

VHF Propagation

For a medium which has a dielectric constant ‘ ϵ ’ and a conductivity ‘ σ ’

$$\nabla \times H = \epsilon \dot{E} + \sigma E$$

If the variation of E with time is sinusoidal,

$$E = E_0 e^{j\omega t}$$

$$\dot{E} = j\omega E$$

$$\begin{aligned}\nabla \times H &= \left(\epsilon + \frac{\sigma}{j\omega} \right) \dot{E} \\ &= \epsilon' \dot{E}\end{aligned}$$

Partially conducting dielectric can be considered as a dielectric that has a complex dielectric constant ϵ'

$$\epsilon' = \epsilon \left(1 + \frac{\sigma}{j\omega\epsilon} \right)$$

The wave equations and reflection coefficient derived for perfect dielectrics will apply directly to dielectric having loss or conductance, if the dielectric ϵ is replaced by an equivalent complex dielectric constant

$$\epsilon' = \left(\epsilon + \frac{\sigma}{j\omega} \right)$$

θ is the angle of incidence measured from the normal in dealing with reflection by the earth, it is usual to express the direction of the incident wave in terms of angle ψ which is measured from the Earth’s surface.

$$\psi = 90^\circ - \theta$$

so that

$$\cos \theta = \sin \psi$$

$$\sin \theta = \cos \psi$$

$$\Gamma_{\text{h}}$$

$$\Gamma_{\text{v}}$$

1) surface wave is neglected

2) ψ is very small

so that Γ_{v} or $\Gamma_{\text{h}} \cong -1$

$$\begin{aligned} |E| &= \frac{60I}{d} \left| 1 + \Gamma_{\text{h}} \angle -\alpha \right| \\ &= \frac{60I}{d} \left| 1 - 1 \angle -\alpha \right| \end{aligned}$$

where

$$\alpha = \frac{2\pi}{\lambda} (R_2 - R_1)$$