



**Lab Project:  
Hot n' Cold Rubidium**  
Under Supervision of Dr. Pablo Solano Palma  
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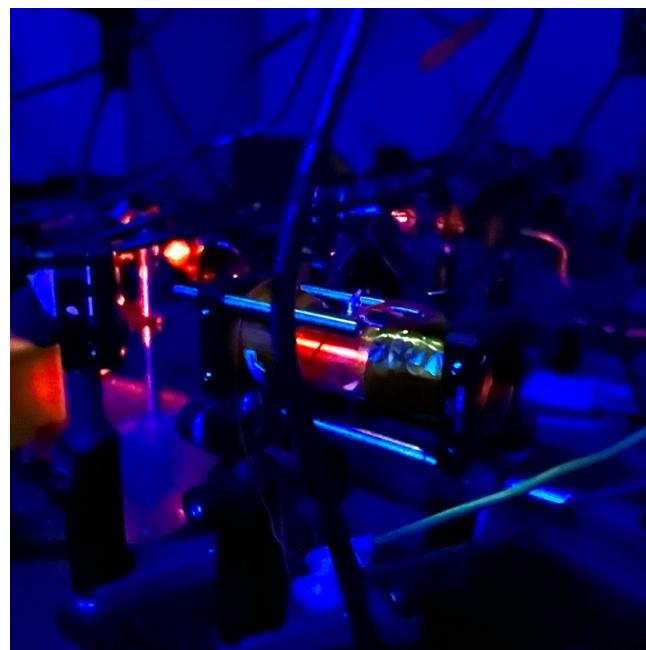


Figure 1: sayans!



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## Summary

The main objective of this project is to study and manipulate the index of refraction of a Rubidium vapour through the interaction with laser light of two different wavelengths. Using a theoretical, numerical and experimental approach, we aim to understand and characterize the Rubidium vapour and the effects of light interacting with this system. The project will be divided into three main stages: theoretical study, numerical simulations, and experimental validation. The theoretical study will focus on the fundamentals of atomic quantum optics, with emphasis on the interaction between light and matter. The numerical simulations will be used to model the interaction between light and Rubidium vapour, and to predict the behaviour of the system under different conditions. Finally, the experimental validation will involve the construction of an experimental setup to measure the index of refraction of the Rubidium vapour and compare the results with the theoretical and numerical predictions. The expected results of this project include a better understanding of the interaction between light and matter, and the development of new techniques for manipulating the index of refraction of Rubidium vapour. This research has the potential to **be a MOT...**

As a note, we will reference and quote the work of Arina Tashchilina (found here!) who has provided an amazing source for new students hoping to learn about experimental atomic physics.



## Rubidium

Rubidium is a soft, ductile alkali metal, composed naturally of two stable isotopes,  $^{85}\text{Rb}$  and  $^{87}\text{Rb}$ , in the following ratio; 72.15% corresponds to  $^{85}\text{Rb}$  and 27.85% to  $^{87}\text{Rb}$ . The latter is well known in the atomic physics community for being one of the most used elements utilized for laser cooling and realizations of Bose Einstein Condensates (BEC). This is due to the fact that the atomic transitions of rubidium are in wavelengths that are easily accessible by commercial lasers.

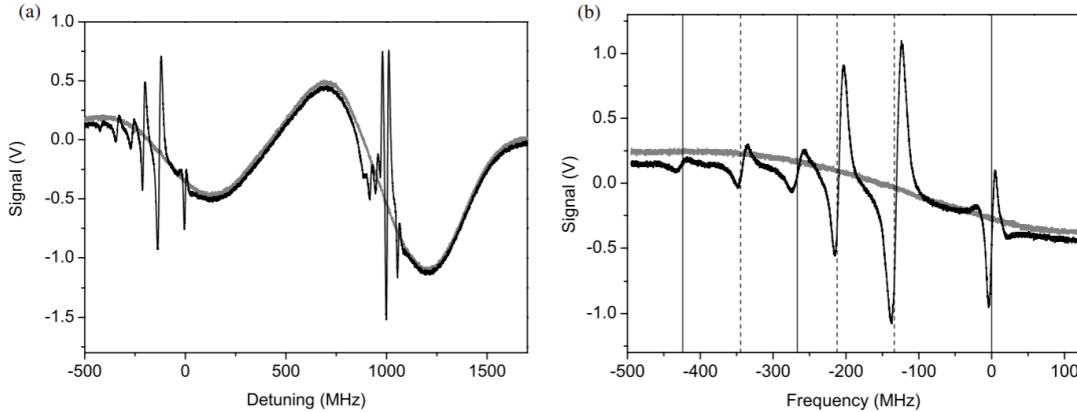


Figure 2: (a) Typical sub-Doppler DAVLL spectra recorded for the  $F = 2 \rightarrow F$  line in  $^{87}\text{Rb}$  and  $F = 3 \rightarrow F$   $^{85}\text{Rb}$  (black line). The sub-Doppler features are superimposed on the conventional DAVLL signal (grey line) obtained by blocking the pump beam. (b) A zoomed-in section of (a) showing the sub-Doppler DAVLL signal for the  $F = 2 \rightarrow F$  transitions of  $^{87}\text{Rb}$ . Vertical lines indicate the expected line centres of the three transitions (solid lines) and three crossovers (dashed lines). Small discrepancies in the location of spectral features relative to the line centres arise from the slightly nonlinear laser scan. Spectra were taken at a magnetic field of 9.5 G, a pump power of 154  $\mu\text{W}$  and a probe power of 20  $\mu\text{W}$ . doi:10.1088/0953-4075/41/8/085401

**Get those other Lasers paying rent**



## How does a Laser Work?

### Laser 1

1. Oscilloscope
2. Signal Generator
3. TEC: Temperature Control
4. Control of Control : Lockbox
5. Laser Control : Negative Current Control
6. Current Control
7. Rubidium Heater for Glass Cell

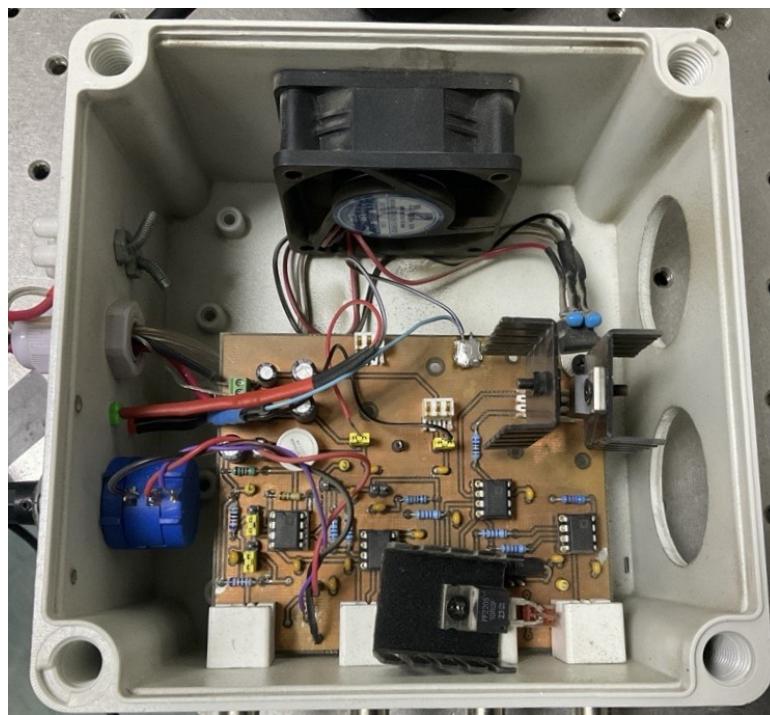


Figure 3: This is what the TEC looks like inside!

### Laser 2

#### Locking a Laser

In order to perform experiments with atomic systems, two main things must be taken into account: first, the laser linewidth must be narrower than the atomic transition linewidth  $\gamma$ , and second, we must be able to control the center frequency  $\omega$  of the laser near the transitions.

For the former requirement, most commercial grade lasers already have the needed linewidths. Since at the Laboratory of Atomic and Molecular Physics (LAMP) we develop our own lasers, we have two main mechanisms to narrow the linewidth; optical feedback from a diffraction grating in LITTROW configuration, and optical feedback from an external cavity. Both of these mechanisms can be used to achieve very narrow linewidths.

For the latter requirement, it is now standard practice to **lock** the laser frequency to an atomic transition. This is done by deflecting a small portion of the laser light to an atomic reference system. The light will interact with an atomic vapour cell, and the transmitted light will be detected using a photodiode. This signal can then be used to send electrical signals and control the laser frequency. In the section that follows, we will explain in further detail how to **lock your laser to an atomic transition**.

#### Locking Mechanisms

Laser diodes have been effective tools for atomic physics experiments. However, as we have hinted, the center frequency of a laser diode is not stable enough as is, being very sensitive to current, temperature, humidity and the environment in general; this will have an effect on the diode frequency such that it will change from the expected one (known as *Drift*). To overcome this problem, the laser frequency is *locked* to an atomic resonance; this means that the laser frequency is continuously adjusted and stabilized via feedback. The feedback is usually done by modulating the laser current, and using the error signal from the atomic reference to correct the frequency.

There are two main quantities which can be used to study the stability of a laser: the Power Spectral Density (studied in frequency domain) and the Allan Deviation (studied in time domain). The first one is associated with the linewidth of the laser and is studied by a beat-note analysis or autocorrelator, while the

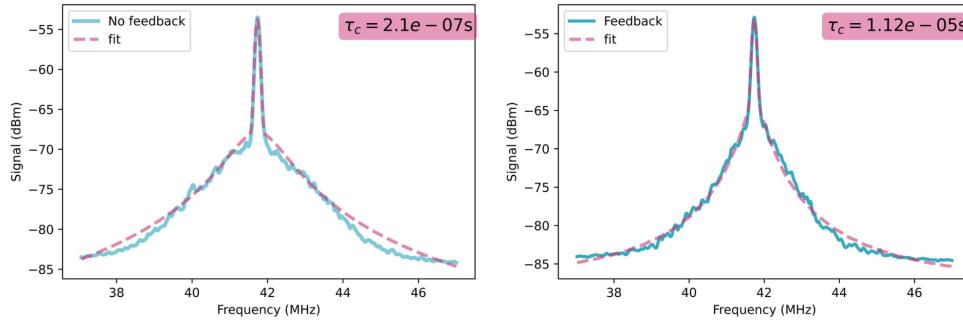


Figure 4: Coherence time  $\tau_c$  of Laser 1 with and without external cavity feedback controlled with piezoelectric. Figure From Florencia Fuentes.

latter is associated to long term effects on performance, akin to standard variation, and studied as a time series from a beat-note or wavemeter. For our particular case, we tend to care more about the first one, since one can always re-lock the laser for experiments.

Two locking mechanisms used in the development of this thesis. They are known as Saturated Absorption Spectroscopy (SAS) and Dichroic Atomic Vapor Laser Lock (DAVLL). Both of these mechanisms use a warm atomic vapor as a reference, and both can be used to lock the laser to a specific transition. The main difference between them is that SAS uses a counter-propagating pump and probe beam to achieve sub-Doppler resolution, while DAVLL, based on the SAS protocol, adds a controlled magnetic field to achieve a higher quality signal in the zeeman manifold.

### SAS and DAVLL

SAS, also known as Doppler Free Spectroscopy, is a technique that allows for the observation and determination of atomic and fine transition frequencies without the effects of Doppler broadening. This is useful when probing atomic vapors, where the thermal motion of atoms can lead to significant broadening of spectral lines.

To illustrate the technique, consider a warm atomic cell (between 30–100 °C) with a weak probe propagating in it. If the atoms have a velocity profile, then atoms will see different frequencies depending on where and how they are moving; something we usually call *Doppler Shift*. If we scan the laser in frequency, we will lose finer transitions due to the thermal noise. In this sense, we are limited to a certain resolution set by the Doppler broadening. For rubidium at room temperature this broadening is around 300 MHz, much larger than the natural linewidth of the  $D_2$  transition (6 MHz).

To overcome this limitation, a counter-propagating strong pump beam is introduced along with the weak probe. The pump beam saturates a set of atomic transitions, while the probe measures the resulting absorption. This configuration produces the familiar Doppler-broadened background but, importantly, a narrow dip (*Lamb dip*) appears at the resonance frequency  $\nu = \nu_0$ .

The physical mechanism behind this dip is that the pump and probe interact with different velocity classes of atoms. While the probe absorption originates from atoms moving in one direction, the pump simultaneously depletes the population of atoms moving in the opposite direction. When both beams address the same group of atoms (i.e., atoms with zero velocity relative to the laser), the transition saturates, leading to a reduction in probe absorption at the exact resonance. This feature provides the Doppler-free signature needed for precise frequency determination and laser frequency stabilization.

In addition to the central Lamb dips, crossover resonances can also appear. These arise when the Doppler broadened profile of two nearby transitions overlaps. In this case, a particular velocity class of atoms can simultaneously satisfy resonance conditions for the probe on one transition and for the pump on another. As a result, the observed crossover resonance signal is typically stronger—often about twice the size of a normal Lamb dip—making it a useful reference feature in saturated absorption spectroscopy.

DAVLL systems can also be operated in the Doppler-free mode, in which a narrow differential absorption signal is used, resulting in a more precise locking of the laser frequency, at the cost of a smaller capture range.

## Laser Linewidth

Also known as Full Width Half Maximum (FWHM) This linewidth is where we consider a cavity being resonant. It is usually a Lorentzian distribution. The ideal case of a laser would be a delta distribution in frequency, but even for us physicists, that's too ideal. The linewidth of a light beam is strongly related to the temporal coherence. We can measure the Linewidth with the setup,

And comparing the linewidth of Laser 1 with and without cavity and piezo feedback, we get the following results:

## Gaussian Beam

(Check the book of Saleh and Teich, Fundamentals of Photonics for the official reference!)



# 1 A Quick Guide on Cooling Atoms

In this section I will briefly explain how we manage to cool a group of atoms ( $10^8$ ) down to hundreds of a few hundred micro Kelvin. This is an essential for experiments in atomic physics, as cold atoms have paved a way for incredible discoveries such as Bose Einstein Condensates, precision atomic clocks, quantum memories, and so much more. The most popular procedure (but not the only one by far) to generate this cloud of atoms is called Magneto Optical Trapping, better known as MOT. While a MOT can typically cool atoms to the *Doppler limit* (a few hundred micro Kelvin for rubidium), one can make use of more than one mechanism, such as Sisyphus cooling, Raman sideband cooling and optical molasses; which in certain situations can help cool even further, down to nanokelvin scale. This means that on earth, we can effectively reach temperatures colder than those found in deep space.

However, the focus of this section will be to explain, in hopefully rather simple concepts from what we have discussed seen so far, how a MOT works. For this goal, we will describe different processes that belong to the interaction and conclude with putting everything together to explain the MOT mechanism and hopefully illustrate why this has been revolutionary to understand light matter interactions.

## 1.1 Light Forces

When radiation interacts with matter, the process of absorption will generate a change in the momentum of the object associated to the force on the object. From classical mechanics, and using the Ehrenfest theorem, we can relate the force on an object to the time derivative of the expectation value of its momentum operator:

$$F = \frac{d\langle \vec{p} \rangle}{dt} = M \frac{d\langle \vec{v} \rangle}{dt} = \frac{1}{i\hbar} \langle [\vec{p}, H] \rangle. \quad (1)$$

If we replace the two-level atom Hamiltonian in the presence of an electric field in this equation, we can calculate the forces on the atom due to the interaction with light. This force contains two components, where the first one is usually called *Dipolar Force*; and the latter is known as *Radiation Pressure*

$$\vec{F} = \frac{2\hbar}{\Omega_0(\vec{R})} \Delta \sigma_{ee}^{st} \vec{\nabla}_R \Omega_0(\vec{R}) + \hbar \Gamma \sigma_{ee}^{st} \vec{\nabla} \phi(\vec{R}), \quad (2)$$

$\vec{R}$  corresponds to the position of the center of mass of the atom.  $\sigma_{ee}^{st}$  is the steady state solution of the Bloch equations for the excited state population.  $\Gamma$  is the spontaneous emission rate of the excited state ( $2\pi \times 6.05$  MHz for  $Rb^{D2}$ ).

The dipolar force corresponds to a conservative potential, is proportional to the gradient of the intensity of the light field, shown by the Rabi frequency  $\Omega_0$ , and decays with the detuning as  $1/\Delta$ . This is the force responsible for the trapping of atoms in optical dipole traps. The radiation pressure, on the other hand, is proportional to the scattering rate of photons by the atom, and decays with detuning as  $1/\Delta^2$ . This force is responsible for the cooling of atoms in optical molasses and magneto-optical traps.

## 1.2 Optical Molasses

Is the name given to the technique which uses counter-propagating beams in three orthogonal directions along the cartesian axes. These lasers all share the same frequency, which is slightly red-detuned from an atomic transition. Due to the Doppler effect, moving atoms will feel a slowing force (as if they were travelling in molasses) and stationary atoms with respect to the center where all lasers intersect will not feel any external force. Since the lasers are relatively close to resonance, the force comes from the radiation pressure term of the light forces discussed before. The force on an atom moving with velocity  $\vec{v}$  due to two counter-propagating laser beams in 1D can be written as:

$$\vec{F}_{\pm} = \gamma_{\pm} \hbar \vec{k}_{\pm} = \pm \frac{1}{2} \frac{s_0 \hbar \vec{k} \Gamma}{1 + s_0 + 4((\Delta_0 \mp k v)/\Gamma)^2}, \quad (3)$$

where  $s_0 = 2\Omega_0^2/\Gamma^2$  is the on-resonance saturation parameter,  $\Delta_0$  is the detuning of the laser from the atomic resonance, and  $\vec{k}_{\pm}$  are the wavevectors of the two beams. The total force on the atom is then given by  $\vec{F} = \vec{F}_+ + \vec{F}_-$ .

The velocity capture range  $\Delta v$  of such a process is determined by the natural width  $\Gamma$  of the atomic excited state. As is, atoms will begin to accumulate slowly in the center of the trap. There is however a limit to how cold one can get atoms using only this method, known as the Doppler limit. This limit arises from the balance between the cooling force (radiation pressure) and the heating effect due to statistical fluctuations. The minimum achievable temperature, known as the Doppler temperature  $T_D$  for a number of dimensions  $D$ , is given by

$$T_D^{min} = \frac{\hbar \Gamma}{2k_B}. \quad (4)$$

For a rubidium atom, since  $\Gamma = 2\pi(6.05 \times 10^6)$  rad/s this temperature is around  $140\mu K$ . To overcome this limit, an addition of polarization and magnetic field engineering makes this method much more effective, something we will know as Magneto-Optical Trapping.

## 1.3 Magneto-Optical Trap

As mentioned, the addition of a set of coils in anti-Helmholtz configuration manage to diminish the effects of any external magnetic field, and maybe most importantly, generate a magnetic field gradient outside the center of the trap. This gradient induces spatially varying Zeeman shifts in the atoms that are farther from the center. Adding then the circular polarization of the counter-propagating beams ensures atoms preferentially scatter photons that push them back to the trap center.

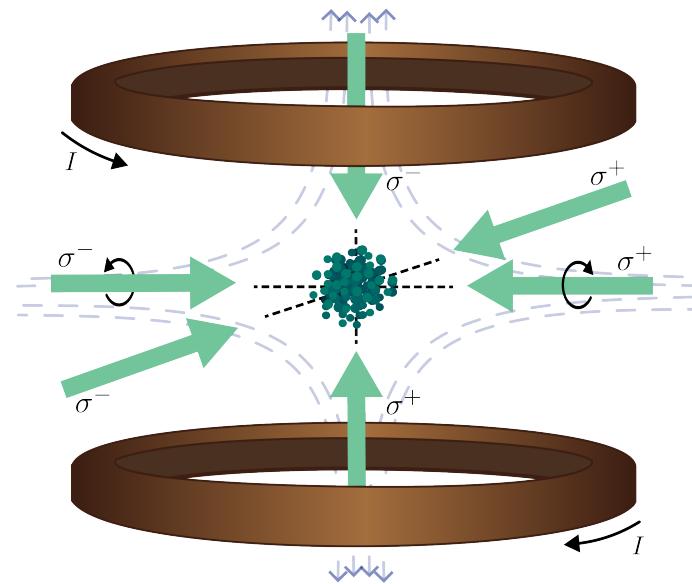


Figure 5: Illustrated mechanism of a magneto optical trap.

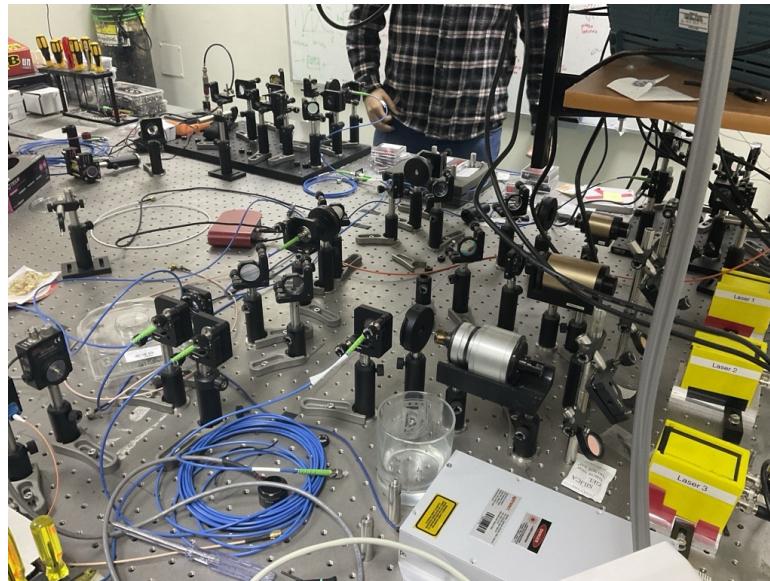


Figure 6: Dont be afraid of a "little" mess! Part of the experimental life.

## How in earth do I find the Rubidium Transition Wavelengths in the experiment?

To start finding the resonances in the DAVLL system (see Fig 2), you first will have to turn on the following (in no particular order, don't worry!):

1. Oscilloscope
2. Signal Generator
3. Laser 1 Box
4. Current Control
5. Heaters for the Rb Cell
6. Photodiodes at the end of the laser path (see Fig 7)

## Experimental Set Up

**Rubidium Borosilicate Reference Cell, Ø25.4 mm x 71.8 mm :** Since each fill material is associated with a unique absorption spectrum that serves as its fingerprint, the contents of a reference cell can be determined via a linear absorption measurement (as depicted by the simplified schematic above). By scanning a tunable diode laser over a wavelength range and detecting light absorption (A) with a photodetector, a series of peaks will be recorded, which is characteristic of the vapor inside the cell. All of the cells offered here are baked and evacuated to 10-8 Torr prior to filling in order to remove contaminants. Additionally, each cell is helium leak checked to ensure the longevity of the vapor cell. The vapor pressure of the alkali metal will cause it to migrate throughout the cell and condense at the coolest area. Heating the windows of the cell rather than the cell body will help ensure the windows stay warmer and thus that the alkali will collect elsewhere. If obstruction of the optics becomes an issue, apply cooling to an area on the cell body, such as near the fill stem,

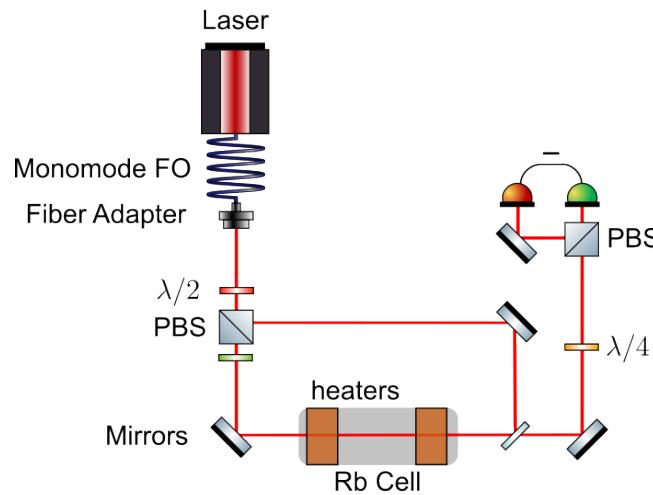


Figure 7: Set up for Laser 1. Dicroich atomic vapor laser lock (DAVLL) system.

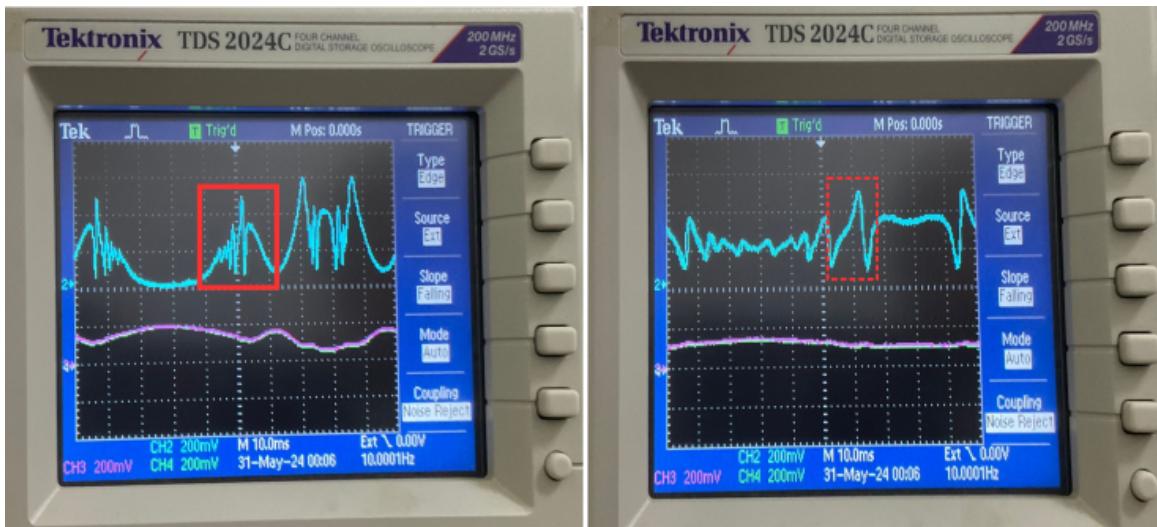


Figure 8: Bragg Reflections in Rubidium Vapours.

and heat the windows in an alternating fashion to drive the metal from the window surfaces and collect it at the cool spot. The metal may eventually move back to the windows depending on how the cell is heated. The rubidium reference cell (GC19075-RB) is sold with the natural isotope ratio of Rb, which is 72.15%  $^{85}\text{Rb}$  and 27.85%  $^{87}\text{Rb}$

**SM1FCA - FC/APC Fiber Adapter Plate with External SM1 (1.035"-40) Threads, Wide Key (2.2 mm) LA1509-B-ML - Ø1" N-BK7 Plano-Convex Lens, SM1-Threaded Mount, f = 100 mm, ARC: 650-1050 nm**

The Rb vapor cell is a glass cell filled with natural rubidium having two isotopes:  $^{85}\text{Rb}$  and  $^{87}\text{Rb}$ . The vapor pressure of rubidium inside the cell is determined by the cell temperature and is about  $4 \times 10^{-5}$  Pa at room temperature.

### Doppler broadened absorption in a vapor cell

The rubidium atoms in the vapor cell are moving according to the Maxwell-Boltzmann velocity distribution at a temperature of around 400 K. The Doppler broadened lines have line widths of several 100 MHz. This is because even if we detune the probe light by several 100 MHz from the resonance frequency for an atom at rest, there are still atoms within the vapor cell that are moving at the right velocity relative to the wavevector

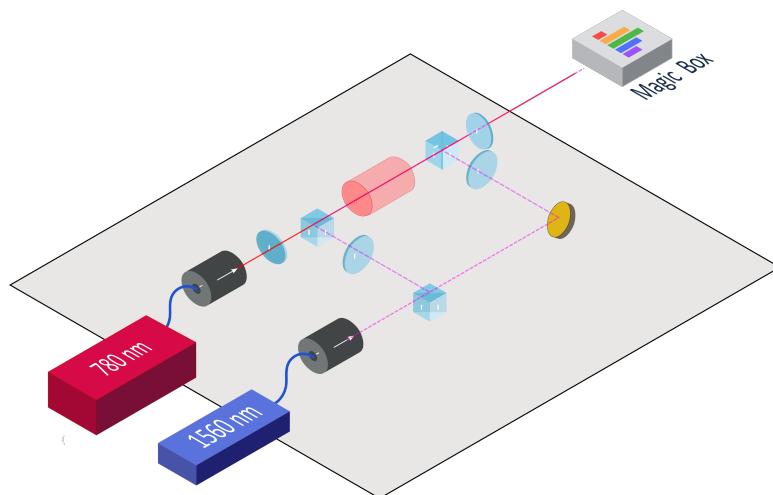


Figure 9: Set up for the experiment of the bragg Vapours.



of the light so that they see the light as being exactly on resonance in their center-of-mass frame. Those atoms absorb light from the incident beam, and thereby attenuate the light beam passing through the vapor cell.

## Bragg Reflections in Cold Rubidium

### Experimental Set Up

#### MOT - Atom Trapping

Invented at MIT and first demonstrated at Bell Labs [4], it combines the abilities of both cooling and also trapping atoms, limiting both their momenta and their positions, while remaining experimentally simple to implement and to integrate with other experimental needs. Using MOTs and other laser cooling methods, a wide variety of ultracold atomic and molecular gases are produced routinely in labs around the world and applied to a range of scientific pursuits, e.g. matter-wave interferometry with coherent atomic beams, condensed-matter like systems created from quantum-degenerate gases, and novel atomic clocks and other modes of precision measurement.

<https://github.com/aisichenko/MOTorNOT/tree/master/MOTorNOT>

1. Scattering Rate
2. Radiation Pressure
3. Doppler Shift
4. Doppler Cooling
5. Capture Velocity
6. Doppler Temperature Limit and Doppler Molasses
7. Effects of the Zeeman shift on light scattering
8. Sub-Doppler Cooling

#### Cooking up (Freezing up?) a MOT

How do we afford to get to these very low pressures ? We have to literally cook the MOT vacuum equipment at 100 Celcius for a determined amount of time (days?), this, so we can clear up any impurities that might be present in the chamber. This is a very important step, since the MOT vacuum has to be around  $10^{-8}$  Torr.



## Atomic Structure

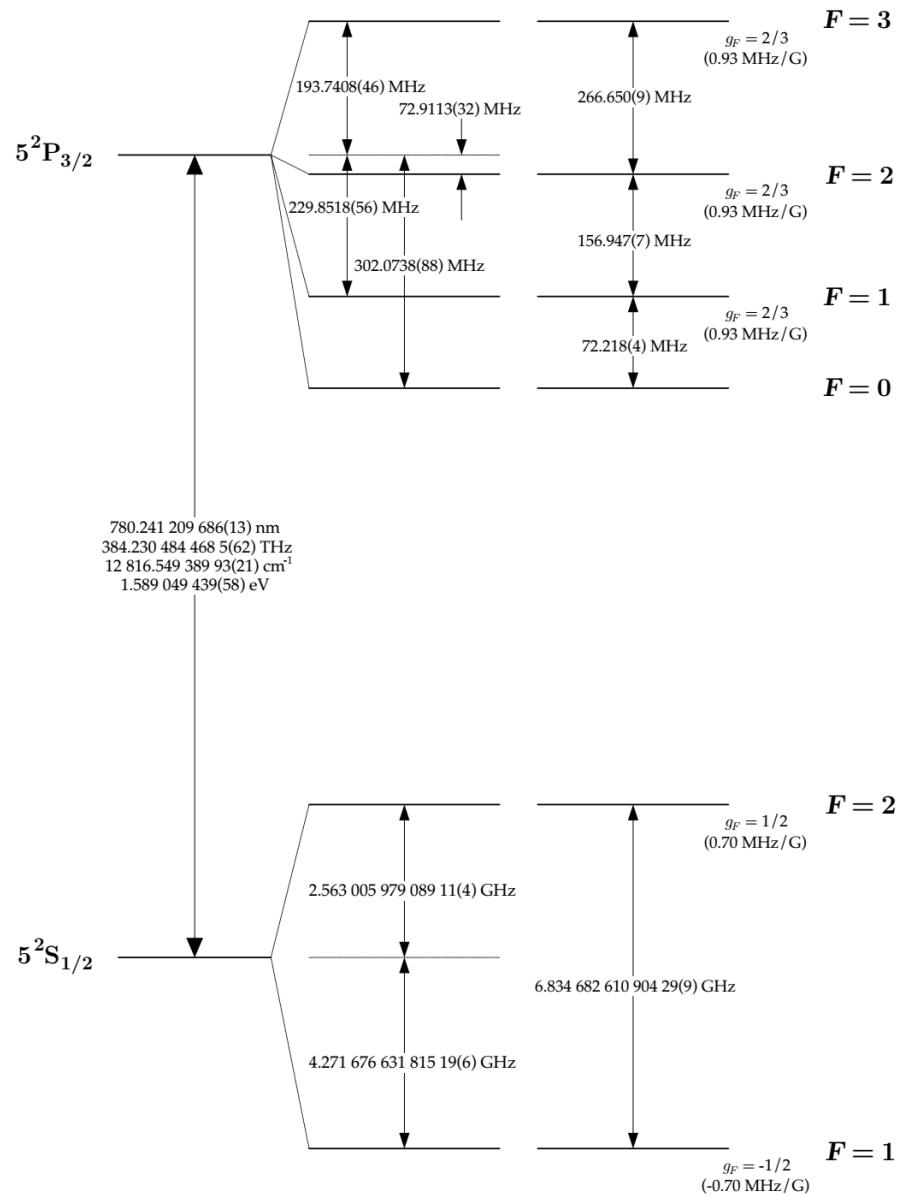


Figure 10: <sup>87</sup>Rb D2 transition hyperfine structure, with frequency splittings between the hyperfine energy levels. The approximate Landé  $g_F$ -factors for each level are also given, with the corresponding Zeeman splittings between adjacent magnetic sublevels. (Steck, 2001)



## References