

MF-Homework

November 30, 2024

1 Matrix Factorization

In this task you are supposed to (manually) implement the matrix factorization variant you learned in the Data Cleaning chapter using the `numpy` library.

```
[108]: import numpy as np
```

We continue the scenario from the tutorials.

Assume that you have a ginormous database D of three users and three movies and ratings provided by some users to some movies, which we represent as a matrix, where the entry D_{ij} represents the rating user i gave to movie j . Since not all users have rated movies, and the rating ranges from 1 to 5, we encode missing ratings as 0.

```
[109]: # missing values encoded as 0
D = [
    [3,1,0],
    [1,0,3],
    [0,3,5],
]
D = np.array(D)

N = len(D)
M = len
```

First, randomly initialize the two factors E and A for $f = 2$ latent features. For evaluating the correctness of your results from the tutorial, you may *additionally* provide hard-coded initial factors as they have been provided in the tutorial.

```
[110]: # number of latent features
f = 2

E = np.random.rand(len(D), f)
A = np.random.rand(f, len(D[0]))

print(E)
print(A)
```

```
[[0.17090442 0.67335086]
 [0.1718979  0.93930908]]
```

```

[0.82030736 0.85955506]]
[[0.09847075 0.69015436 0.19238301]
 [0.19110697 0.25447107 0.70284467]]

```

Implement a function that takes the data matrix D , the initial factors E, A , the number of epochs (iterations), the learning rate η , and performs the factorization of D . Use a default number of 5000 for the epochs and 0.001 for η .

Updates to E and A are applied immediately. \tilde{D} is updated after an entry from D was completely dealt with. Update ordered by latent features and E before A .

```

[111]: def train(D: np.ndarray, E: np.ndarray, A: np.ndarray, learning_rate: float = 0.
        ↪001, epochs: int = 5000) -> list[float]:
        temp = []
        for _ in range(epochs):
            Dt = np.matmul(E, A)

            # calculate the sse-gradient
            d_sse = 2*(D - Dt)

            # calculate the Summed-Squared-Error to visualize an error-curve later.
            sse = 0
            for i in range(len(D)):
                for j in range(len(D)):
                    if D[i][j] != 0:
                        sse += (D[i][j] - Dt[i][j])**2
                        # parameter updates on every latent factor as well a with_
        ↪epoch size 1
                        for k in range(f):
                            # hmm shouldn't there be a way to update all parameters_
        ↪by directly doing matrix multiplication?
                            E[i][k] = E[i][k] + learning_rate * d_sse[i][j] *_
        ↪A[k][j]
                            A[k][j] = A[k][j] + learning_rate * d_sse[i][j] *_
        ↪E[i][k]
                            #print(sse)
                            temp.append(sse)
        return temp

```

Now test your matrix factorization for the parameters specified above.

```

[112]: # "DEA" lmao
errors = train(D, E, A)
print(np.matmul(E, A))

import matplotlib.pyplot as plt

plt.title("Gradient decent matrix factorization")
plt.plot(errors)

```

```
plt.xlabel("epochs")  
plt.ylabel("summed square error")  
plt.legend(["error with learning rate 0.001"])  
plt.show()
```

```
[[2.9992587  1.00006906 6.42077004]  
 [1.0021269  1.39268882 2.99914167]  
 [1.37862299 2.99988207 5.00021907]]
```

