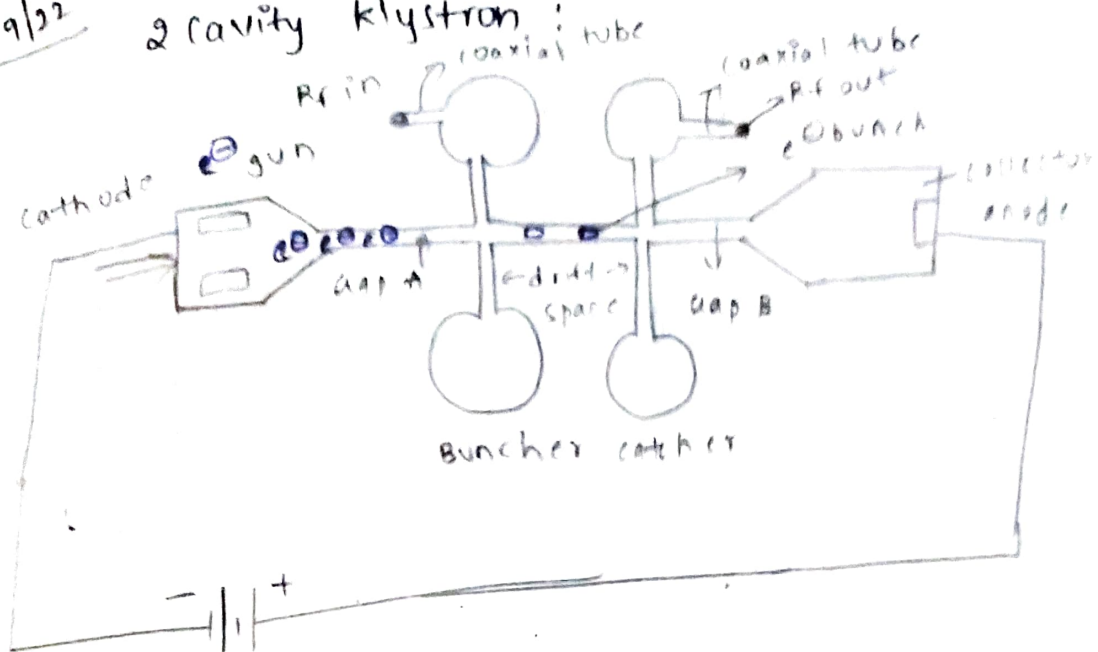
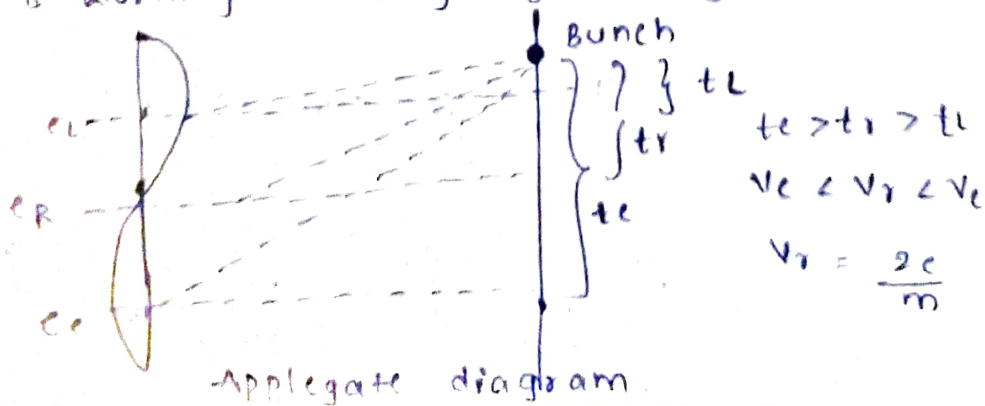


01/09/22

## 2 cavity klystron:



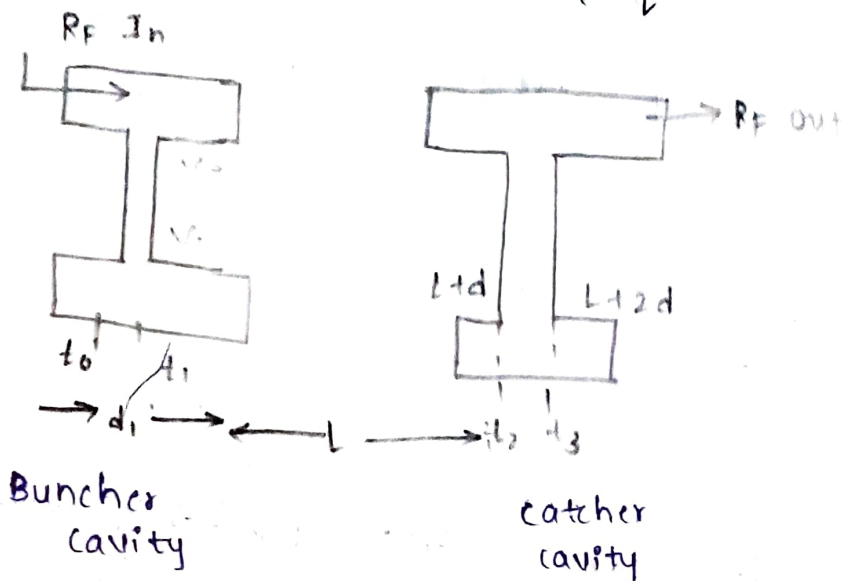
- There are 2 cavities, Buncher & catcher.
- 2 cavity klystron used as amplifier.
- $e^-$  gun emit out electrons,  $e^-$  moves out,
- As the  $e^-$  gun is connected to negative the  $e^-$  starts emitting.
- first electron coming from  $e^-$  gun, is early electron
- Deceleration occurs as the potential is  $\ominus$
- for +ve RF signal, the polarity changes the  $e^-$  accelerates and there is more acceleration
- reference is neither +ve nor -ve, it remains/moves with constant velocity with which it had started
- It is working at very high voltage.



12/09/22

## Cavity klystron amplifier :

Relation between O/P power &  $\eta$  :



Let the dc voltage b/w anode & cathode is  $V_0$ ,  $v_0$  is velocity of electron,  $L$  is length of drift space <sup>where bunching occurs</sup>,  $R_F$  input signal to be amplified by the klystron be  $V_s$

$$v_0 = \sqrt{\frac{2eV_0}{m}} = 5.92 \times 10^5 \sqrt{V_0}$$

$$V_s = (V_s \sin \omega t) \rightarrow \text{ilp signal from buncher cavity}$$

After  $v_0$  distance, the electron is taken from  $v_1$ , then

$$\frac{1}{2} m v_1^2 = e (V_0 + V_s \sin \omega t)$$

$$v_1 = \sqrt{\frac{2e(V_0 + V_s \sin \omega t)}{m}}$$

$$v_1 = \sqrt{\frac{2eV_0}{m}} \sqrt{1 + \frac{V_s}{V_0} \sin \omega t} = \left(1 + \frac{V_s}{V_0} \sin \omega t\right)^{1/2}$$

$$V_1 = V_0 \left( 1 + \frac{V_0}{2V_0} \sin \omega t \right) \rightarrow \text{Velocity modulation}$$

$$\omega t_1 = \omega t_0 + \frac{\theta_g}{2}$$

$\theta_g$  is the phase angle of RF input voltage during which electron is accelerated.

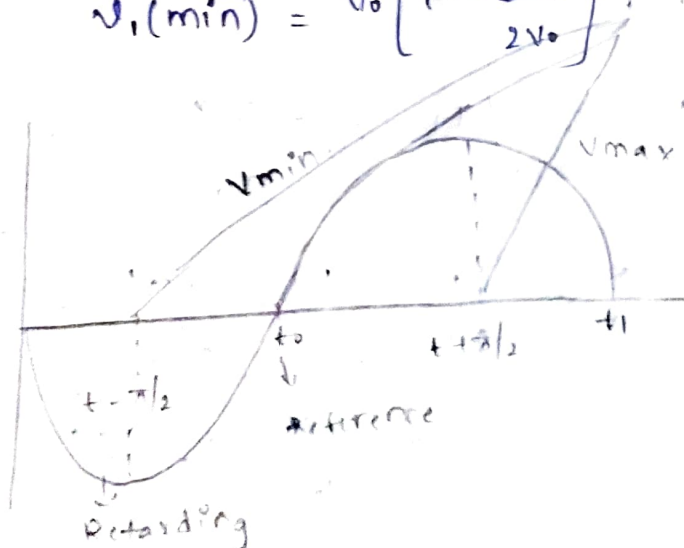
→ Maximum Velocity occurs at  $\pi/2$ , so that voltage will be maximum

$$\theta_g = (\omega \{ t_1 - t_0 \})$$

$$V_1(\max) = V_0 \left[ 1 + \frac{V_1}{2V_0} \right]$$

→ minimum velocity occurs at  $\pi/2$ , so that voltage will be minimum

$$V_1(\min) = V_0 \left[ 1 - \frac{V_1}{2V_0} \right]$$



→ If the distance in the drift space at which bunching occurs from the buncher grid at time  $t_1$  is  $L_1$

$$L_1 = v_0(t_1 - t_0)$$

$$L_1 \text{ at } t - \pi/2 = v_{\min}(t_1 - t - \pi/2)$$

$$L_1 \text{ at } t + \pi/2 = v_{\max}(t_1 - t + \pi/2)$$

$$t - \pi/2 = t_0 - \frac{\pi}{2\omega}$$

$$t + \pi/2 = t_0 + \frac{\pi}{2\omega}$$

$$L_1 \text{ at } t - \pi/2 = v_0 \left(1 - \frac{v_1}{2v_0}\right) \left(t_1 - t_0 + \frac{\pi}{2\omega}\right)$$

$$L_2 \text{ at } t + \pi/2 = v_0 \left(1 + \frac{v_1}{2v_0}\right) \left(t_1 - t_0 + \frac{\pi}{2\omega}\right)$$

$$\therefore L_1 = v_0(t_1 - t_0) + v_0 \left[ \frac{\pi}{2\omega} - \frac{v_1}{2v_0} (t_1 - t_0) - \frac{v_1}{2v_0} \frac{\pi}{2\omega} \right]$$

If the distance has to be same for  $-\pi/2, 0, +\pi/2$  bunches the  $L_1$  for all 3 should be equal to  $v_0(t_1 - t_0)$

$$\frac{\pi}{2\omega} - \frac{v_1}{2v_0} (t_1 - t_0) - \frac{v_1 \pi}{2v_0 \cdot 2\omega} = 0$$

neglect

$$\frac{\pi}{2\omega} = \frac{v_1 (t_1 - t_0)}{2v_0} + \frac{v_1 \pi}{2v_0 \cdot 2\omega}$$

$$= \frac{2\omega v_1 (t_1 - t_0) + v_1 \pi}{2v_0 \cdot 2\omega}$$

$$\frac{\pi}{2\omega} (t_1 - t_0) = \frac{v_1 \pi}{2v_0 \cdot 2\omega}$$

$$(t_1 - t_0) = \frac{\pi}{2\omega}$$

$$\frac{\pi}{2\omega} - \frac{V_1}{2V_0} (t_1 - t_0) - \frac{V_1 \pi}{2V_0 2\omega} = 0$$

$$\frac{\pi}{2\omega} - \frac{V_1 \pi}{2V_0 2\omega} = \frac{V_1}{2V_0} (t_1 - t_0) = 0$$

$$\frac{\pi}{2\omega} - \frac{V_1}{2V_0} (t_1 - t_0) = \frac{V_1 \pi}{2V_0 2\omega}$$

$$t_1 - t_0 = \frac{2V_0}{V_1} \cdot \frac{\pi}{2\omega} - \frac{2V_0}{2V_1} \cdot \frac{V_1 \pi}{2V_0 2\omega}$$

$$= \frac{2V_0}{V_1} \cdot \frac{\pi}{2\omega} - \frac{\pi}{2\omega}$$

$$\therefore (t_1 - t_0) = \frac{\pi}{2\omega} - \frac{\pi}{\omega} \cdot \frac{V_0}{V_1}$$

Bunching occurs as the RF signal changes.

from  $(-\frac{\pi}{2} \text{ to } +\frac{\pi}{2})$  for a value of  $\pi$ , we are taking 3.682, so optimum bunching occurs

$$L_1 = V_0 \left( \frac{\pi V_0}{\omega V_1} \right) \rightarrow \text{Voltage is very high}$$

$$L_1 = 3.682 \frac{V_0 V_0}{\omega V_1}$$

→ If the Beam coupling coefficient of i/p cavity is  $\beta$ , where  $\beta = \frac{\sin(\theta_g/2)}{(\theta_g/2)}$  ( $\therefore \theta_g = \frac{\omega d}{V_0}$ )

$$\eta_{\max} = 3.682 \frac{V_0 V_0}{\omega \beta V_1} \left[ \eta = \frac{P_{\text{out}}}{P_{\text{in}}} \right]$$

Calculate  $\eta = \frac{P_{\text{out}}}{P_{\text{in}}}$



Performance characteristics for 2 cavity klystron

→ frequency, works on  $(250\text{MHz} - 200\text{GHz})$

→ power,  $(10\text{kW} - 500\text{kW})$  CW -  $30\text{MW}$  (pulse)

→ power gain  $(15\text{dB} - 70\text{dB})$

→ Band width  $(10 - 60\text{MHz})$

→ Noise figure  $(15 - 20\text{dB})$

→ theoretical frequency  $(58\%)$

Applications:

→ It is used as power out tubes

a) In ultra high frequencies as TV transmitter

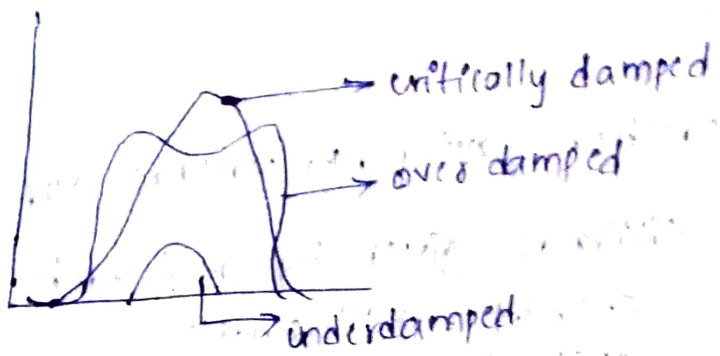
~~It is transmitter~~

b) In troposphere scatter transmitter

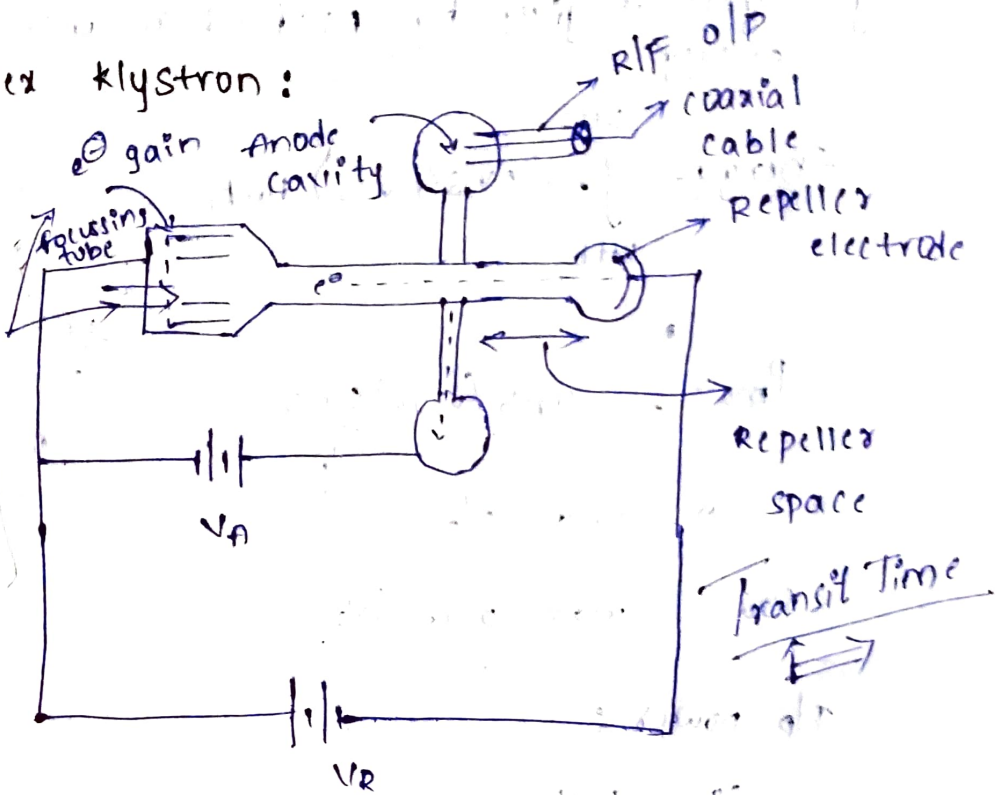
c) Satellite communications, Ground station

d) Radar transmitters

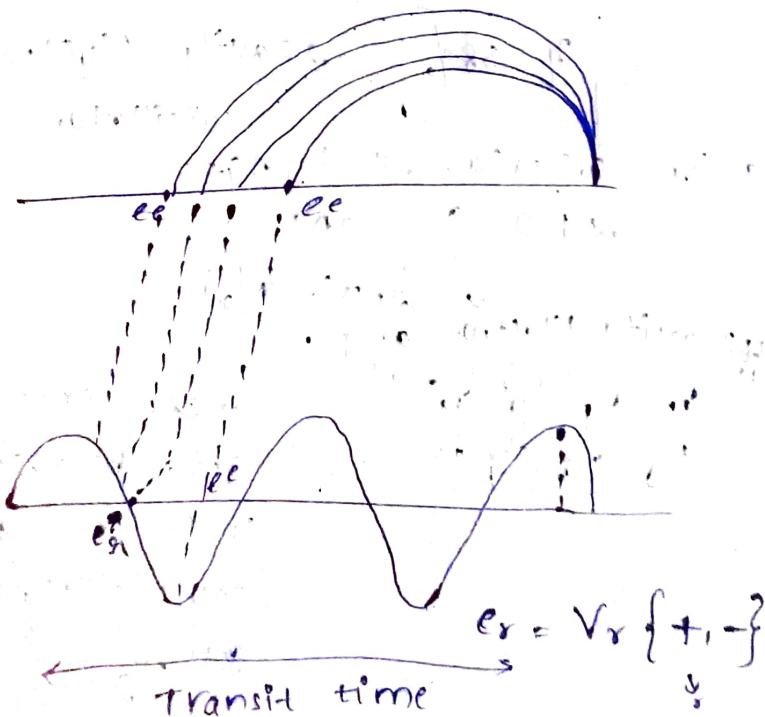
→ It is used as power oscillator  $(5 - 50\text{GHz})$  if used as klystron.



Reflex klystron:



- Q. If focussing tube is not connected then all  $e^-$  will move in separate paths.



① Bunching : occurs at different parts (Modulation & demodulation occurs)

$$e_c \Rightarrow v_c \rightarrow a_c \rightarrow v \uparrow$$

$$e_r \Rightarrow v_r \rightarrow \downarrow \rightarrow v \text{ (conducting)}$$

$$e_{s1} = v_{s1} \rightarrow -v_e \rightarrow de_{acc}$$

$$-e_c \rightarrow t_c^-$$

$$e_r \Rightarrow t_r$$

$$e_{s1} \rightarrow t_{s1}$$

$$t_c > t_r > t_{s1}$$

$$v_c > v_{s1} > v_r$$

$$v_{de} > v_{dr} > v_{de}$$

$$\text{Transit time } t = n + \frac{3}{4}$$

↓

time taken by the  $e^0$  to travel from repeller point to back to the  $e^0$

→ Always transit time should be  $+90^\circ$

→ Low efficiency and power though we are using only single cavity.

\* No Bunching

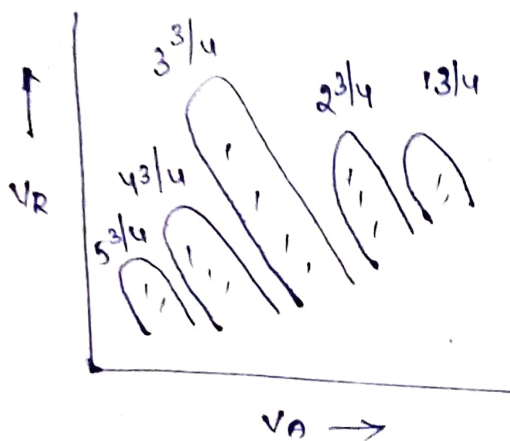
\* Sustained Oscillations

↓  
occurs at fixed intervals of time



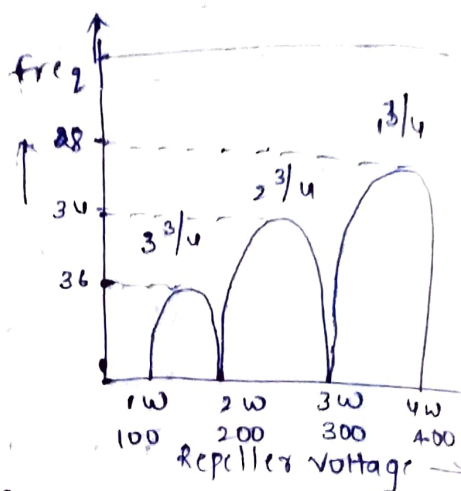
- If more no of  $e^-$  are decelerating then more energy is released resulting in more power
- Low freq, low efficiency, low power device

### Reflex klystron Oscillator



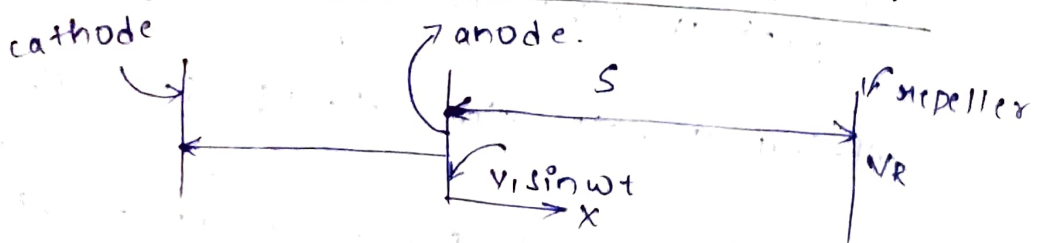
Voltage characteristics

$$T = n + 3/4$$



O/p power freq  
power character  
- P<sub>eff</sub>

### Mathematical Analysis of Reflex klystron:



→  $v_1 \sin \omega t$  = RF voltage at cavity gap

$V_R$  = Repeller voltage w.r.t cathode

$S$  = distance b/w cavity gap & repeller electrode

$v_0$  = Velocity of  $e^-$  in gun

$v_1$  = Velocity due of RF voltage in addition to the  $e^-$  accelerating voltage  $v_0$

$t_0$  = time for  $e^\ominus$  entering cavity gap at  $x=0$

$t_1$  = time for same  $e^\ominus$  leaving cavity gap at  $x=d$

$t_2$  = time for same  $e^\ominus$  return by the retarding field at  $x=d$

$$V_0 = \sqrt{\frac{2eV_0}{m}}$$

$$V_R = (V_0 + V_1 \sin \omega t_1)$$

$$V_1 = V_0 \sqrt{\frac{1 + V_1}{V_0} \cdot \sin \omega t}$$

$$= V_R - V_0$$

$$\therefore V_0 + V_1 \sin \omega t_1 = \{V_1 \leq V_0\}$$

→ retarding electrostatic field b/w repeller & anode is,

$$E = -\frac{V}{d} \{V = t d\}$$

$$= -\frac{(V_R - V_0)}{s}$$

$$F = +e \frac{(V_R - V_0)}{s}$$

$$ma = \frac{md^2x}{dt^2} = \frac{e(V_R - V_0)}{s}$$

$$\int \frac{d^2x}{dt^2} = \int \frac{e(V_R - V_0)}{ms}$$

$$\boxed{\frac{dx}{dt} = \frac{e(V_R - V_0)t}{ms} + C}$$

At  $t = t_1$ ,

$$\text{assume } \frac{dx}{dt} = V_1$$

$$V_1 = \frac{e(V_R - V_0)t_1}{ms} + C$$

$$C = V_1 - \frac{e(V_R - V_0)t_1}{ms}$$

$$\therefore \frac{dx}{dt} = \frac{e(V_R - V_0)t}{ms} + v_1 - \frac{e(V_R - V_0)t_1}{ms}$$

$$\boxed{\frac{dx}{dt} = \frac{e(V_R - V_0)(t - t_1)}{ms} + v_1}$$

$$\int \frac{dx}{dt} = \int \frac{e(V_R - V_0)(t - t_1)}{ms} + v_1$$

$$\therefore \boxed{x = \frac{e}{2ms} (V_R - V_0)(t - t_1)^2 + v_1 t + C_1}$$

At  $x = 0$ , at point of return from the sheath space assume  $t = t_2$

$$0 = \frac{e}{2ms} (V_R - V_0)(t_2 - t_1)^2 + v_1 t_2 + C_1$$

$$C_1 = -\frac{e}{2ms} (V_R - V_0)(t_2 - t_1)^2 - v_1 t_2$$

$$\therefore x = \frac{e}{2ms} (V_R - V_0)(t - t_1)^2 + v_1 t - \frac{e}{2ms} (V_R - V_0)(t_2 - t_1)^2 - v_1 t_2$$

$$\therefore \boxed{x = \frac{e}{2ms} (V_R - V_0) \left[ (t - t_1)^2 - (t_2 - t_1)^2 \right] + v_1 (t - t_2)}$$

$$(t^2 + t_1^2 - 2tt_1 - (t_2^2 + t_1^2 - 2t_1t_2))$$

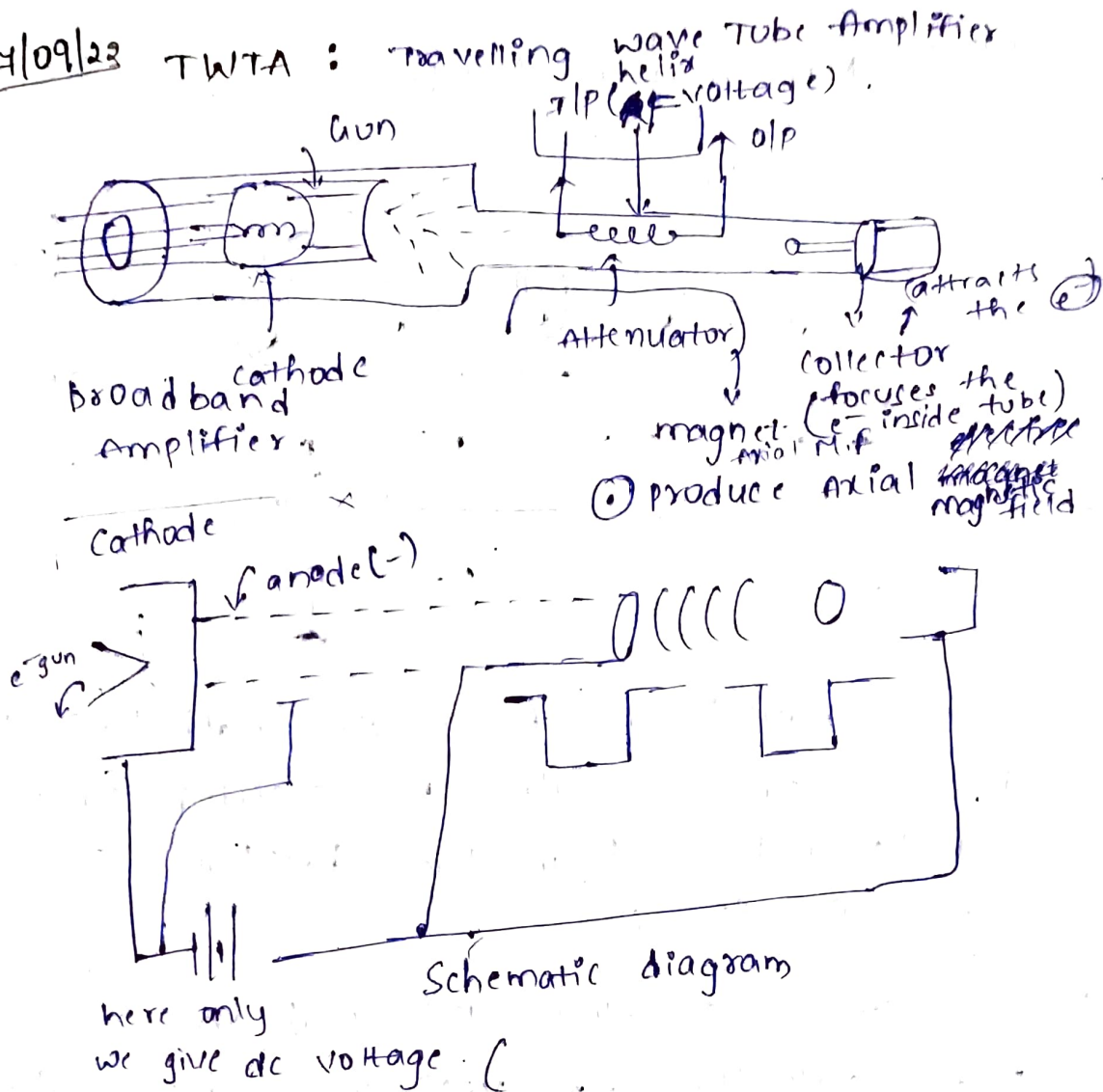
At  $x = 0$ ,  $t = t_1$

$$0 = \frac{e}{2ms} (V_R - V_0) \left[ -(t_2 - t_1)^2 \right] + v_1 (t_1 - t_2)$$

$$= \frac{e}{2ms} (V_R - V_0) (t_2 - t_1)^2 = v_1 (t_2 - t_1) \quad (-1)$$

$$\boxed{t_2 - t_1 = \frac{-v_1 \cdot 2ms}{e(V_R - V_0)}}$$

27/09/22 TWTA : Travelling wave Tube Amplifier



helical structure : slow wave structural helix.  
 $= 0.1 v_c$  (velocity of light)

bunching effect:

$$v_n = v_c \left[ \frac{\text{pitch of helix}}{\text{circumference of helix}} \right] \left\{ \begin{array}{l} \text{distance from} \\ \text{any helix to} \\ \text{other helix} \end{array} \right\} \rightarrow 2\pi r$$

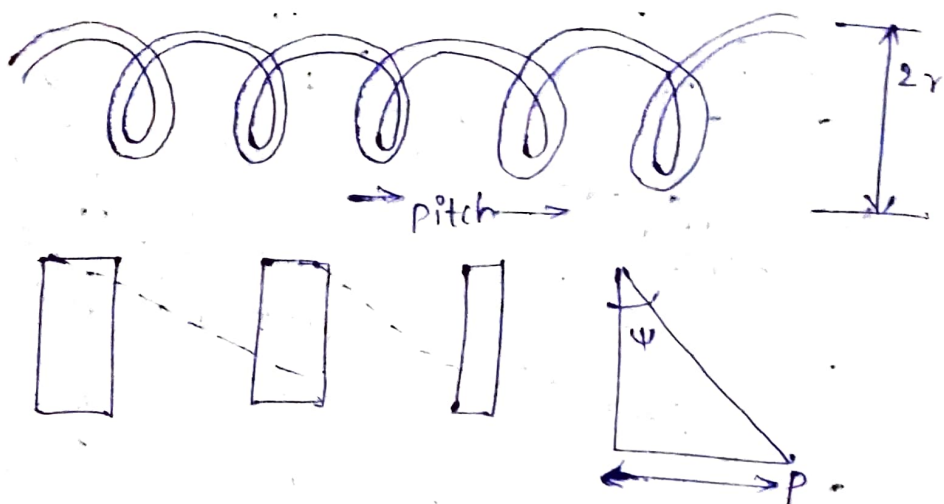
① due to reduce of electric field.

② interaction of  $e^-$  which are in high position only they interact.

→ As we are using broadband amplifier it should be modulated.

28/09/22

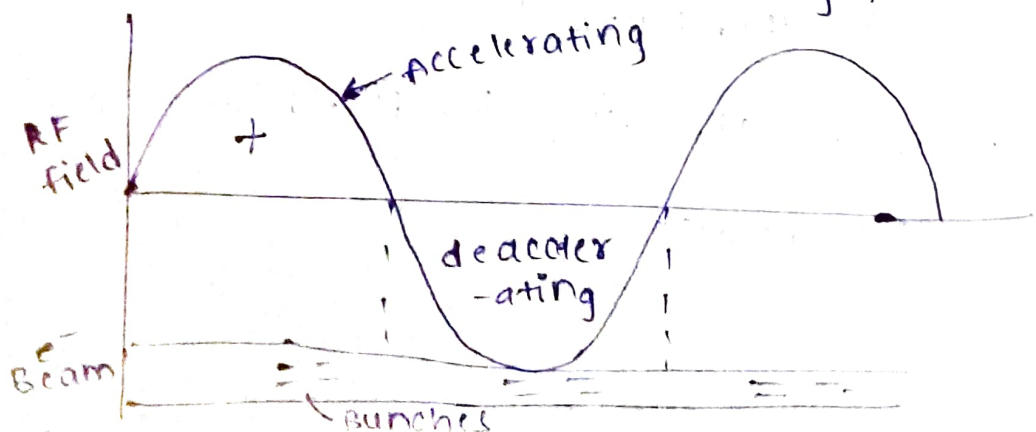
## Mathematical Analysis :



① The conductivity of smooth sheath helix in direction of helix wire is specified to be infinite and that in the direction  $\perp$  to helix wire is '0'.

② helix support a slow wave with an axial phase velocity  $v_p = v \sin \psi$ , where ' $\psi$ ' is the helix angle,  $\psi = \tan^{-1}(p/2\pi r)$ .

③ The wave travelling along helix has a longitudinal component of electric field which causes <sup>velocity</sup> modulation of electron <sup>beam</sup> ( $v$ ). This velocity modulation causes bunching of elec at regular interval of one wavelength.





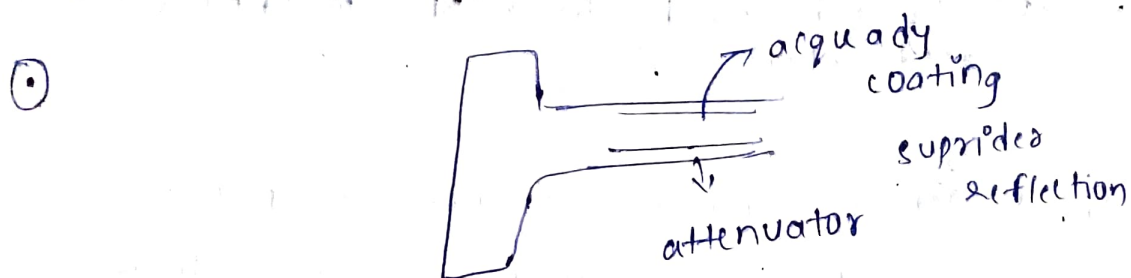
① Gain of TWT  $\left[ \begin{aligned} G &= -9.54 + 47.3 N \text{ (dB)} \\ C &= \text{gain parameter} = k \left( \frac{I_0}{V_0} \right)^{1/3} \end{aligned} \right]$

$N = \text{helix length in wavelength} = \frac{L}{\lambda_g}$

$\lambda_g = \frac{v_p}{f}$

Here 'k' is constant,  $v_p$  is axial phase velocity  
 $I_0$  is dc beam current,  $V_0$  is dc beam voltage

① The gain will be maximum when beam voltage is approximately in synchronism with the axial ~~phase~~ <sup>phase</sup> velocity ( $v_p$ )



Performance characteristics of TWT :

① frequency of operation : (0.5 MHz - 95 GHz)

① power output : (5 mW - 10 W power TWT)

250 kW : ~~low~~ <sup>CW</sup> (high power)

10 MW : pulsed

3 GHz : continuous wave

① efficiency : (5-20%)

① noise figure (4-6 dB) - low power

25 dB - high power at 40 GHz

## Applications of TWT :

- ① Low noise RF amplifier in broadband amp
- ① Repeater amplifier in wide band communication links & coaxial cables
- ① Due to long tube life TWT is used as power output tube in communication satellite
- ① continuous wave high power TWT's are used in tropo scatter links.
- ① Air borne & ship borne pulsed high power radars
- ① GBR (ground based radar) used in ECM. (broad band TWT)

Eg:- A Reflex klystron operates at peak mode of  $N = 2$ , with beam voltage  $V_0 = 300\text{V}$ , beam current  $I_0 = 20\text{mA}$ , signal voltage  $V_1$  is  $40\text{V}$

Determine i, Input power in Watts

ii o/p power in Watts

iii efficiency.

Eg:- i, Input power =  $V_0 I_0$

$$= 300 \times 20 \times 10^{-3}$$

$P_{dc}$

$$= 6\text{Wts}$$

$\rightarrow 1.25$

ii o/p power

$$= \frac{2 V_0 I_0 \times \overbrace{1}^{1.25}}{2n\pi - \pi/2} \left( \frac{V_1}{V_0} \right)$$

$$= \frac{2(300)(0.02) \times 1.25}{2(2)\pi - \pi/2}$$

$P_{ac}$

$$= \frac{12 \times 1.25}{4\pi - \pi/2} = 1.364\text{Wts}$$

$$\text{iii efficiency} = \frac{P_{dc}}{P_{ac}}$$

$$= \frac{1.36}{6}$$

$$= 22.7\%$$

eg. (2) - A reflex klystron operates at the peak  $N=1$  on  $3/4$ . The dc power i/p 400mw, ratio of  $V_1$  over  $V_0$  is 0.278.  $\therefore$  determine efficiency of

Reflex klystron

ii, Total power o/p in mw

iii If 20% of power delivered by electron beam is dissipated in cavity walls. find the power delivered to the load.

Sol:- i  $\eta = \frac{2x'J_1(x')}{2n\pi + \pi/2}$  ,  $n=1$  2x + 1/2  
5/2

$$= \frac{2(125)}{100(5\pi/2)} = \frac{5256 \times 2}{100(5\pi)} = 1/\pi$$

$$\eta = 0.318 \Rightarrow 31.8\%$$

iii o/p power = 2