

$$1. (i) pnorm(200, 500, 0.4) = 0.5194108$$

$$P(Z < 0.0456) = pnorm(0.456) = 0.5182$$

$$(ii) \bar{X} \sim \text{Binomial}(500, 0.4)$$

$$\begin{aligned} E[X] &= np \\ &= 500(0.4) \\ &= 200 \end{aligned}$$

$$\begin{aligned} \text{var}(X) &= np(1-p) \\ &= 120 \end{aligned}$$

$$sd = 2\sqrt{30}$$

$$\begin{aligned} P(X < 200.5) \quad \text{w/ correction} \\ &= P\left(\frac{X-200}{2\sqrt{30}} < \frac{200.5-200}{2\sqrt{30}}\right) \\ &= P(Z < 0.0456) \\ &= 0.5182 \end{aligned}$$

$$2. (i) 1 - pbinom(750, 1000, 0.7) = 0.0001985473$$

$$1 - pnorm(3.48483) = 0.0002462249$$

$$(ii) P(X > 750)$$

$$\text{var}(X) npq = 210$$

$$P\left(X > \frac{750.5 - 700}{\sqrt{210}}\right)$$

$$\mu(X) np = 700$$

$$P(Z > 3.48483) \approx 0.0002$$

3) 6.8 Text

a) point estimate = 0.25

b)  $np = 1000 \cdot 0.25$  conditions are met

$= 250 > 10$ , expect 10 successes & 10 failures

c)  $\alpha = 0.05$

$$Z(0.025) = 1.96$$

$$p \pm Z \cdot \sqrt{\frac{p(1-p)}{n}}$$

$$0.25 \pm 1.96 \sqrt{\frac{0.25(1-0.25)}{1000}}$$

$$(0.2231616, 0.2768384)$$

d) our confidence interval would get bigger

e) our confidence interval would decrease

4) 6.14 Text

$$a) p \pm z \cdot \sqrt{\frac{p(1-p)}{n}}$$

$$\alpha = 1 - 0.9 \\ = 0.1$$

$$Z = 1.645$$

$$\frac{\alpha}{2} = 0.05$$

$$C = 0.48 \pm \sqrt{\frac{0.48 \cdot 0.52}{331}}$$

$$= 0.48 \pm 1.645 \cdot 0.027$$

$$= 0.48 \pm 0.044$$

$$(0.435, 0.526)$$

Between 0.435 and 0.526 americans wouldn't go to college

$$b) moe = Z \cdot \sqrt{\frac{p(1-p)}{n}} \\ = 0.015$$

$$moe = 1.645 \cdot \sqrt{\frac{0.48 \cdot 0.52}{n}} = 0.015$$

$$\frac{0.675}{n} = 0.000225$$

$$n = \frac{0.675}{0.000225}$$

$$n = 3000$$

$$5) 6.16$$

$$p = 61\% = 0.61$$

$$moe = 0.02$$

$$z = 1 - 0.95$$

$$z = 0.05$$

$$\frac{z}{2} = \frac{0.05}{2} = 0.025$$

$$z_{2/2} = z_{0.025} = 1.96$$

$$n = \frac{z_{2/2}^2 \cdot p(1-p)}{E}$$

$$= \left( \frac{1.96}{0.02} \right)^2 \cdot 0.61(0.39)$$

$$n = 2285$$

$$6)$$

$$z \sqrt{\frac{p(1-p)}{n}}$$

$$= \sqrt{\frac{0.88(0.12)}{1000}}$$

$$= 0.01028$$

$$pe: \frac{880}{1000} = 0.88$$

$$moe = 1.28 (0.01028)$$

$$= 0.01315$$

$$p = 0.88 \pm 0.01315$$

$$7) \left( \frac{1.96}{2(0.02)} \right)^2$$

$$n \geq$$

$$= 2401$$

$$\text{so, } n \geq 2401$$