## GATE 2023[IN]-36

## EE23BTECH11066 - Yakkala Amarnath Karthik

## Question:

The impulse response of an LTI system is  $h(t) = \delta(t) + 0.5\delta(t-4)$ , where  $\delta(t)$  is continuous-time unit impulse signal if the input signal  $x(t) = \cos\left(\frac{7\pi t}{4}\right)$ , the output is (GATE IN 2023)

## Solution:

Variable	Description	value
$\delta\left(t\right)$	continuous-time unit impulse signal	1 if t=0;
		0 in other cases
$h\left(t\right)$	impulse response	$\delta\left(t\right) + 0.5\delta\left(t - 4\right)$
x(t)	input signal	$x(t) = \cos\left(\frac{7\pi t}{4}\right)$
$y\left(t\right)$	output signal	x(t)* h(t)
TABLE I		

A TABLE WITH INPUT PARAMETERS

from Table I

$$y(t) = x(t) * h(t)$$

$$= x(t) * (\delta(t) + 0.5\delta(t - 4))$$

$$= x(t) + 0.5x(t - 4)$$

$$= \cos\left(\frac{7\pi t}{4}\right) + 0.5\cos\left(\frac{7\pi(t - 4)}{4}\right)$$
(4)

$$= \cos\left(\frac{7\pi t}{4}\right) + 0.5\cos\left(\frac{7\pi t}{4} - 7\pi\right) \tag{5}$$

$$=0.5\cos\left(\frac{7\pi t}{4}\right)\tag{6}$$

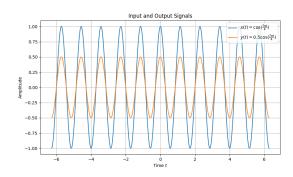


Fig. 1. Graph showing x(t) and y(t)