

R18**Code No: 153BQ****JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD****B. Tech II Year I Semester Examinations, December - 2019****PROBABILITY THEORY AND STOCHASTIC PROCESSES****(Electronics and Communication Engineering)****Time: 3 Hours****Max. Marks: 75****Note:** This question paper contains two parts A and B.

Part A is compulsory which carries 25 marks. Answer all questions in Part A. Part B consists of 5 Units. Answer any one full question from each unit. Each question carries 10 marks and may have a, b as sub questions.

PART – A**(25 Marks)**

- 1.a) What is the importance of Rayleigh distribution function? [2]
- b) How interval conditioning is different from point conditioning? [2]
- c) Define WSS random process. [2]
- d) Define rms bandwidth of the power spectrum. [2]
- e) What is meant by conditional Entropy? [2]
- f) Write the conditions to be satisfied by a function to be a random variable. [3]
- g) Define joint characteristic functions of two random variables. [3]
- h) Determine the mean-square value of a random process with autocorrelation function:
 $R_{XX}(\tau) = e^{-|\tau|}$ [3]
- i) Write any three properties of cross-power density spectrum. [3]
- j) Write the equation of an average Noise Figure of cascaded networks. [3]

PART – B**(50 Marks)**

- 2.a) Give Classical and Axiomatic definitions of Probability.
- b) In a single throw of two dice, what is the probability of obtaining a sum of at least 10? [5+5]

OR

- 3.a) Define conditional distribution and density functions and list their properties.
- b) In a box there are 100 resistors whose resistances and tolerances are as shown in the table below. Let A be the event of drawing a 47Ω resistor, B be the event of drawing a resistor with 5% tolerance, and C be the event of drawing a 100Ω resistor. Find $P(A/B)$, $P(A/C)$ and $P(B/C)$. [5+5]

Resistance (Ω)	Tolerance		Total
	5%	10%	
22	10	14	24
47	28	16	44
100	24	8	32
Total	62	38	100

- 4.a) State and explain the central limit theorem.
 b) Obtain the variance of Raleigh random variable. [5+5]

OR

- 5.a) Find the mean of Binomial random variable.
 b) Identify the value of moment μ_{22} , if statistically independent random variables X and Y have moments $m_{10} = 2$, $m_{20} = 14$, $m_{02} = 12$ and $m_{11} = -6$ [5+5]

- 6.a) List and explain various properties of Autocorrelation function.
 b) Given the Autocorrelation function of the processes:

$$R_{XX}(\tau) = 25 + \frac{4}{1 + 6\tau^2}$$

Find the mean and variance of the process X(t). [5+5]

OR

- 7.a) Compare the Cross Correlation Function with Autocorrelation function.
 b) Assume that an Ergodic random process X(t) has an autocorrelation function:

$$R_{XX}(\tau) = 18 + \frac{2}{6 + \tau^2} [1 + 4 \cos(12\tau)]$$

- i) Find $|\bar{x}|$.
 ii) Does this process have periodic component?
 iii) What is the average power in X(t)? [5+5]

8. Compute the average power of the process having power spectral density $6\omega^2/(1+\omega^4)$. [10]

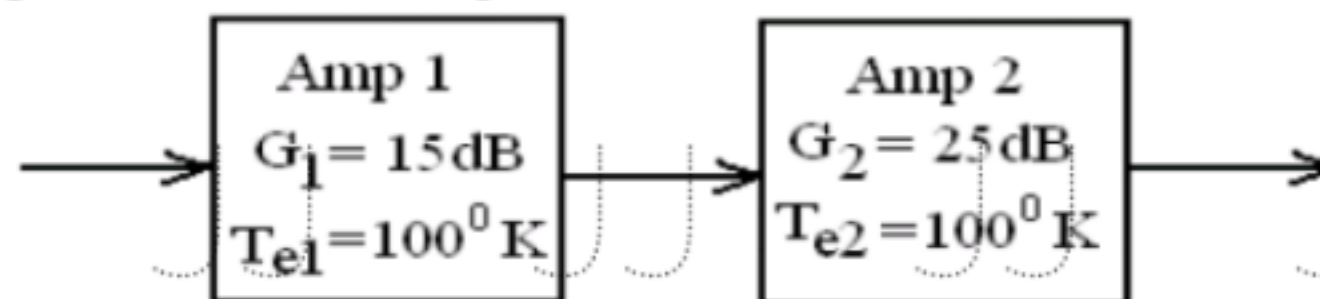
OR

- 9.a) If the PSD of X(t) is $S_{xx}(\omega)$. Find the PSD of $dx(t)/dt$.
 b) If $Y(t) = A \cos(\omega_0 t + \theta) + N(t)$, where 'θ' is a uniform random variable over $(-\pi, \pi)$, and N(t) is a band limited Gaussian white noise process with $PSD = K/2$. If 'θ' and N(t) are independent, find the PSD of Y(t). [5+5]

- 10.a) Derive noise figure in terms of network transfer function.
 b) Explain Huffman coding with example. [5+5]

OR

- 11.a) Find the overall noise figure and equivalent input noise temperature of the circuit shown in figure. Take room temperature = 27°C .



- b) How to trade off between band width and SNR? Explain with example. [5+5]

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