GATE 2023[IN]-36

EE23BTECH11066 - Yakkala Amarnath Karthik

Question:

The impulse response of an LTI system is $h\left(t\right)=\delta\left(t\right)+0.5\delta\left(t-4\right)$, where $\delta\left(t\right)$ is continuous-time unit impulse signal.if the input signal $x(t)=\cos\left(\frac{7\pi t}{4}\right)$,the output is (GATE IN 2023)

Solution:

Variable	Description	value
$\delta\left(t\right)$	continuous-time unit impulse signal	1 if t=0; 0 in other cases
$h\left(t\right)$	impulse response	$\delta\left(t\right)+0.5\delta\left(t-4\right)$
$x\left(t\right)$	input signal	$x(t)=\cos\left(\frac{7\pi t}{4}\right)$
$y\left(t\right)$	output signal	x(t)∗ h(t)

TABLE I

A Table with input parameters

from Table I

$$y\left(t\right)=x\left(t\right)*h\left(t\right) \tag{1}$$

$$=x\left(t\right)*\left(\delta\left(t\right)+0.5\delta\left(t-4\right)\right) \tag{2}$$

$$=x\left(t\right)+0.5x\left(t-4\right) \tag{3}$$

$$=\cos\left(\frac{7\pi t}{4}\right)+0.5\cos\left(\frac{7\pi\left(t-4\right)}{4}\right) \tag{4}$$

$$=\cos\left(\frac{7\pi t}{4}\right)+0.5\cos\left(\frac{7\pi t}{4}-7\pi\right) \tag{5}$$

$$=0.5\cos\left(\frac{7\pi t}{4}\right) \tag{6}$$

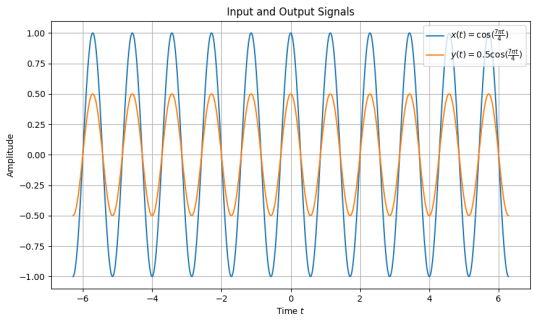

Fig. 1. Graph showing first 8 terms of the GP