Daily Coding Problem #129

Problem

Given a real number n, find the square root of n. For example, given n = 9, return 3.

Solution

This is a classic question that was first solved by Heron of Alexandria after the first century.

Alexandra's algorithm starts with a guess and iteratively improves until convergence. In each iteration, we improve our guess by averaging guess and n / guess. This formula comes from the fact that if guess is an overestimate, then n / guess would be an underestimate. For example, If n is 9, then a guess of 4 is an overestimate and 9 / 4 is an underestimate. On the other hand, if guess is an underestimate, then n / guess is an overestimate. The process converges when guess is 3 which is equal to 9 / 3. For the full proof, please see here.

```
def squareroot(n, error=0.00001):
    guess = 1

while abs(guess ** 2 - n) >= error:
    guess = (guess + n / guess) / 2.0
    return guess
```

A more realistic answer, in an interview setting, would be to use binary search. We can pick an underestimate lo = 0 and an overestimate hi = n to start. And we can keep the loop invariant that the true squareroot(n) would always lie between [lo, hi]. To do this, we see if guess = (lo + hi) / 2 is an overestimate, and if it is, bring the hi down to guess. Otherwise, we bring the lo up to guess. The loop finishes when guess

```
def squareroot(n, error=0.00001):
    lo = 0.0
    hi = n
    guess = (lo + hi) / 2.0

while abs(guess ** 2 - n) >= error:
    if guess ** 2 > n:
        hi = guess
    else:
        lo = guess
    guess = (lo + hi) / 2.0
```

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