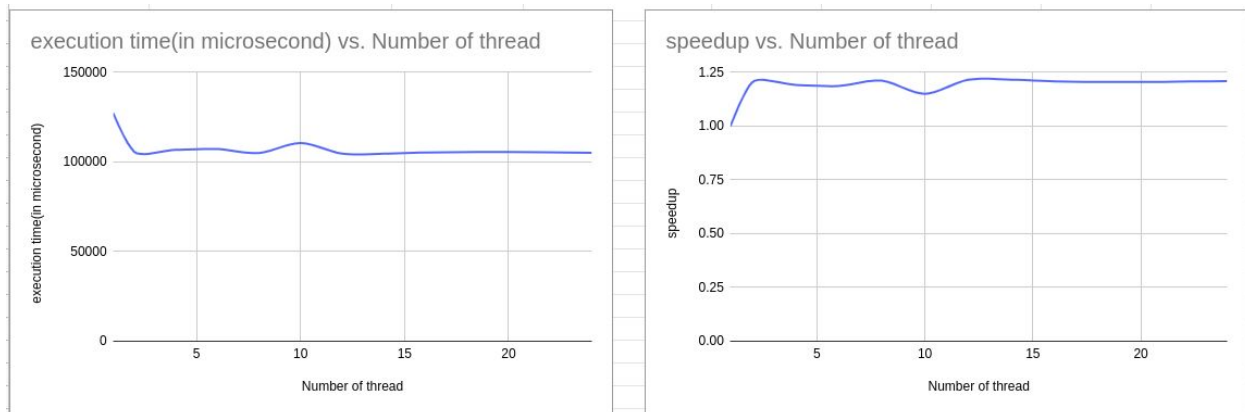
Instead of running the program serially, we can distribute the task of adding n elements among the threads so that my program could run parallelly and in turn save the execution time.

Therefore , in `#pragma omp parallel block` , for loop consists of these granular instructions. We also have shared a,b and c to run the program in parallel.

## Graph and tables

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Number of iterations = 10 <sup>7</sup>			
Number of thread	execution time(in microsecond)	speedup	parallelization fraction(f)
1	127199	1	0
2	105749	1.202838798	0.3372668024
4	106726	1.191827671	0.2146033643
6	107203	1.186524631	0.1886429925
8	105000	1.211419048	0.1994534997
10	110578	1.150310188	0.1451880736
12	104648	1.215493846	0.1934063232
14	104616	1.215865642	0.1911976812
16	105279	1.208208665	0.1838169587
20	105552	1.20508375	0.1791391111
24	105141	1.209794466	0.1809530223



## Calculation of parallelization fraction

$T(1) = 127199$  microseconds

Here , for  $P = 14$  the execution time is minimum

$T(P) = 104616$  microseconds

$$\text{Speedup} = \frac{T(1)}{T(P)} = \frac{127199}{104616} = 1.215865642.$$

From Amdahl's Law,

$$\text{Speedup} = \frac{1}{(f/P) + (1-f)} \text{ Where , } f = \text{Parallelization factor } P = \text{Thread Number}$$

$$\text{So, } f = \frac{(1-T(P)/T(1))}{(1-(1/P))}$$

Therefore,  $f = 0.1911976812$  which means that approx. 19% of the program is parallelizable.

# VECTOR DOT PRODUCT

(USING REDUCTION)

## Strategy

In my program for addition of n numbers, the instruction which is running in parallel is  
**asum = asum + a[i]\*b[i]**

Here i am using reduction method to add these product of a and b otherwise it should lead to racing conditions and thus should give wrong results. Due to reduction, the value of asum is not shared by all the threads and thus it gives the right result.

For example - suppose thread1 has to execute for iteration 1 to 10, then asum is only shared with iteration 1 to 10 not others. Also it is not shared with other threads to avoid racing conditions.

Instead of running the program serially, we can distribute the task of adding n multiplied elements among the threads so that my program could run parallelly and in turn save the execution time.

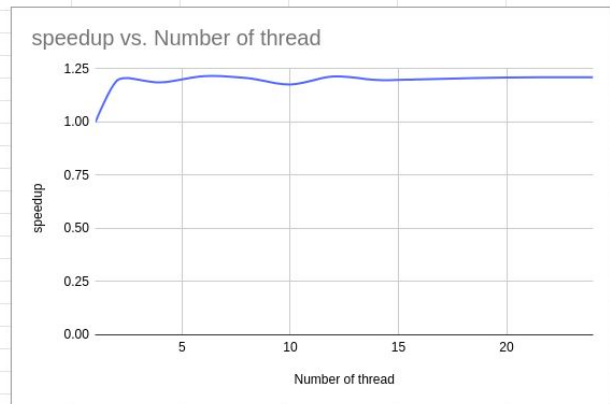
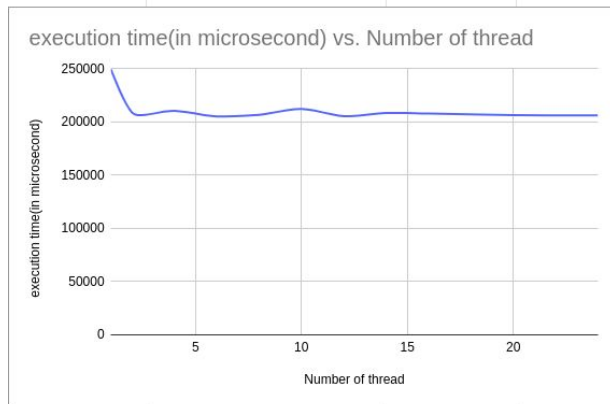
Therefore , in #pragma omp parallel block , for loop consists of these granular instructions. We also have shared a,b and c to run the program in parallel.

## Graph and tables

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**Number of iterations = 10<sup>7</sup>**

Number of thread	execution time(in microsecond)	speedup	parallelization fraction(f)
1	249625	1	0
2	208884	1.195041267	0.3264176264
4	210505	1.185838816	0.2089534301
6	205308	1.215856177	0.2130411617
8	206856	1.206757358	0.1958091423
10	212222	1.176244687	0.1664852835
12	205558	1.214377451	0.1925812355
14	208442	1.197575345	0.1776701976
16	207916	1.200605052	0.1782257386
20	206434	1.209224256	0.1821300372
24	206140	1.21094887	0.1817752716



## Calculation of parallelization fraction

$T(1) = 249625$  microseconds

Here , for  $P = 6$  the execution time is minimum

$T(P) = 205308$  microseconds

$$\text{Speedup} = \frac{T(1)}{T(P)} = \frac{249625}{205308} = 1.215856177.$$

From Amdahl's Law,

$$\text{Speedup} = \frac{1}{(f/P) + (1-f)} \text{ Where , } f = \text{Parallelization factor } P = \text{Thread Number}$$

$$\text{So, } f = \frac{(1-T(P)/T(1))}{(1-(1/P))}$$

Therefore,  $f = 0.2130411617$  which means that approx. 21% of the program is parallelizable.



# VECTOR DOT PRODUCT

(USING CRITICAL SECTION)

## Strategy

In my program for addition of n numbers, the instruction which is running in parallel is

**psum = psum + a[i] \* b[i]**

and **asum = asum + psum** is in critical section.

Here i am using critical section method to add these product of a and b otherwise otherwise it should lead to racing conditions and thus should give wrong results. Due to critical section, the value of psum is not shared by all the threads and it is used in critical section for finding total psum which is equal to asum and thus it gives the right result. For example - suppose thread1 has to execute for iteration 1 to 10, then psum is only shared with iteration 1 to 10 not others. Also it is not shared with other threads to avoid racing conditions.

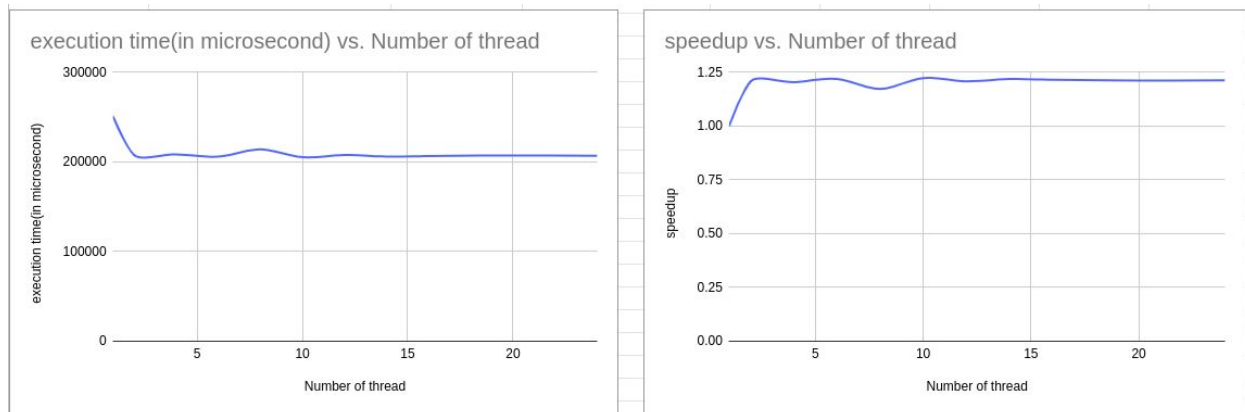
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Therefore , in #pragma omp parallel block , for loop consists of these granular instructions. We also have shared a,b and c to run the program in parallel.

## Graph and tables

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Number of iterations = 10 <sup>7</sup>				
Number of thread	execution time(in microsecond)	speedup	parallelization fraction(f)	
1	251055	1	0	
2	207855	1.207837194	0.3441476967	
4	208401	1.204672722	0.2265320348	
6	205888	1.219376554	0.2158905419	
8	214121	1.172491255	0.1681316274	
10	205234	1.223262228	0.202793102	
12	207781	1.208267358	0.1880384776	
14	205986	1.218796423	0.1933275424	
16	206580	1.215291897	0.1889625779	
20	207203	1.211637862	0.1838640935	
24	206882	1.213517851	0.1835994711	



## Calculation of parallelization fraction

$T(1) = 251055$  microseconds

Here , for  $P = 10$  the execution time is minimum

$T(P) = 205234$  microseconds

$$\text{Speedup} = \frac{T(1)}{T(P)} = \frac{251055}{205234} = 1.223262228.$$

From Amdahl's Law,

$$\text{Speedup} = \frac{1}{(f/P) + (1-f)} \text{ Where , } f = \text{Parallelization factor } P = \text{Thread Number}$$

$$\text{So, } f = \frac{(1-T(P)/T(1))}{(1-(1/P))}$$

Therefore,  $f = 0.202793102$  which means that approx. 20% of the program is parallelizable.