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COMPS – C31

ML Experiment 6

ML - Experiment 6

Aim: To implement Back propagation

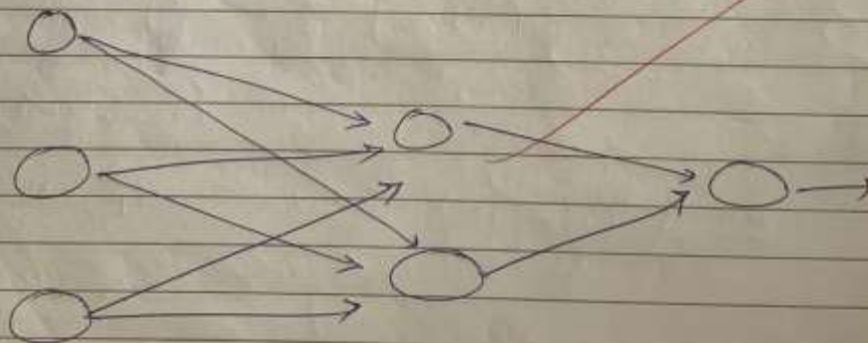
Theory

Back propogtⁿ is an algorithm that Back Propogates the errors from the output nodes to input nodes

It is widely used Algorithm for training feed forward neural networks

It computes the gradient of loss function with respect to the network weights

It is very efficient, rather than naively directly computing the gradient concerning each weight



Parameters:

x = inputs training Vector (x_1, x_2, \dots, x_n)

t = target ~~of~~ vector (t_1, t_2, \dots, t_c)

S_n = error at output unit

δ_j = error at hidden layer

α = learning rate

V_{oj} = bias of hidden unit j

conclusion: Thus, we implemented back propagation

Implementation:

```
import numpy as np
class NeuralNetwork:
    def __init__(self, input_size, hidden_size, output_size):
        self.input_size = input_size
        self.hidden_size = hidden_size
        self.output_size = output_size
        # Initialize weights and biases
        self.weights_input_hidden = np.random.randn(self.input_size,
            self.hidden_size)
        self.bias_input_hidden = np.random.randn(1, self.hidden_size)
        self.weights_hidden_output = np.random.randn(self.hidden_size,
            self.output_size)
        self.bias_hidden_output = np.random.randn(1, self.output_size)
    def sigmoid(self, x):
        return 1 / (1 + np.exp(-x))
    def sigmoid_derivative(self, x):
        return x * (1 - x)
    def forward(self, inputs):
        self.hidden_input = np.dot(inputs, self.weights_input_hidden) +
            self.bias_input_hidden
        self.hidden_output = self.sigmoid(self.hidden_input)
        self.final_input = np.dot(self.hidden_output,
            self.weights_hidden_output) + self.bias_hidden_output
        self.final_output = self.sigmoid(self.final_input)
        return self.hidden_output, self.final_output
    def backward(self, inputs, targets, learning_rate):
        error = targets - self.final_output
        delta_output = error * self.sigmoid_derivative(self.final_output)
        delta_hidden = np.dot(delta_output, self.weights_hidden_output.T) *
            self.sigmoid_derivative(self.hidden_output)
        self.weights_hidden_output += np.dot(self.hidden_output.T,
            delta_output) * learning_rate
        self.bias_hidden_output += np.sum(delta_output, axis=0,
            keepdims=True) * learning_rate
        self.weights_input_hidden += np.dot(inputs.T, delta_hidden) *
            learning_rate
        self.bias_input_hidden += np.sum(delta_hidden, axis=0,
            keepdims=True) * learning_rate
    def train(self, inputs, targets, learning_rate):
        hidden_output, final_output = self.forward(inputs)
        error = self.backward(inputs, targets, learning_rate)
        print("Output of hidden layer:")
        print(hidden_output)
        print("Output of output layer:")
        print(final_output)
        print("Error found:")
        print(error)
        print("Updated weights after 1 iteration:")
        print("Weights from input to hidden layer:")
        print(self.weights_input_hidden)
        print("Weights from hidden to output layer:")
        print(self.weights_hidden_output)
```

```
dataset = pd.read_csv('reduced_digits_dataset.csv')
inputs = dataset.drop(columns=['target']).values
targets = dataset['target'].values.reshape(-1, 1)
input_size = inputs.shape[1]
output_size = len(np.unique(targets))
hidden_size = 3
nn = NeuralNetwork(input_size, hidden_size, output_size)
nn.train(inputs, targets, learning_rate=0.1)
```