

Code No: 153BT

JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD

B.Tech II Year I Semester Examinations, October - 2020

**SIGNALS AND SYSTEMS**

(Common to ECE, EIE)

Time: 2 hours

Max. Marks: 75

Answer any five questions

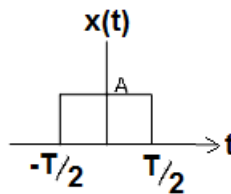
All questions carry equal marks

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- 1.a) Show that  $f(t)$  is orthogonal to signals  $\cos t, \cos 2t, \cos 3t, \dots \cos nt$  for all integer values of  $n, n \neq 0$ , over the interval  $(0, 2\pi)$  if  $x(t) = \begin{cases} 1, & \text{for } 0 < t < \pi \\ -1, & \text{for } \pi < t < 2\pi \end{cases}$
- b) Discover the analogy of vectors and signals in terms of orthogonality. [6+9]
- 2.a) Estimate the mean square error value of a function  $f(t)$ .
- b) Sketch the following signals (i)  $r(t) - r(t-1) - r(t-3) + r(t-4)$  (ii)  $\pi\left(\frac{t-2}{2}\right) + \pi(2t - 3.5)$  [7+8]
- 3.a) Assume that  $T=2$ , determine the Fourier series expansion of the signal shown below figure 1 with amplitude of  $\pm 1$ .

**Figure: 1**

- b) Prove the following properties of the Fourier transform: (i) duality (ii) modulation. [8+7]
- 4.a) Determine the exponential Fourier series from trigonometric Fourier series.
- b) Solve the Fourier transform of the rectangular pulse. [6+9]
- 5.a) Find the convolution of the rectangular pulse given below figure 2 with itself.

**Figure: 2**

- b) Explain causality and physical realizability of a system and give Paley Wiener criterion. [8+7]
- 6.a) A system produces an output of  $y(t) = e^{-t} u(t)$  for an input of  $x(t) = e^{-2t} u(t)$ . Determine the impulse response and frequency response of the system.
- b) Compare the signals and system bandwidth. [9+6]
7. Evaluate the Laplace Transforms of the following functions:  
a) Exponential function      b) Unit step function      c) Damped sine function. [15]
- 8.a) Prove that for a signal, auto correlation and PSD form a Fourier transform pair.
- b) A function  $f(t)$  has a PSD of  $S(w)$ . Find the PSD of i) integral of  $f(t)$  and ii) time derivative of  $f(t)$ . [7+8]