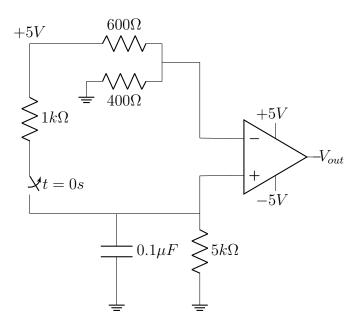
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GATE 2022[IN]-64

EE23BTECH11066 - Yakkala Amarnath Karthik

Question:

In the circuit shown, the switch is initially closed. It is opened at t=0 s and remains open thereafter. The time (in milliseconds) at which the output voltage V_{out} becomes LOW is (round off to three decimal places)



Solution:

At $t=0^-$, when the switch is closed, The voltage across the capacitor is:

$$V_c\left(0^-\right) = 5 * \frac{5}{5+1}$$

$$= \frac{25}{6}V$$
(2)

 $V_{c}\left(0^{-}\right)$ is also the non inverting voltage of the OP-AMP

At $t = 0^+$, when the switch is open, The voltage across inverting terminal is:

$$V_I = 5 * \frac{600}{600 + 400} \tag{3}$$

$$=2V\tag{4}$$

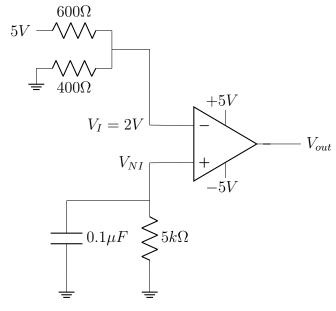


Fig. 1. circuit diagram at $t = 0^+$

Immediately after the switch is open, voltage across capacitor do not change.

So $V_{NI} > V_I$, Hence the output of OP-AMP is fixed to +5V. Later, Capacitor discharges into $5K\Omega$ resistor.

The discharging equation is as follows:

$$V_C(t) = V_C(0^-) e^{\frac{-t}{\tau}}$$
(5)

$$2 = \frac{25}{6} * e^{\frac{t_0}{RC}} \tag{6}$$

$$t = RC \ln \left(\frac{25}{12}\right) \tag{7}$$

$$= 0.1 * 10^{-6} * 5 * 10^{3} \ln \left(\frac{25}{12}\right)$$
 (8)

$$t = 0.367ms \tag{9}$$