

## UNIT - 1

### Multistage Amplifiers:

#### Classification of Amplifiers:

1. Based on the Transistor configurations, the amplifiers are classified as,

- Common Emitter Amplifier
- Common Base Amplifier
- Common Collector Amplifier

2. Based on the Frequency range

- Audio Frequency range amplifier (20 to 20 KHz)
- Video Frequency range Amplifier / Pulse amplifier (Hz to few MHz)
- Radio Frequency range Amplifier / High frequency range Amplifier (Hundreds to MHz)
- Ultra high frequency range Amplifier (VHF) (100s to 1000 MHz)

3. Based on the type of coupling

- RC coupled Amplifier
- Transformer coupled Amplifier
- Direct coupled Amplifier

4. Based on the method of operation / Power amplifiers

- Class A power Amplifier
- Class B power Amplifier
- Class C power Amplifier
- Class AB power Amplifier

5. Based on the type of signal

→ Small signal Amplifiers

→ Large signal Amplifiers

6. Based on Application

→ Voltage Amplifiers

→ Current Amplifiers

→ Power Amplifier

→ Tuned Amplifier

### Distortions in Amplifiers

1. Nonlinear Distortion / Amplitude distortion:

In this type of distortion some new frequencies are present in output which are not present in input.

2. Frequency Distortion: It occurs due to some reactive components.

They are identified in frequency response

3. Phase shift Distortion: It occurs due to complex conjugate components present in the circuit.

Different types of coupling schemes:

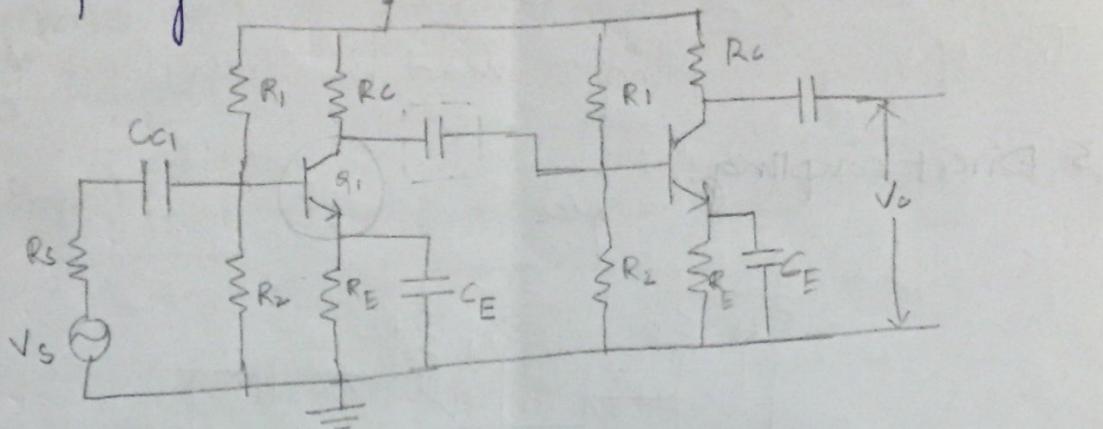
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1. RC coupling

2. Transformer coupling

3. Direct coupling

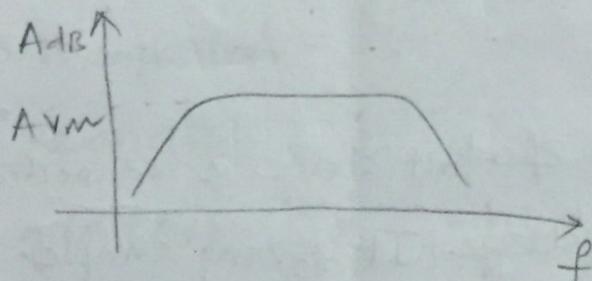
## 1. RC coupling:



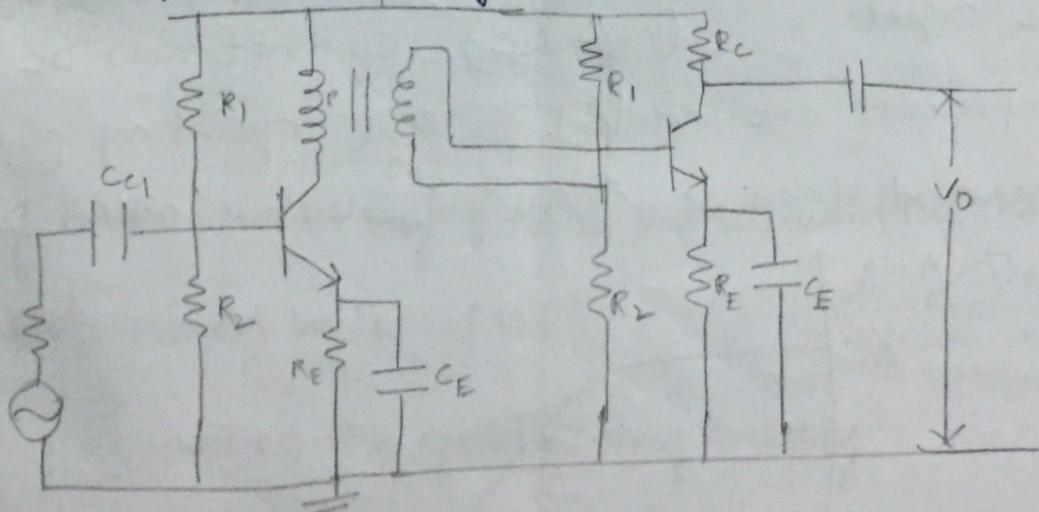
(Two stage RC coupled Amplifier)

There are no disturbances in the operating point due to  
RC coupling.

Capacitor allows only AC signal to the next level by  
blocking the DC signal so the response will be as  
expected.



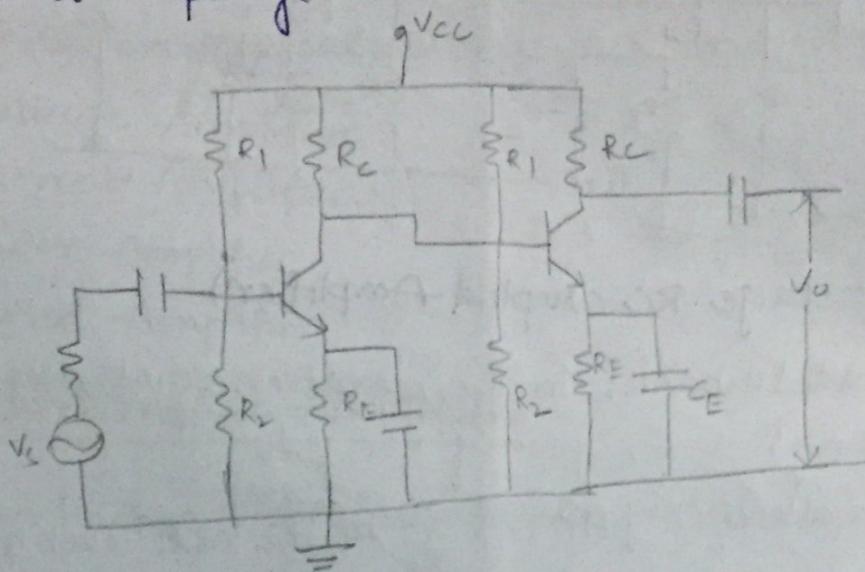
## 2. Transformer coupling:



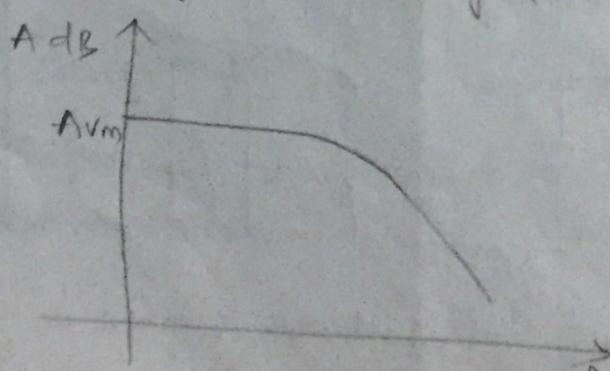
The output of the first stage is given as the  
input of the next stage through transformer. As the  
inductive elements are present, there will be some  
leakage so

the frequency response is distorted. Circuit is also complex  
 Transformer coupling is used in Impedance matching.

### 3. Direct coupling:



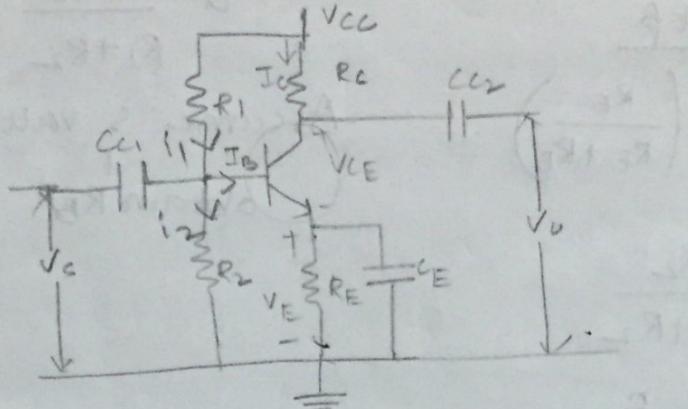
The output of first stage is connected directly to the next stage. It is very simple. By  $R_1, R_2$  and  $V_{cc}$  some DC components are added to the signal.  $\downarrow$  (new DC) so that new DC components are added so that operating point of the next stage is changed which is called Drift.



where ever the DC amplification is required the Direct coupled Amplifier is used.

RC coupled Amplifier is preferred because the frequency response will be similar to ideal response. Circuit is also simple.

Design & Analysis  
Design of CE Amplifier circuit:



$R_1$  &  $R_2$  — Biasing Resistors ;  $R_c$  — Collector Resistance

$R_E$  — Emitter Resistance ;  $C_{c1}$ ,  $C_{c2}$  — Coupling capacitors

$C_E$  — Bypass capacitor.

Design of  $R_C$  and  $R_E$

$$\text{Voltage gain } (A_v) = \frac{A_i R_L}{Z_i} = -\frac{h_{fe} R_L}{h_{ie}} = -\frac{h_{fc} R_C}{h_{ie}}$$

$$V_{CC} = I_C R_C + V_{CE} + V_E$$

$$R_C = \frac{V_{CC} - V_{CE} - V_E}{I_C} \quad \text{--- (1)}$$

→  $V_{CE}$  should be 50% of  $V_{CC}$  to avoid the thermal

→  $V_E$  should be 10% of  $V_{CC}$

Runaway  
(self destruction of Transistor)

to maintain the good biasing stability

$$V_E = I_E R_E$$

Assumptions  
before finding  $R_C$

$$R_E = \frac{V_E}{I_E} \quad (I_C \approx I_E) \quad \text{--- (2)}$$

## Design of $R_1$ & $R_2$

$$V_B = V_{CC} \frac{R_2}{R_1 + R_2} \quad \text{--- (3)}$$

$$S = \frac{1+\beta}{1+\beta \left( \frac{R_E}{R_E + R_B} \right)}$$

$$R_B = \frac{R_1 R_2}{R_1 + R_2} \quad \text{--- (4)}$$

Assume 'S' value and obtain  $R_B$

$$\frac{V_B}{V_{CC}} = \frac{R_2}{R_1 + R_2}$$

$$\Rightarrow \frac{R_B}{R_1} = \frac{R_2}{R_1 + R_2}$$

(Alternative method)

$$I_B \approx \text{negligible} \Rightarrow i_1 = i_2 ; R_1 = \frac{V_{CC} - V_B}{i_2}$$

$i_2$  value is taken as 10% of  $I_C$

## Design of coupling capacitors

For designing coupling capacitors, consider the lower cutoff frequency, as it effects the  $f_L$  value

$$X_{C1} = \frac{1}{2\pi f_L C_{C1}}$$

For good biasing, choose  $X_{C1}$  such that it should be equal to 10% of  $R_i$

$$f_L = \frac{1}{2\pi R_i C_{C1}}$$

$$(R_i = R_1 || R_2 || h_{ie})$$

$$X_{C2} = \frac{1}{2\pi f_L C_{C2}}$$

$$X_{C2} = 10\% \text{ of } R_o$$

$$(R_o = R_{out} || R_L)$$

## Design of Bipolar capacitor

(C<sub>E</sub>)

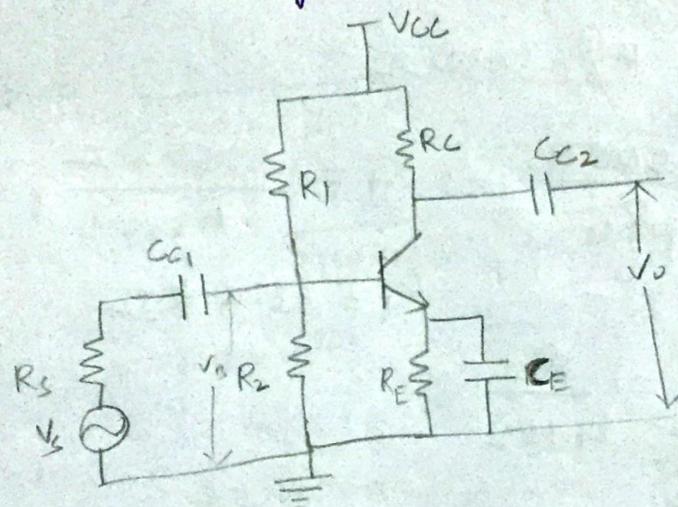
X<sub>CE</sub> value should be equal to 10% of R<sub>E</sub>

$$X_{CE} = \frac{1}{2\pi f_L C_E}$$

→ Design a single stage RC coupled Amplifier. Assume

V<sub>CC</sub> = 12V, I<sub>C</sub> = 1mA; β = 100; R<sub>L</sub> = 1kΩ; R<sub>E</sub> = 1kΩ

f<sub>L</sub> = 100Hz. Stability factor (S = 5).



$$\beta = \frac{I_C}{I_B} \Rightarrow \frac{10^3}{I_B} = 10$$

$$I_B = 10^5$$

$$R_C = \frac{12 - 6 - 1.2}{1 \times 10^3} \Rightarrow \frac{4.8}{10^3} \Rightarrow 4.8 \text{ k}\Omega$$

$$R_E = \frac{1.2}{1 \times 10^3} \Rightarrow 1.2 \times 10^3$$

$$V_B = 12 \left( \frac{R_2}{R_1 + R_2} \right)$$

$$V_B = V_{BE} + V_E \Rightarrow 0.6 + 1.2$$

$$5 = \frac{1+100}{1+100 \left( \frac{1.2 \times 10^3}{1.2 \times 10^3 + R_B} \right)} \Rightarrow 1.8$$

$$\frac{1.8}{12} = \frac{R_B}{R_1}$$

$$5 + 500 \left( \frac{1.2 \times 10^3}{1.2 \times 10^3 + R_B} \right) = 101$$

$$500 \left( \frac{1.2 \times 10^3}{1.2 \times 10^3 + R_B} \right) = 96$$

$$\frac{1.2 \times 10^3}{1.2 \times 10^3 + R_B} = 0.192$$

$$\frac{1.2 \times 10^3}{0.192} = 1.2 \times 10^3 + R_B$$

$$6.25 \times 10^3 = 1.2 \times 10^3 + R_B \Rightarrow R_B = 5.05 \times 10^3$$

$$R_B = 5.05 \times 10^3 \Omega$$

$$R_B = 5050 \Omega$$

$$\frac{1.8}{12} = \frac{5050}{R_1} \quad R_1 = \frac{5050 \times 12}{1.8}$$

$$R_1 = 33.6 \times 10^3 \Omega$$

$$\frac{5050}{33.6 \times 10^3} = \frac{R_2}{R_1 + R_2}$$

$$\frac{33.6 \times 10^3}{5050} = 1 + \frac{R_2}{R_2}$$

$$6.65 - 1 = \frac{R_1}{R_2}$$

$$5.65 = \frac{R_1}{R_2} \Rightarrow R_2 = \frac{33.6 \times 10^3}{5.65}$$

$$R_2 = 5.9 \times 10^3 \Omega$$

$$X_{C1} = \frac{1}{2\pi f_L C_1}$$

$$R_i = R_1 || R_2 || hie$$

$$\frac{1}{R_i} = \frac{1}{10^3} (0.02 + 0.16 + 1)$$

$$\frac{1}{R_i} = \frac{1}{33.6 \times 10^3} + \frac{1}{5.9 \times 10^3} + \frac{1}{10^3}$$

$$\frac{1}{R_i} = \frac{(1.18)}{10^3}$$

$$R_i = \frac{10^3}{1.18}$$

$$\frac{1}{R_i} = \frac{1}{10^3} \left( \frac{1}{33.6} + \frac{1}{5.9} + 1 \right)$$

$$R_i = 0.849 \times 10^3 \Rightarrow 849 \Omega$$

$$C_{C1} = \frac{1}{100 \times 2 \times 3.14 \times 847}$$

$$C_{C1} = \frac{1}{531916} = 1.87 \times 10^6 F$$

$$C_C = 1.87 \mu F$$

$$R_0 = R_C \parallel R_L$$

$$\frac{1}{R_0} = \frac{1}{4.8 \times 10^3} + \frac{1}{10^2} = \left( \frac{1}{4.8} + 1 \right) \times \frac{1}{10^2} = \frac{1}{R_0}$$

$$X_{C2} = 0.83 \times 10^2 \\ = 83$$

$$(1.2) \times \frac{1}{10^2} = \frac{1}{R_0}, \\ R_0 = 0.83 \times 10^3$$

$$83 = \frac{1}{2 \times 3.14 \times 100 \times C_{C2}}$$

$$C_{C2} = \frac{1}{314 \times 166} = \frac{1}{52124} = 19.1 \times 10^{-6} F \\ = 19.1 \mu F$$

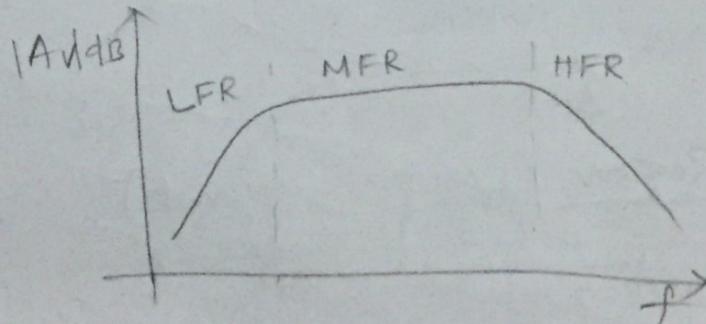
$$X_{CE} = 1.2 \times 10^2$$

$$120 = \frac{1}{2 \times 314 \times C_E} \quad C_E = \frac{1}{314 \times 240} = \frac{1}{75360}$$

$$C_E = 13.2 \times 10^{-6} F$$

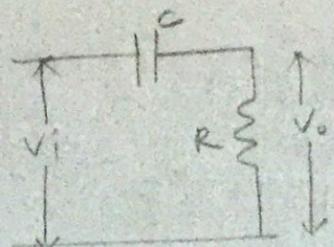
$$C_E = 13.2 \mu F$$

### Frequency response of CE Amplifier



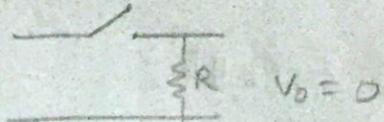
### Low-frequency Region (High pass circuit)

In low frequency region, it acts as a high pass filter.

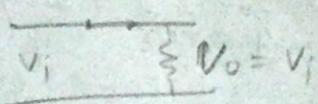


$$X_C = \frac{1}{2\pi f C}$$

$$f=0 \quad X_C = \frac{1}{0} = \infty$$



$$f=\infty \quad X_C = \frac{1}{\infty} = 0$$



$$V_o = V_i \frac{R}{R+X_C}$$

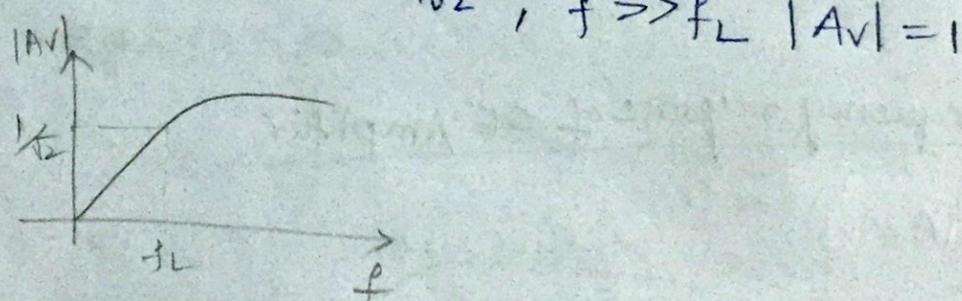
$$A = \frac{V_o}{V_i} = \frac{R}{R+X_C} = \frac{1}{1 + \frac{X_C}{R}} = \frac{1}{1 + \frac{1}{\omega CR}} = \frac{1}{1 + \frac{1}{2\pi f R C}}$$

$$|A_{vL}| = \frac{1}{\sqrt{1 + (\frac{f_L}{f})^2}}$$

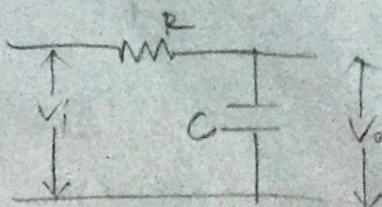
$$\text{where } f_L = \frac{1}{2\pi R C}$$

$$f=0; |A_v|=0$$

$$f=f_L; |A_v| = \frac{1}{\sqrt{2}}; \quad \because f > f_L \quad |A_v| \approx 1$$



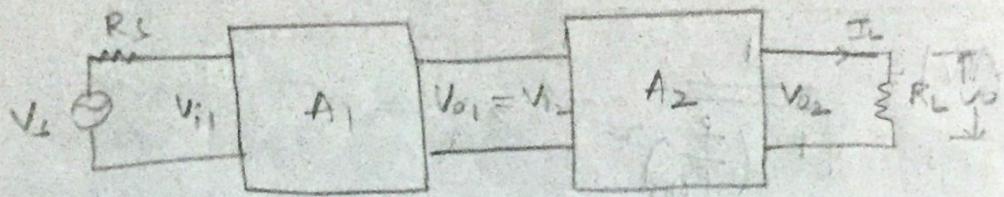
High frequency Region (Lowpass circuit)



$$\frac{V_o}{V_i} = \frac{X_C}{R+X_C} \Rightarrow$$

$$\frac{\frac{1}{j\omega C}}{R + \frac{1}{j\omega C}}$$

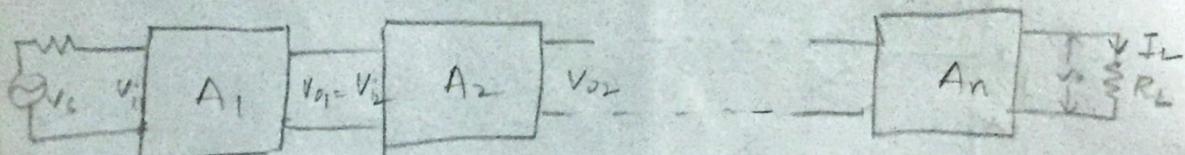
# Analysis of Multistage Amplifiers



Two stage amplifier

$$A_v = \frac{V_{o2}}{V_{i1}} = \frac{V_{o2}}{V_{i2}} \times \frac{V_{i2}}{V_{i1}} = A_{v2} \times A_{v1}$$

The gain of two stage amplifier is equal to product of individual stage gains.

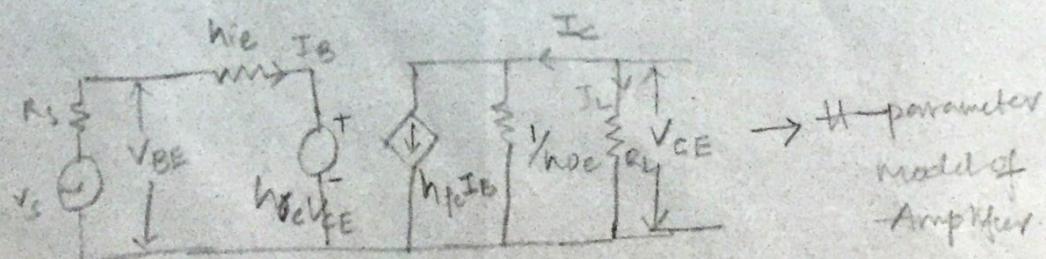
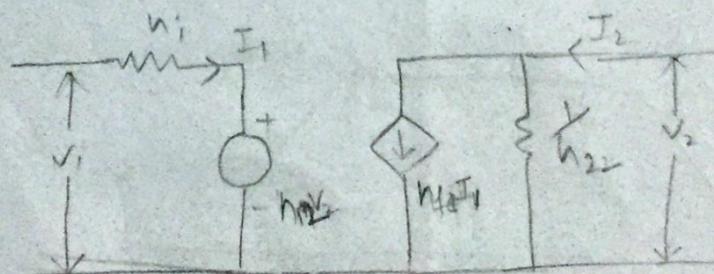


$$A_v = A_{v1} \times A_{v2} \dots A_m$$

H-parameter model

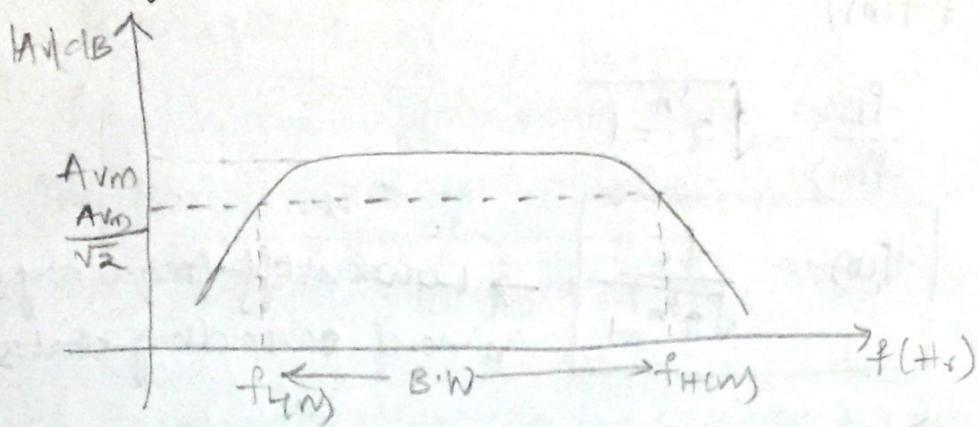
$$V_1 = h_{11}I_1 + h_{12}I_2$$

$$I_2 = h_{21}I_1 + h_{22}V_2$$



# Effect of bandwidth on Multistage Amplifier

2/1/2020



$$\text{Overall gain, } A_{vnj} = A_{v1} \times A_{v2} \times \dots \times A_{vn}$$

$$\text{Bandwidth, } B.W(n) = f_{H(n)} - f_{L(n)}$$

The voltage gain at low frequency region is,

$$|A_{VL}| = \frac{1}{\sqrt{1 + \left(\frac{f_L}{f}\right)^2}}$$

The voltage gain at high frequency region is,

$$|A_{VH}| = \frac{1}{\sqrt{1 + \left(\frac{f}{f_H}\right)^2}} \quad (\text{identical stages})$$

At lower frequency, the gain of 'n' no. of stages is

$$\frac{1}{\sqrt{2}} = \left[ \frac{1}{\sqrt{1 + \left(\frac{f_L}{f_{L(n)}}\right)^2}} \right]^n$$

$$\frac{1}{\sqrt{2}} = \left( \sqrt{1 + \left(\frac{f_L}{f_{L(n)}}\right)^2} \right)^{-n}$$

$$\alpha = \left( 1 + \left( \frac{f_L}{f_{L(n)}} \right)^2 \right)^{-n}$$

$$\frac{1}{2} = 1 + \left( \frac{f_L}{f_{L(n)}} \right)^2$$

$$\left(\frac{f_L}{f(n)}\right)^2 = 2^n - 1$$

$$\frac{f_L}{f(n)} = \sqrt{2^n - 1}$$

$$f(n) = \frac{f_L}{\sqrt{2^n - 1}}$$

$\rightarrow$  Low cutoff frequency for  
 $n$ : no. of cascading stages

$f_L \rightarrow$  Lower cutoff frequency of single stage.

$n \rightarrow$  no. of cascading stages.

At high frequency region

$$\frac{1}{\sqrt{2}} = \left(1 + \left(\frac{f}{f_H}\right)^2\right)^{-n}$$

$$\sqrt{2} = \left(1 + \left(\frac{f}{f_H}\right)^2\right)^n$$

$$\Rightarrow \alpha = \left(1 + \left(\frac{f}{f_H}\right)^2\right)^n$$

$$2^n = 1 + \left(\frac{f}{f_H}\right)^2$$

$$\left(\frac{f(n)}{f_H}\right)^n = \alpha^n - 1$$

$$\frac{f(n)}{f_H} = \sqrt{\alpha^n - 1}$$

$$f(n) = f_H \sqrt{\alpha^n - 1}$$

$f_H(n)$  - upper cutoff frequency of  $n$  no. of cascading stages  $\rightarrow$  (identical stages)

$f_H \rightarrow$  upper cutoff frequency of single stage

$n \rightarrow$  no. of cascading stages.

$$B.W(n) = f_H(n) - f_L(n)$$

$$B.W(n) \approx f_H(n)$$

$f_H(n)$  is the approximate bandwidth.

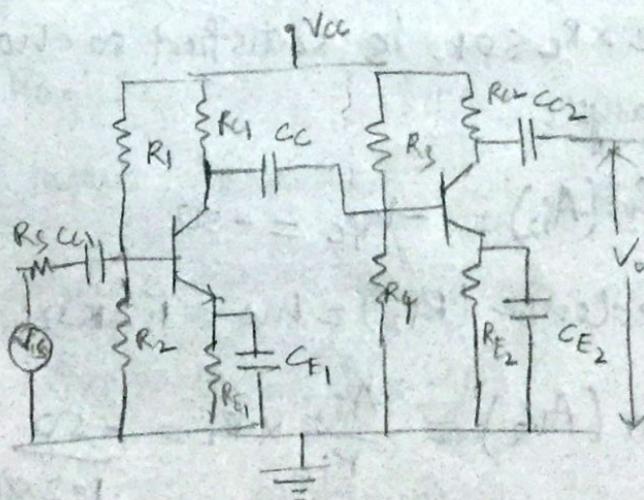
The Band width of 'n' no. of cascading stages is

$$B.W(n) = f_H \sqrt{2^n - 1}$$

- The Bandwidth decreases by cascading no. of stages, and the gain increases. [Gain × Bandwidth = constant]
- In multistage amplifiers  $f_{un}$  is always greater than  $f_L$  and  $f_H(n)$  is always less than  $f_H$ . Therefore we can say that bandwidth of multistage amplifier is less than the single stage.
- If the stages are not identical then  $f_H$ , the bandwidth is approximately equal to  $f_{H1}$

i.e.,  $\frac{1}{f_H} = 1.1 \sqrt{\frac{1}{f_1^2} + \frac{1}{f_2^2} + \dots + \frac{1}{f_n^2}}$

Analysis of two stage RC coupled CE-CE cascade Amplifier.



Assume all the external capacitors are short circuited.

1) Calculate  $R_i$ ,  $A_V$ ,  $A_i$ ,  $R_o$ , and  $A_{IS}$ ,  $A_{VS}$  if circuit parameters

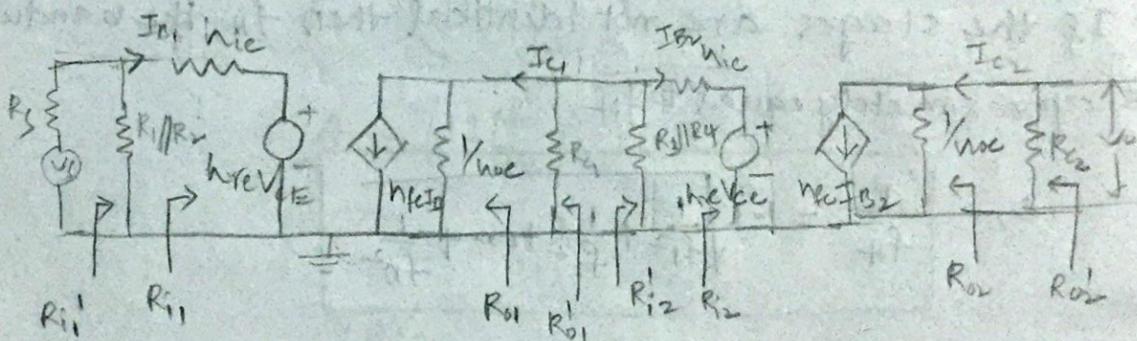
are  $R_S = 1K$ ,  $R_{C1} = 15K\Omega$ ,  $R_{E1} = 100\Omega$ ,  $R_{C2} = 4K\Omega$ ,  $R_{E2} = 330\Omega$

with  $R_1 = 200K\Omega$  and  $R_2 = 20K\Omega$  for first stage.

$R_1 = 4.7K\Omega$  and  $R_2 = 4.7K\Omega$  for second stage. Assume that  $h_{ie} = 1.2K\Omega$ ,  $h_{fe} = 50$ ,  $h_{re} = 2.5 \times 10^{-7}$  and  $h_{oe} = 25 \times 10^6$

The condition for approximate model is  $h_{oe} \cdot R_1 \leq 0.1$

$$h_{oe} \times R_L = 25 \times 10^6 \times 4 \times 10^3 \\ = 100 \times 10^3 \\ = 0.1$$



Second stage Analysis

3/12/2020

The condition  $h_{oe} \times R_L \leq 0.1$  is satisfied so choose the approximate analysis

1. Current gain ( $A_{i2}$ ) =  $-h_{fe} = -50$

2. Input impedance ( $R_{i2}$ ) =  $h_{re} = 1.2K\Omega$

3. Voltage gain ( $A_{V2}$ ) =  $\frac{A_{i2}}{R_{i2}} \times R_L = \frac{-50}{1.2 \times 10^3} \times 4 \times 10^3$

$$\Rightarrow -\frac{500}{3} = -166.6$$

## First stage analysis

$$h_{oc} \cdot R_L' \leq 0.1$$

$$R_L' = R_{C1} \parallel R_{i2}' = R_{C1} \parallel R_1 \parallel R_2 \parallel R_{i2}$$

$$\frac{1}{R_L'} = \frac{1}{15 \times 10^3} + \frac{1}{47 \times 10^3} + \frac{1}{4.7 \times 10^3} + \frac{1}{1.2 \times 10^3}$$

$$\frac{1}{R_L'} = \left( \frac{1}{15} + \frac{1}{47} + \frac{1}{4.7} + \frac{1}{1.2} \right) \frac{1}{10^3}$$

$$\frac{1}{R_L'} = (0.06 + 0.02 + 0.21 + 0.83) \times \frac{1}{10^3}$$

$$R_L' = \frac{1000}{1.12} = 892.85 \approx 0.89 \text{ k}\Omega$$

$$892.9 \times 25 = 0.02$$

1. current gain ( $A_{i1}$ ) =  $-h_{fe} = -50$

2.  $R_{i1} = h_{ie} = 1.2 \text{ k}\Omega$

3. Voltage gain  $A_{v1} = \frac{-50}{1.2 \times 10^3} \times 892 = -37$

Overall voltage gain  $\Rightarrow A_v = A_{v1} \times A_{v2} = 6164.2$

overall current gain  $\Rightarrow A_i = 2500$

overall output impedance  
 $R_{o2} = \infty$

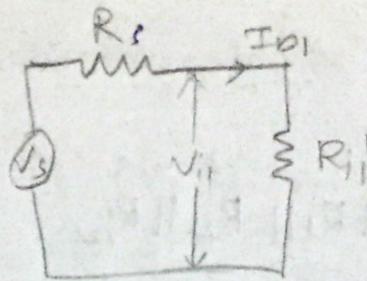
$$R_{o2}' = R_{o2} \parallel R_{C2} = R_{C2} = 4 \text{ k}\Omega$$

overall input impedance  $= R_{i1}' = R_1 \parallel R_2$

Overall voltage gain including source

$$A_{v3} = \frac{V_o}{V_s} = \frac{V_o}{V_{i1}} \times \frac{V_{i1}}{V_s}$$

$$= A_v \times \frac{V_{i1}}{V_s}$$



$$V_{i1} = \frac{V_s \cdot R_{i1}'}{R_{i1}' + R_s}$$

$$\frac{1}{R_{i1}'} = \left( \frac{1}{200} + \frac{1}{20} \right) \frac{1}{10^3}$$

$$\frac{V_{i1}}{V_s} = \frac{0.018}{1000 \cdot 0.018} = 1.8 \times 10^{-5}$$

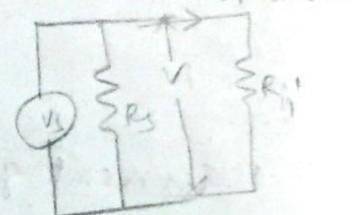
$$\frac{1}{R_{i1}'} = (5 + 50)$$

$$R_{i1}' = \frac{200 \times 20 \times 10^6 / 10^3}{(200+20) \cdot 10^3}$$

$$R_{i1}' = \frac{1}{55} = 0.018$$

$$Av_s = Av \times \frac{V_{i1}}{V_s}$$

$$A_{vS} = \frac{I_2}{I_S} = \frac{I_2}{I_{b1}} \times \frac{I_{b1}}{I_S} = A_v \times \frac{I_{b1}}{I_S}$$



$$I_{b1} = \frac{I_S \cdot R_s}{R_s + R_{i1}'}$$

$$\frac{I_{b1}}{I_S} = \frac{R_s}{R_s + R_{i1}'} = \left( \frac{1}{1+18} \right) \times \frac{10^3}{10^3}$$

$$\frac{I_{b1}}{I_S} = 0.052$$

$$A_{vS} = 2500 \times 0.052 \\ = 130,$$

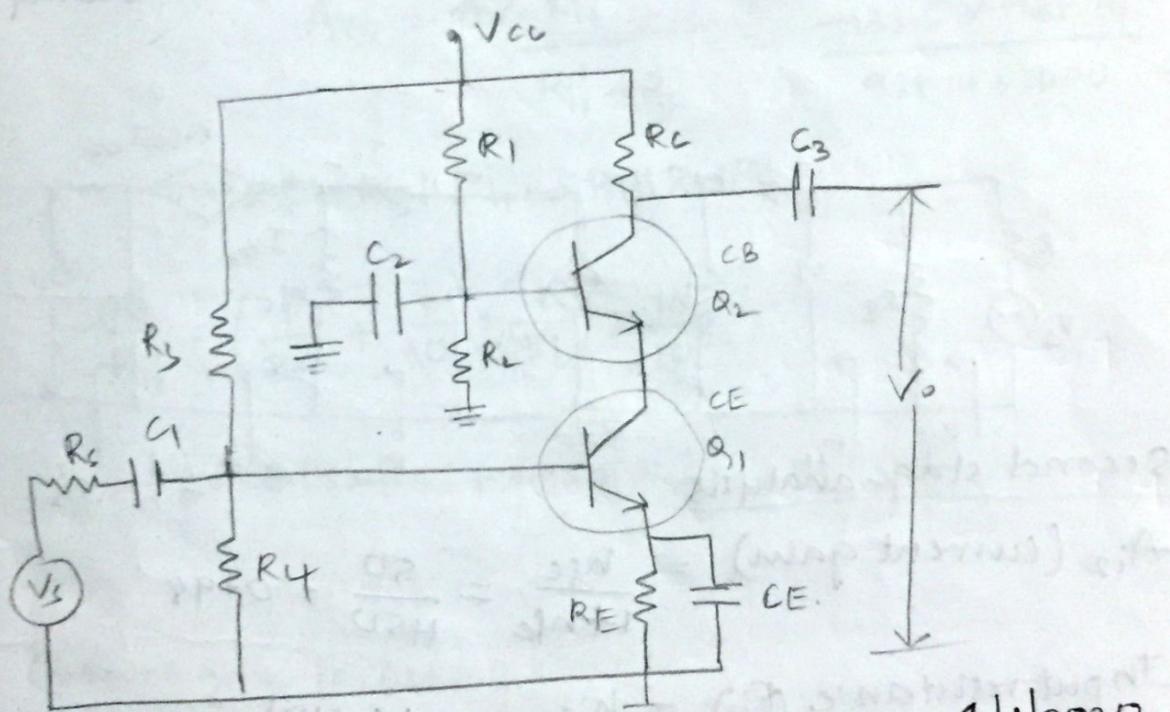
Cascode Amplifier =  $(CE + CB)$  amplifier.

Cascading of CE amplifier with CB amplifier is called as cascode amplifier.

The uses of cascode amplifier is ~~highly~~ input impedance, moderate output impedance, high voltage gain, high bandwidth.

It is used in high frequency and high voltage applications.

Cascode amplifier is ~~CS+CG~~ in case of FETs



4/1/2020

Cascode Analysis

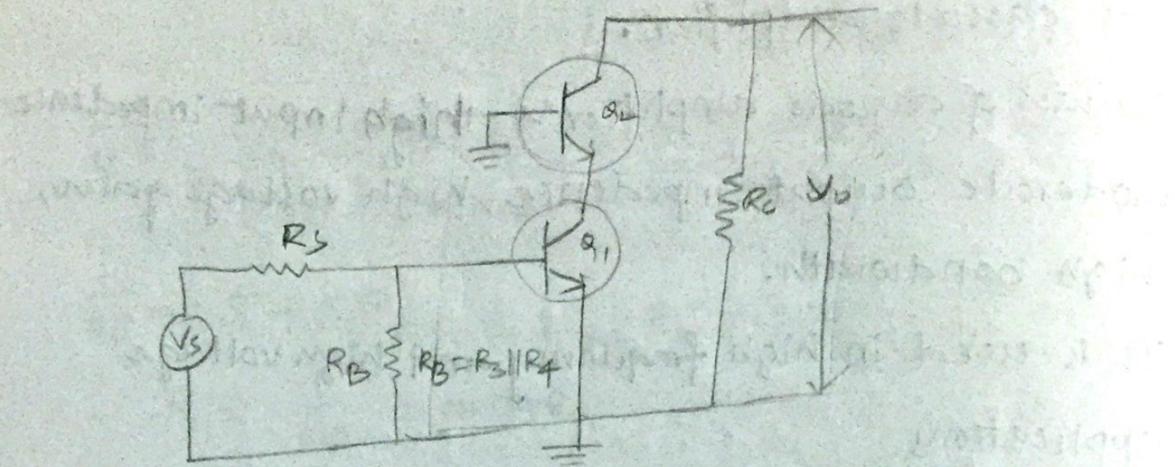
Second stage analysis [CB Amplifier]

Let us consider the circuit parameters are  $R_S = 1K\Omega$ ,

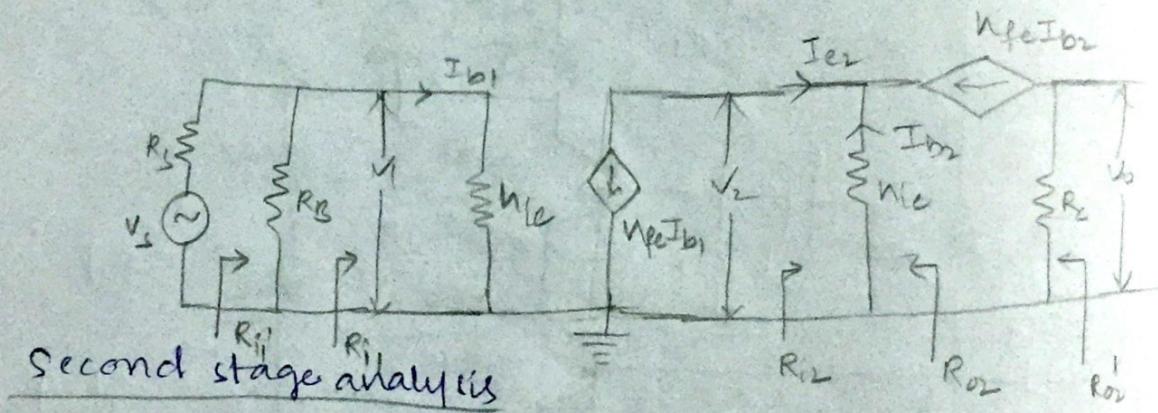
$R_3 = 800K\Omega$ ;  $R_4 = 10K\Omega$  and  $R_L = 12K\Omega$

The transistor parameters for both the transistors are  $N_{fe} = 1.1K$  and  $N_{fe} = 50$

For AC analysis, short all the capacitors, connect the DC power supply to the ground.



$\text{h}_{\text{oe}} \cdot R_L \leq 0.1$  so the approximate analysis is considered.



$$A_{i2} \text{ (current gain)} = \frac{h_{fe}}{1+h_{fe}} = \frac{50}{1+50} = 0.98$$

$$\text{Input resistance } (R_{i2}) = \frac{h_{ie}}{1+h_{fe}} = \frac{1.1 \times 10^3}{51} \Rightarrow 21.5 \Omega$$

$$\text{Voltage gain } (A_{v2}) = \frac{0.98}{21.5} \times 3 \times 10^3 = 136.7$$

$$\text{h}_{\text{oe}} \cdot R_L \Rightarrow 25 \times 10^4 \times 21.5 < 0.1$$

$\downarrow$

$R_{i2}$

$\text{h}_{\text{oe}} \cdot R_L$  value is less than also consider the approximate model for first stage analysis also

## First stage analysis (CE amp)

$$1. A_{i1} = -h_{fe} = -50$$

$$2. R_{i1} = h_{ie} = 1.1 \times 10^3$$

$$3. AV_1 = \frac{A_{i1} R_{i2}}{R_{i1}} = \frac{-50 \times 21.5}{1.1 \times 10^3} = -0.977$$

overall voltage gain  $\Rightarrow AV = AV_1 \times AV_2 \Rightarrow -133.5$

overall current gain  $\Rightarrow A_i = A_{i1} \times A_{i2} \Rightarrow -49$

Voltage gain including source:

$$AV_s = AV \cdot \frac{R_{i1}}{R_{i1}' + R_s} = \frac{-133.5 \times 988.14}{988.14 + 1000}$$

$$R_{i1}' = R_B \parallel R_{i1} = R_1 \parallel R_2 \parallel R_{i1}$$

$$\frac{1}{R_{i1}'} = \left( \frac{1}{300} + \frac{1}{10} + \frac{1}{1.1} \right) \times \frac{1}{10^3}$$

$$\frac{1}{R_{i1}'} = (0.003 + 0.1 + 0.909) \times \frac{1}{10^3} = \frac{1.012}{10^3}$$

$$R_{i1}' = 988.14$$

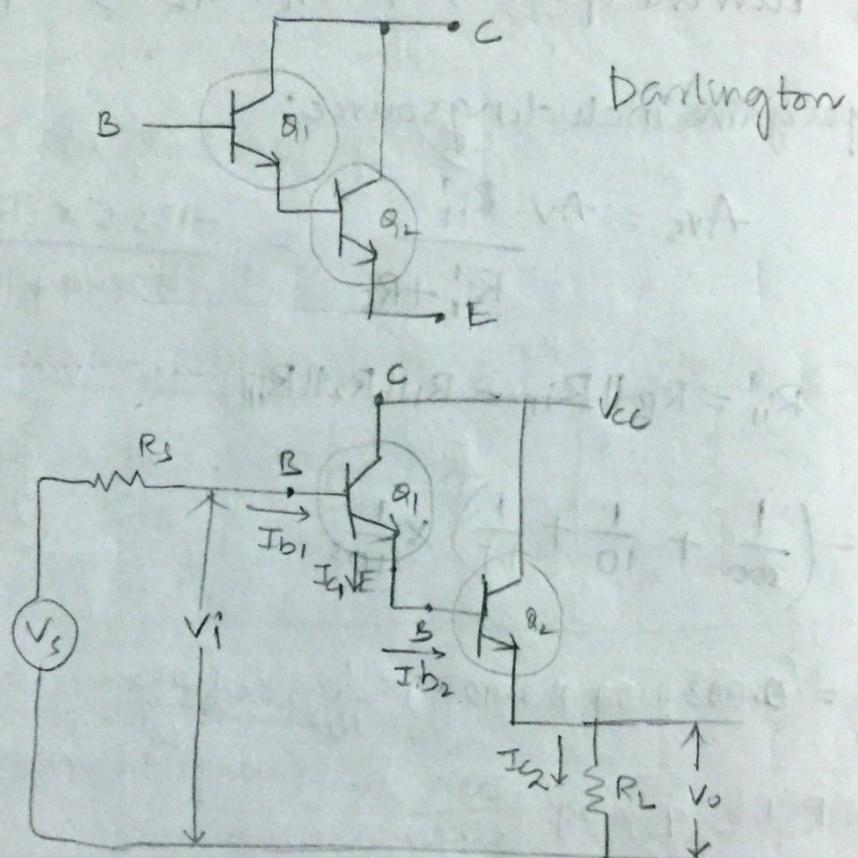
Current gain including source

$$AV_i = \frac{A_i \times R_s}{R_{i1}' + R_s} = \frac{-49 \times 1000}{988.14 + 1000}$$

## Darlington amplifier

The cascading of two emitter followers is called Darlington pair. To increase the input impedance we are following two techniques, they are

1. Direct coupling (Darlington)
2. Bootstrap technique.



cascading of two emitter followers (Darlington pair)

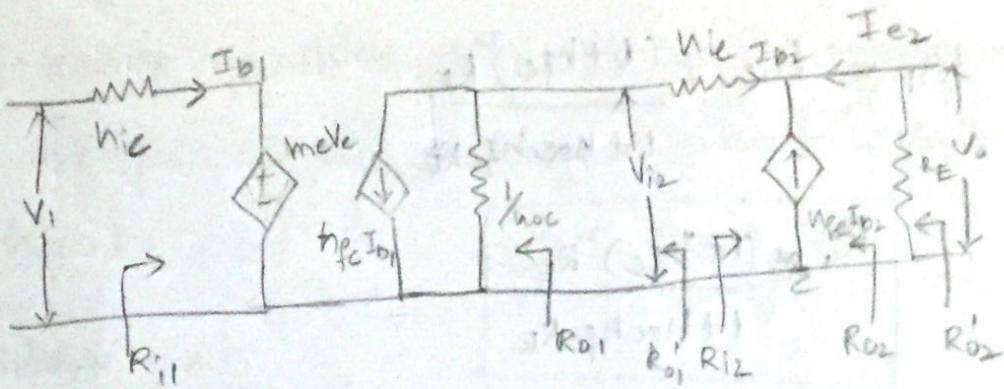
## Analysis of Darlington circuit

6/1/2020

Second stage Analysis (CC Amp)

Assume  $\mu_{OC} \cdot R_L \leq 0.1$  i.e.,  $\mu_{OC} \cdot R_E \leq 0.1$

so choose the approximate model



$$1. \text{ Current gain } (A_{i2}) = 1 + h_{fe}$$

$$2. \text{ Input impedance } (R_{i2}) = h_{ie} + (1 + h_{fe})R_E$$

$$R_{i2} \approx (1 + h_{fe})R_E$$

First stage analysis

$h_{oe} \cdot R_{i2} \leq 0.1$  is not satisfied because the value of  $R_{i2}$  is very high so the exact model is considered.

$$1) \text{ Current gain } (A_{i1}) = \frac{-h_{fe}}{1 + h_{oc}R_{i2}}$$

$$= \frac{(1 + h_{fe})}{1 + h_{oc}(1 + h_{fe})R_E}$$

$$= \frac{(1 + h_{fe})}{1 + h_{oc}(1 + h_{fe})R_E}$$

$$A_{i1} = \frac{(1 + h_{fe})}{1 + h_{oc}h_{fe}R_E}$$

conversion formulae

$$h_{fe} = -(1 + h_{fe})$$

$$h_{oc} = h_{oc}$$

$$h_{ic} = h_{ie}$$

$$h_{re} = 1$$

$$2) \text{ Input resistance } (R_i) = h_{ic} + h_{re}A_{i1}R_{i2}$$

$$= h_{ie} + A_{i1}R_{i2}$$

$$= h_{ie} + \frac{1 + h_{fe}}{1 + h_{oc}h_{fe}R_E} \times (1 + h_{fe})R_E$$

$$R_{i1} = \frac{h_{ie} + (1+h_{fe})^2 R_E}{1+h_{oe}h_{fe}R_E}$$

$$R_{i1} \approx \frac{(1+h_{fe})^2 R_E}{1+h_{oe}h_{fe}R_E}$$

Overall current gain  $A_I = A_{i1} \times A_{i2}$

$$= \frac{1+h_{fe}}{1+h_{oe}h_{fe}R_E} \times (1+h_{fe})$$

$$A_I = \frac{(1+h_{fe})^2}{1+h_{oe}h_{fe}R_E}$$

Now by comparing input resistance and current gain of a single stage emitter follower and Darlington circuit with  $R_E = 4k\Omega$ .

When single stage is considered, the second stage is taken

Single stage (cc)

$$A_{i2} = 1+h_{fe} \\ = 51$$

$$R_{i2} = (1+h_{fe}) R_E \\ = (51) 4k \\ \Rightarrow 204k\Omega$$

Darlington pair (cc+cc)

$$A_I = \frac{(1+50)^2}{1+50 \times 25 \times 4 \times 10^3} = \frac{250000}{1250000} = 200 \\ \Rightarrow 490 \Rightarrow 433.5$$

$$R_I = \frac{(51)^2 \times 4 \times 10^3}{1+25 \times 10^6 \times 4 \times 80 \times 10^3}$$

$$\frac{2500 \times 10^3 \times 4}{1+5} = \frac{10^7}{6} \\ = 1.6M\Omega$$

The above equations of the input resistance and current gain of the darlington circuit is valid for  
 $h_{oc} \cdot R_E \leq 0.1$

### Voltage gain

$$A_V = \frac{A_i R_L}{R_i}$$

$$\begin{aligned} R_i &= h_{ie} + h_{rc} A_i R_L \\ &= h_{ie} + A_i R_L \end{aligned}$$

$$A_i R_L = R_i - h_{ie}$$

$$A_V = \frac{A_i R_L}{R_i} = \frac{R_i - h_{ie}}{R_i} = 1 - \frac{h_{ie}}{R_i}$$

$$A_V = 1 - \frac{h_{ie}}{R_i}$$

$$A_{V1} = 1 - \frac{h_{ie}}{R_{i1}} ; A_{V2} = 1 - \frac{h_{ie}}{R_{i2}}$$

$$A_V = A_{V1} \times A_{V2} = \left[ 1 - \frac{h_{ie}}{R_{i1}} \right] \left[ 1 - \frac{h_{ie}}{R_{i2}} \right]$$

$$= 1 - \frac{h_{ie}}{R_{i2}} - \frac{h_{ie}}{R_{i1}} + \frac{h_{ie}^2}{R_{i1} R_{i2}}$$

$$A_V = 1 - \frac{h_{ie}}{R_{i2}} \quad (R_{i1} \gg R_p)$$

### Output Impedance

7/1/2020

$$R_{O1} = \frac{1}{y_o}$$

$$y_o = h_{oc} - \frac{h_{fc} h_{rc}}{R_s + h_{ic}}$$

$$Y_o = h_{oe} - \left( \frac{1+h_{fe}}{h_{ie}+R_s} \right)$$

$$Y_o = h_{oe} + \frac{1+h_{fe}}{h_{ie}+R_s}$$

$$Y_o = \frac{1+h_{fe}}{h_{ie}+R_s}$$

$$R_{o1} = \frac{1}{Y_{o1}} = \frac{h_{ie}+R_s}{1+h_{fe}}$$

First stage output impedance acts as the source of second stage

$$R_{o2} = \frac{h_{ie}+R_{o1}}{1+h_{fe}}$$

$$R_{o2} = h_{ie} + \frac{\left( \frac{h_{ie}+R_s}{1+h_{fe}} \right)}{1+h_{fe}} \Rightarrow \frac{h_{ie}(1+h_{fe}) + h_{ie}+R_s}{(1+h_{fe})^2}$$

$$R_{o2} = h_{ie} + h_{ie}h_{fe}$$

$$R_{o2} = \frac{h_{ie}}{1+h_{fe}} + \frac{h_{ie}+R_s}{(1+h_{fe})^2}$$

→ output impedance  
of Darlington pair

overall output impedance of Darlington pair

$$\approx R_{o2} \| R_E$$

### Advantages of Darlington circuit-

1. Very high input resistance (in MΩ)
2. Very large current gain.
3. Very low output resistance
4. Voltage gain is less than 1.

5. Darlington pairs are available in a single package with just 3 leads like a transistor.

### Disadvantages

1. In the above analysis we have assumed that the h-parameters of  $Q_1$  and  $Q_2$  are identical but h-parameters for both the transistors will not be same.
2. Leakage current is more, which is not desired.
3. It is not possible to use more than two transistors in the Darlington connection.

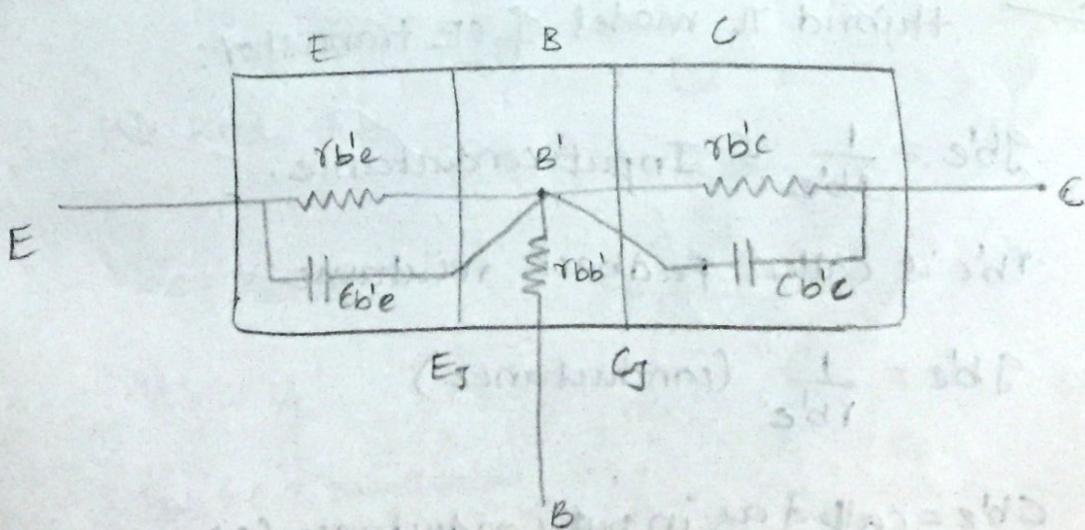
### Hybrid $\pi$ -Model

Hybrid  $\pi$ -Model is suitable for high frequencies.

As the internal capacitors are effecting the gain at high frequencies so h-parameter model is not suitable.

Also the diffusion of electrons is faster at high frequencies  
(diffusion current)

Giacoleto Model is the another name for Hybrid- $\pi$  model



$r_{bb'}$  - Base spreading Resistance

It is the resistance between base and virtual base terminal.

The value of  $r_{bb'}$  is  $100\Omega$

$r_{be}$

It is the resistance between emitter and virtual base.

The value of  $r_{be}$  is  $1k\Omega$

$r_{bc'}$  - Feedback resistance

It is the resistance between collector and virtual base.

The value of  $r_{bc'}$  is  $4M\Omega$

$C_{be}$  - Forward Diffusion capacitance

The value of  $C_{be}$  is  $100PF$

$C_{bc'}$  - Reverse Transition capacitance.

The value of  $C_{bc'}$  is  $3PF$

The values of above parameters are taken at

$$\begin{aligned} T &= 27^\circ C \\ I_C &= 1.3 \text{ mA} \end{aligned} \quad \left. \begin{array}{l} \text{specifications} \\ \text{etc.} \end{array} \right\}$$

8/1/2020

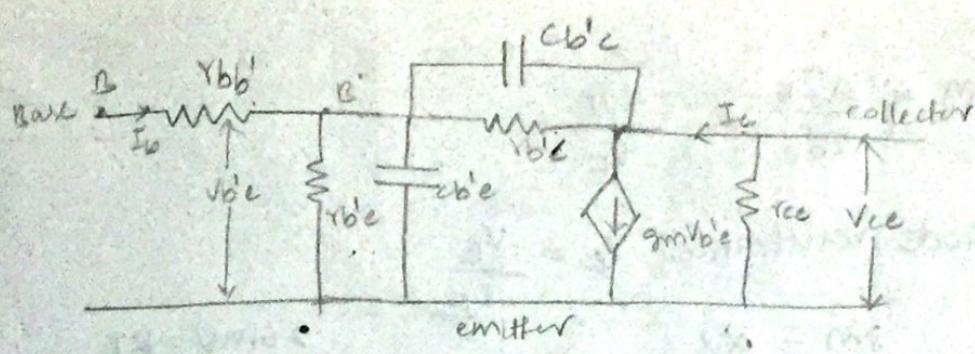
Hybrid  $\pi$ -model of CE transistor:

$$g_{be} = \frac{1}{r_{be}} = \text{Input conductance.}$$

$r_{be}$  is called Feedback resistance

$$g_{be} = \frac{1}{r_{be}} \quad (\text{conductance})$$

$C_{be}$  = called as input conductance ( $C_e$ ) or  $C_\pi$



$gmVbe$  is a current generator, it is equal to collector current  $I_c$ , where  $gm$  is transconductance. It is defined as the ratio of output current to i/p voltage

$$gm = \frac{I_c}{V_{be}}$$

$$I_c = gmVbe$$

i.e. it is the output resistance b/w the collector and emitter.  $Vce$  is very high value  $= 80\text{ k}\Omega$

$$gm = 50 \text{ mA/V}$$

Relationship between high frequency  $\pi$  model and low frequency h-parameter model.

### 1. Transistor Transconductance ( $gm$ )

It is defined as ratio of o/p current to i/p voltage

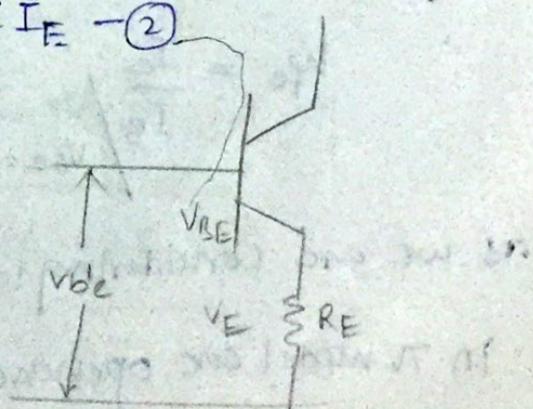
$$\text{i.e., } gm = \frac{I_c}{V_{be}} \quad \text{--- (1)}$$

We know that,  $I_c = \alpha I_E$  --- (2)

$$V_{be} = V_{BE} + V_E$$

$$V_{be} \approx V_E$$

$$\text{as } V_{BE} = 0.7 \text{ (small value)}$$



$$g_m = \frac{\alpha I_E}{V_{be}} = \frac{\alpha I_E}{V_E}$$

Emitter diode resistance,  $r_e = \frac{V_E}{I_E}$

$$g_m = \frac{\alpha}{r_e}$$

$$26mV = kT$$

$V_T = \text{Thermal temperature}$

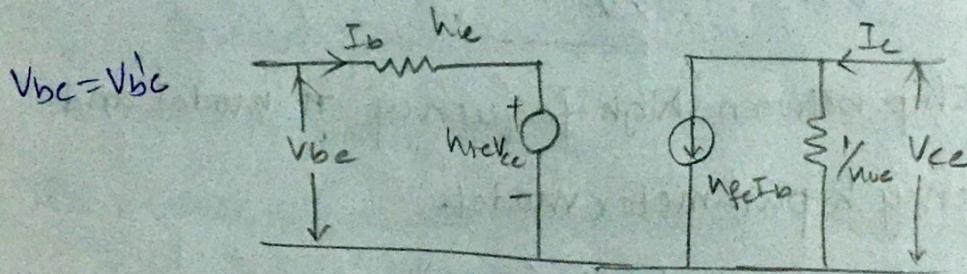
Dynamic resistance of forward bias diode.

$$r_e = \frac{V_T}{I_E}$$

$$g_m = \frac{\alpha I_E}{V_T}$$

$$g_m = \frac{I_E}{V_T} \quad \frac{1.3m}{2.6m} = 80mA/V$$

$V_{be}/g_{be}$ :

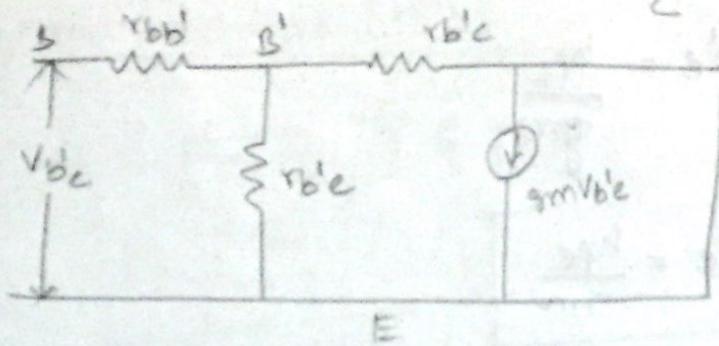


$$V_{be} = h_{ie} I_b + h_{re} V_{ce} \quad \text{---(1)}$$

$$I_c = h_{fe} I_b + h_{re} V_{ce} \quad \text{---(2)}$$

$$h_{fe} = \frac{I_c}{I_B} / V_{ce=0}$$

as we are considering low frequency, all capacitors in  $\pi$  model are open circuited, and  $V_o = 0$

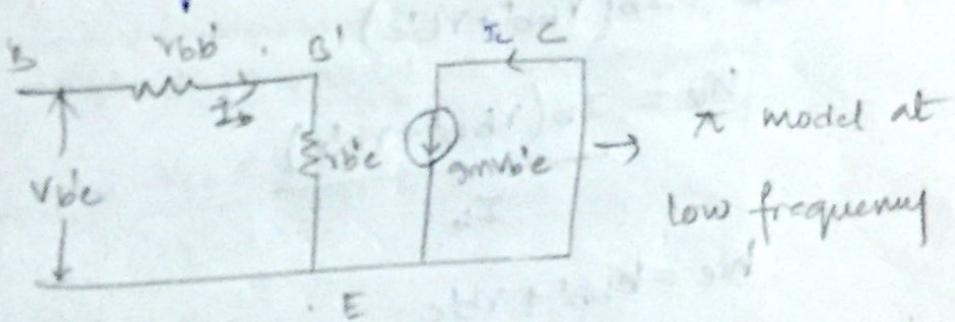


as  $r_{b'e} \gg r_{b'c}$

$r_{b'c} = \infty \rightarrow \text{open circuit}$

If output is short circuited,  $r_{ce}$  is negligible in circuit.

$C_{b'e}, C_{bc}$  internal junction capacitors are open circuited so the equivalent circuit is at low frequency.



$$I_c = g_m V_{b'e}$$

$$V_{b'e} = (r_{bb'} + r_{b'e}) I_b$$

$$r_{bb'} \ll r_{b'e}$$

$$V_{b'e} = r_{b'e} I_b$$

$$I_c = g_m I_b r_{b'e}$$

$$\frac{I_c}{I_b} = \boxed{g_m r_{b'e} = h_{fe}}$$

$$r_{b'e} = \frac{h_{fe}}{g_m}$$

$$r_{b'e} = \frac{h_{fe}}{g_m}$$

Input conductance  $\Rightarrow g_{b'e} = \frac{g_m}{h_{fe}}$

### Base spreading Resistance ( $r_{bb}$ )

$$h_{ie} = \frac{V_{b'e}}{I_b}$$

$$V_{b'e} = I_o(r_{bb'} + r_{b'e})$$

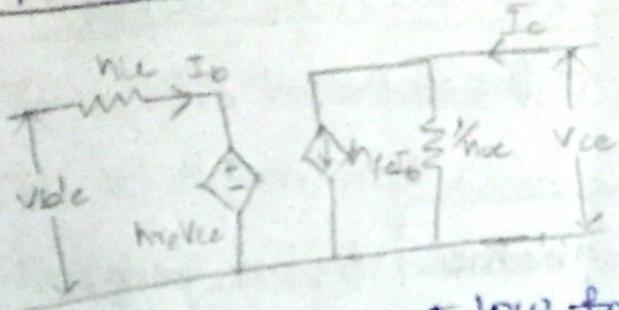
$$h_{ie} = \frac{I_b(r_{bb'} + r_{b'e})}{I_b}$$

$$h_{ie} = r_{bb'} + r_{b'e}$$

$$r_{bb'} = h_{ie} - r_{b'e}$$

## Feedback resistance ( $r_{b'c}$ )

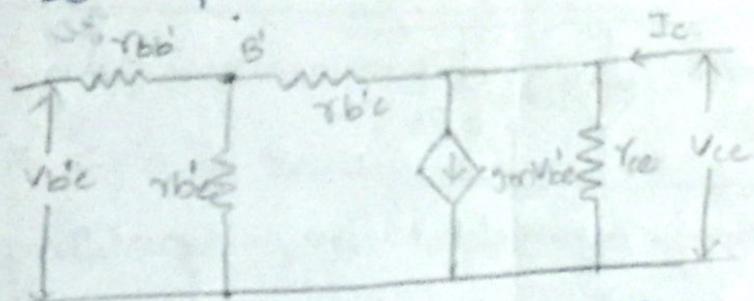
9/11/2020



$h$ -parameter at low frequency

$$v_{be}' = h_{fe}I_b + h_{re}v_{ce}$$

$$I_o' = h_{fe}I_b + h_{re}V_{CB}$$



Hybrid- $\pi$  model at low frequency

$$v_{be}' = \frac{v_{ce} \times r_{be}}{r_{be} + r_{b'c}}$$

$$\frac{v_{be}'}{v_{ce}} = \frac{r_{be}}{r_{be} + r_{b'c}}$$

$$h_{re} = \frac{r_{be}'}{r_{be} + r_{b'c}}$$

$$h_{re}(r_{be} + r_{b'c}) = r_{be}$$

$$h_{re}r_{be} + h_{re}r_{b'c} = r_{be}$$

$$\frac{h_{re}r_{be}}{(1-h_{re})} = r_{b'c}$$

$$r_{b'c} = \frac{r_{be}(1-h_{re})}{h_{re}}$$

$$\Rightarrow \frac{10^3(1 - 2.5 \times 10^{-4})}{2.5 \times 10^{-4}} \Rightarrow \frac{10^3 - 0.25}{2.5 \times 10^{-4}} = 3.99 \text{ M}\Omega \approx 4 \text{ M}\Omega$$

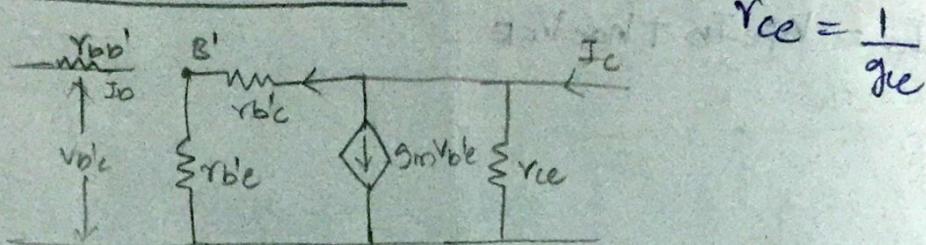
$$r_{b'e} = \frac{r_{be}}{h_{re}}$$

- feedback resistance

$$g_{b'e} = \frac{h_{re}}{r_{be}} = g_{b'e} h_{re}$$

feed conductance

### Output resistance ( $r_{ce}$ )



$$r_{ce} = \frac{1}{g_{ce}}$$

hybrid- $\pi$  model at low frequency

$$I_c = \frac{V_{ce}}{r_{ce}} + g_m V_{be} + \frac{V_{ce}}{r_{be} + r_{b'e}}$$

$$I_c = V_{ce} \left[ \frac{1}{r_{ce}} + \frac{g_m V_{be}}{V_{ce}} + \frac{1}{r_{be} + r_{b'e}} \right] \quad [g_m = h_{fe} = \frac{g_{b'e}}{r_{be}}]$$

$$I_c = V_{ce} \left[ \frac{1}{r_{ce}} + \frac{g_m V_{be}}{V_{ce}} + \frac{1}{r_{be} + r_{b'e}} \right]$$

$$\frac{I_c}{V_{ce}} = g_{ce} + h_{fe} g_{b'e} h_{re} + g_{b'e}$$

$r_{b'e} \gg r_{be}$

$$h_{oe} = g_{ce} + h_{fe} g_{b'e} \frac{g_{b'e}}{g_{b'e}} + g_{b'e} \left[ h_{re} = \frac{g_{b'e}}{g_{b'e}} \right]$$

$$h_{oe} = g_{ce} + g_{b'e} h_{fe} + g_{b'e}$$

$$h_{oe} = g_{ce} + g_{b'e} (1 + h_{fe})$$

$$g_{ce} = h_{oe} - g_{b'e} h_{fe} = \frac{1}{V_{ce}} = \frac{1}{80 \text{ k}\Omega}$$

## Diffusion capacitance [Cb'e]

It is also represented as  $C\pi$  in hybrid  $\pi$ -model  
 $C_{b'e}$  is determined from a measurement of  $f_T$ ,  
the frequency at which the CE short circuit current  
gain drops to unity. It is given by

$$C_{b'e} = \frac{g_m}{2\pi f_T} = C\pi$$

## Transition capacitance [Cb'c]

It is also represented as  $C_\mu$  in hybrid  $\pi$  model  
 $C_\mu = C_{b'c}$  is measured as  $\text{CB output}$   
 $\text{capacitance}$  with input open and is usually  
specified by manufacturer as  $C_{OB} \rightarrow \text{open circuit}$   
Base capacitance

$$g_m = \frac{I_c}{V_T} = 50 \text{ mA/V}$$

$$\frac{1}{g_{b'e}} = r_{b'e} = \frac{h_{fe}}{g_m} = 1K\Omega$$

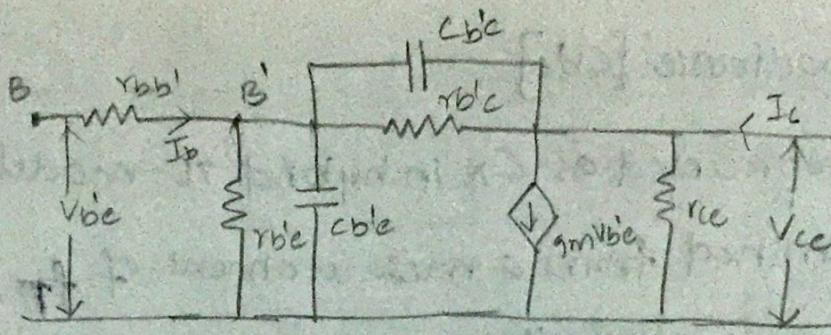
$$r_{bb'} = h_{ie} - r_{b'e} = 100\Omega$$

$$\frac{1}{g_{b'c}} = r_{bc} = 4M\Omega = \frac{r_{b'e}}{h_{re}}$$

$$g_{ce} = h_{oe} - g_{b'c}h_{fe} = \frac{1}{r_{ce}} = \frac{1}{80K}$$

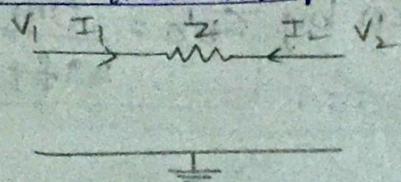
$$C_{b'e} = C\pi = \frac{g_m}{2\pi f_T}$$

$$C_\mu = C_{b'c}$$



Hybrid -  $\pi$  model

Miller's Theorem:



$$Z_1 = \frac{Z}{1 - Av}$$

$$Z_2 = \frac{Z Av}{Av - 1}$$

$$I_1 = \frac{V_1 - V_2}{Z} = \frac{V_1(1 - \frac{V_2}{V_1})}{Z}$$

$$\frac{I_1}{V_1} = \frac{-Av}{Z} \Rightarrow Z_1 = \frac{Z}{1 - Av}$$

$$I_2 = \frac{V_2 - V_1}{Z} = \frac{V_2(1 - \frac{V_1}{V_2})}{Z} = \frac{V_2(Av - 1)}{Z Av}$$

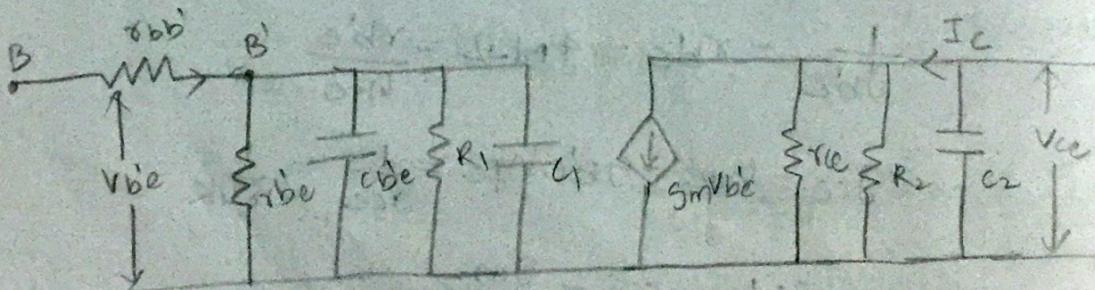
$$Z_2 = \frac{V_2}{I_2} = \frac{Z Av}{Av - 1}$$

Assignment

Derive Miller's Theorem, duals of Miller's theorem and

Miller effect capacitance , with examples..

figure can be modified by using Miller's theorem



Hybrid-pi model using Miller's theorem

$$R_1 = \frac{r_{b'}c}{1 - Av}$$

$$G = C_{bc}(1 - Av)$$

$$R_2 = \frac{r_{b'}c Av}{Av - 1}$$

$$C_2 = C_{bc}\left(1 - \frac{1}{Av}\right)$$

## C.E short circuit current gain at high frequencies.

short circuit current gain means output terminals are short circuited.

If the output terminals are short circuited,  $r_{ce}$ ,  $R_2$  and  $C_2$  are not considered.

10/1/2020

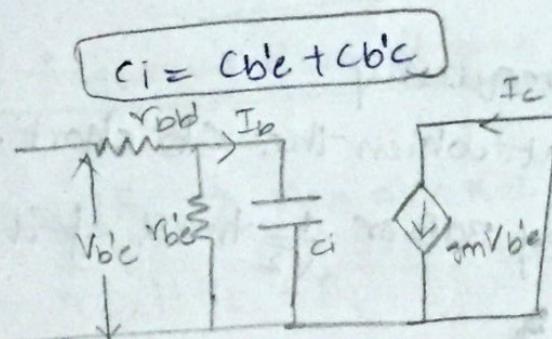
### (CE short circuit current gain at high frequency):

$r_{ce}$  becomes zero so it is neglected because o/p terminals are short circuited

$r_{be}'$  is parallel to  $R_1 \Rightarrow r_{be}' \parallel R_1 \approx r_{be}'$

$$c_i = r_{be}' + C_1$$

$$= r_{be}' + C_{bc}(1 - A_v)$$



$$A_i = \frac{I_L}{I_b} = \frac{-I_c}{I_b} = \frac{-g_m V_{be}'}{I_b}$$

$$I_b = V_{be}' \left[ \frac{1}{r_{be}'} + \frac{1}{j\omega C_i} \right]$$

$$I_b = V_{be}' \left[ \frac{1}{r_{be}'} + j\omega C_i \right]$$

$$A_i = \frac{-g_m V_{be}'}{I_b} = \frac{-g_m V_{be}'}{V_{be}' \left[ \frac{1}{r_{be}'} + j\omega C_i \right]}$$

$$A_i = \frac{-g_m r_{be}'}{1 + j\omega r_{be}' C_i}$$

$$A_i = \frac{-\beta}{1 + j 2\pi f r b_e c_i} \quad [ \because h_{fe} = \beta = g_m r b_e ]$$

$$A_i = \frac{-\beta}{1 + j \frac{\beta}{f_p}} \quad \text{where } f_p = \frac{1}{2\pi R b_e c_i}$$

$$|A_i| = \frac{\beta}{\sqrt{1 + \left(\frac{\beta}{f_p}\right)^2}} \quad \beta \text{ cutoff frequency}$$

$$\text{If } f = f_p \text{ then } |A_i| = \frac{\beta}{\sqrt{2}}$$

$f_p$  - It is a frequency at which the CE short circuit current gain drops by 3dB or  $\frac{1}{\sqrt{2}}$  times of its value at low frequency.

$f_A$  -  $\alpha$  cut off frequency

It is a frequency at which the CB short circuit current gain drops by 3dB or  $\frac{1}{\sqrt{2}}$  times of its value at low frequency.

$$f_A = \frac{1 + h_{fe}}{2\pi R b_e c_i \alpha}$$

Unity gain frequency ( $f_T$ )

It is a frequency at which the CE short circuit current gain becomes unity. Hence it is called unity gain frequency (or) Bandwidth

$$f_T = \beta f_p$$

Relation b/w - unity gain frequency ( $f_T$ ) and  
 $\beta$ -cutoff frequency ( $f_B$ )

The unity gain frequency ( $f_T$ ) is the product of low frequency current gain ( $\beta/\alpha_{FE}$ ) and  $\beta$ -cutoff frequency at high frequency.

$$f_T = \beta f_B$$

$$= \alpha_{FE} \times \frac{1}{2\pi r_b' e C_1}$$

$$= \frac{g_m r_b' e}{2\pi r_b' e C_1} = \frac{g_m}{2\pi (C_{b'e} + C_{b'c})}$$

$$f_T = \frac{g_m}{2\pi C_{b'e}}$$

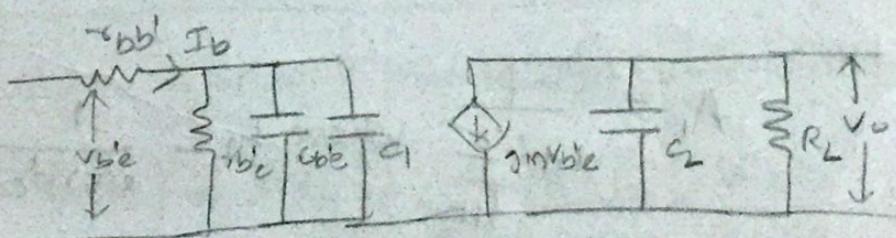
$$\Rightarrow C_{b'e} = \frac{g_m}{2\pi f_T}$$

High frequency current gain with resistive load

$$r_{ce} \parallel R_L \rightarrow r_{ce} = 80 \text{ k}\Omega \quad \text{neglect } r_{ce}$$

$$r_{ce} \parallel R_L = R_L$$

$$r_{b'e} \parallel R_i = r_{b'c}$$



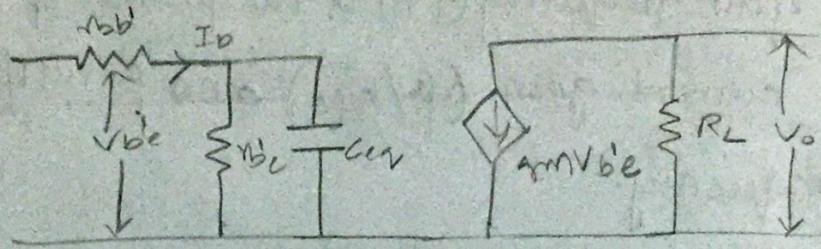
$$C_1 = C_{b'c} (1 - A_v)$$

$$A_v = \frac{v_o}{v_{b'e}} = -\frac{g_m V_{b'e} R_L}{v_{b'e}} = g_m R_L$$

$$C_1 = C_{b'c} (1 + g_m R_L)$$

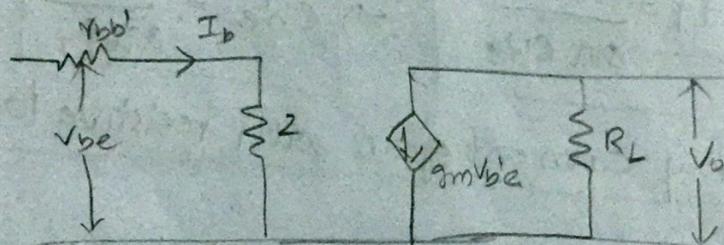
$$C_{eq} = C_{b'e} + C_{b'c}(r + g_m R_L)$$

$$C_A = C_{b'c} \left(1 - \frac{1}{A_V}\right) \approx C_{b'c}$$



$$Z = r_{b'e} \parallel \frac{1}{j\omega C_{eq}} = \frac{r_{b'e} \times \frac{1}{j\omega C_{eq}}}{r_{b'e} + \frac{1}{j\omega C_{eq}}}$$

$$Z = \frac{r_{b'e}}{1 + j\omega r_{b'e} C_{eq}}$$



$$A_i = -\frac{I_c}{I_b} = -\frac{g_m V_{be}}{I_b} = -g_m Z$$

$$= -g_m \left( \frac{r_{b'e}}{1 + j\omega r_{b'e} C_{eq}} \right)$$

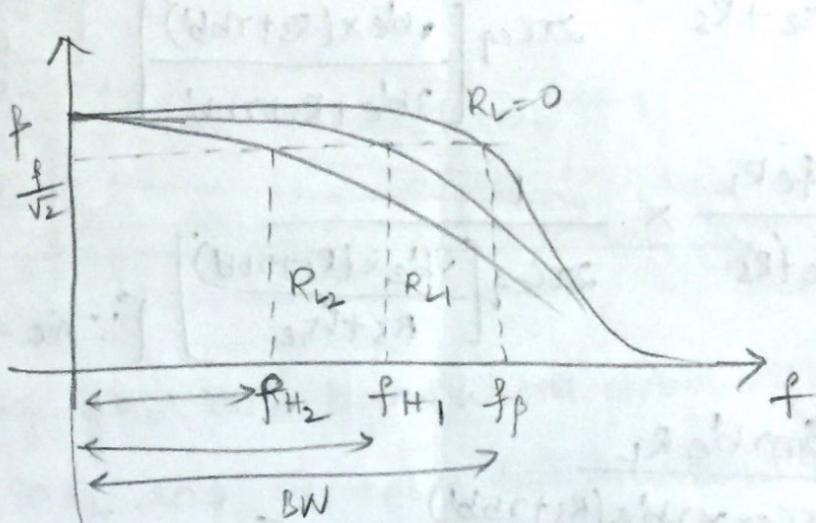
$$A_i = \frac{-f}{1 + j\frac{f}{f_H}} \quad \text{where } f_H = \frac{1}{\pi r_{b'e} C_{eq}}$$

$$|A_i| = \frac{f}{\sqrt{1 + \left(\frac{f}{f_H}\right)^2}} \quad \text{if } f = f_H \Rightarrow |A_i| = \frac{f}{\sqrt{2}}$$

- $f_{H1}$  is the higher cutoff frequency at which the CE current gain drops by  $\frac{1}{\sqrt{2}}$  or 3dB from its value.

$$f_H = \frac{1}{2\pi r b'_e [cbe + cb'c(1+gmR_L)]}$$

$$f_p = \frac{1}{2\pi c b'_e (cb'e + cb'c)} \quad \text{with } R_L = 0$$



If the load increases, Bandwidth decreases.

The max possibility of  $f_H$  (Bandwidth) is  $f_p$  as  $R_L$  increases the  $c$  equivalent capacitance increases so that bandwidth decreases.

### Gain and Bandwidth product:

i) Voltage gain with source and Bandwidth product

$$|Av_s| = Av \cdot \frac{R_i'}{R_i' + R_s} = \frac{A_i R_L}{Nie} \times \frac{Nie}{Nie + R_s} = \frac{A_i R_L}{Nie + R_s}$$

$$f_H = \frac{1}{2\pi R_{eq} C_{eq}}$$

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$$|A_{VS} \times F_H|$$

$$= |A_{VS} \times F_H| = \frac{A_V \cdot R_I}{R_I + R_S} \times \frac{1}{2\pi C_{eq} C_{eq}}$$

$$= \frac{A_I R_L}{R_I} \times \frac{R_I}{R_I + R_S} \times \frac{1}{2\pi C_{eq} [r_{be} \| (R_S + r_{bb'})]}$$

$$= \frac{h_{fe} R_L}{h_{ie} + R_S} * \frac{1}{2\pi C_{eq} \left[ \frac{r_{be} \times (R_S + r_{bb'})}{r_{be} + R_S + r_{bb'}} \right]}$$

$$= \frac{h_{fe} R_L}{h_{ie} + R_S} \times \frac{1}{2\pi C_{eq} \left[ \frac{r_{be} \times (R_S + r_{bb'})}{R_S h_{ie}} \right]} \quad [\because h_{ie} = r_{be} + r_{bb'}]$$

$$= \frac{g_m r_{be} R_L}{2\pi C_{eq} \times r_{be} (R_S + r_{bb'})} \quad [\because h_{fe} = g_m r_{be}]$$

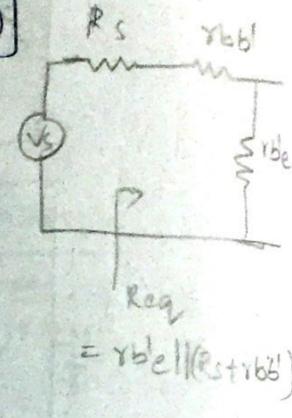
$$= \frac{g_m}{2\pi (C_{be} + C_{bc} (1 + g_m R_L))} \times \frac{R_L}{R_S + r_{bb'}}$$

$$= \frac{2\pi f_T C_{be}}{2\pi [C_{be} + C_{bc} 2\pi f_T C_{be} R_L]} \times \frac{R_L}{R_S + r_{bb'}}$$

$$= \frac{2\pi f_T C_{be}}{2\pi [C_{be} + C_{bc} 2\pi f_T C_{be} R_L]} \times \frac{R_L}{R_S + r_{bb'}}$$

$$(A_{VS} \times f_H) = \frac{2\pi f_T C_{be}}{2\pi C_{be} [1 + 2\pi f_T C_{bc} R_L]} \times \frac{R_L}{R_S + r_{bb'}}$$

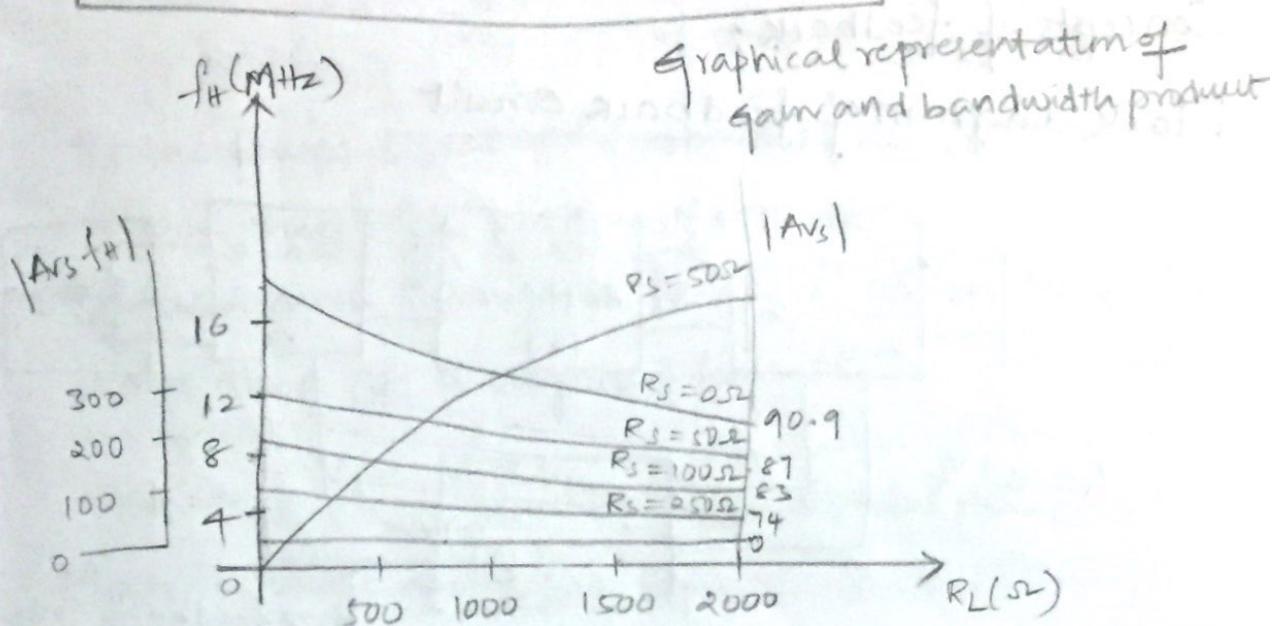
$$|A_{VS} \times F_H| = \frac{f_T}{1 + 2\pi f_T C_{bc} R_L} \times \frac{R_L}{R_S + r_{bb'}}$$



$$= r_{be} \| (R_S + r_{bb'})$$

Similarly for, product of current gain and bandwidth

$$|A_{IS} \times f_H| = \frac{f_T}{1 + 2\pi f_T C b' c R_L} \times \frac{R_S}{R_S + r_{bb'}}$$



→ The voltage gain and band width product increases with increase in  $R_L$  and decreases with increase in  $R_S$ .

Therefore we can say that the gain-bandwidth product is not constant but it depends on values of  $R_L$  and  $R_S$ .