### 563 HW4

#### Amber Wang, Daniel Chen, Xilong Liang

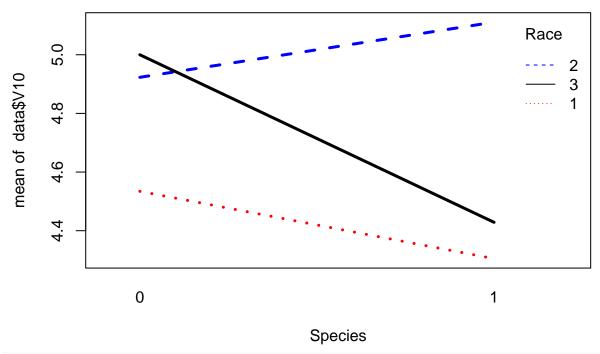
#### 3/16/2022

```
library(MASS)
library(biotools)

## ---
## biotools version 4.2
library(DiscriMiner)
library(klaR)
library(car)

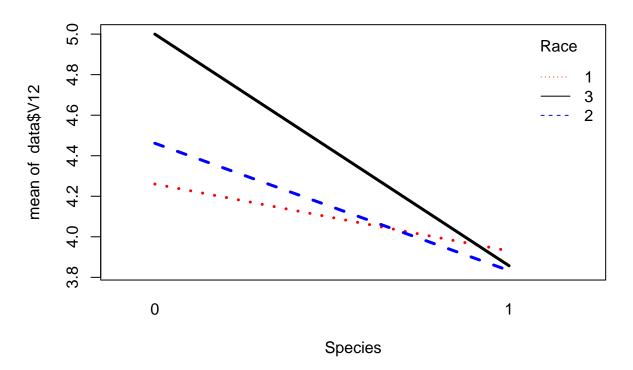
## Loading required package: carData
library("readxl")
setwd("~/Downloads")
data <- read_excel("ohiocrimehm.xls")
data = na.omit(data)
#First, we fit a two-way MANOVA model. For two categorical factors, make interaction plots for each of
interaction.plot(data$V70, data$V71, data$V10,
    lwd = 3, col = c("red", "blue", "black"), trace.label = "Race",
    xlab = "Species", main = "Interaction Plot for v10")</pre>
```

### **Interaction Plot for v10**



```
interaction.plot(data$V70, data$V71, data$V12,
  lwd = 3, col = c("red", "blue", "black"), trace.label = "Race",
  xlab = "Species", main = "Interaction Plot for v12")
```

### **Interaction Plot for v12**



```
\#V70 and V71 are both having interaction, when we set V10 and V12 as response variable. The interaction
```

```
options(contrasts = c("contr.sum", "contr.poly"))
model <- lm(cbind(V10, V12) ~ V70*V71,</pre>
             data = data)
#Multivariate and univariate results
summary(Anova(model, type = 3), univariate = T)
## Type III MANOVA Tests:
## Sum of squares and products for error:
         V10
               V12
## V10 815.5805 465.0591
## V12 465.0591 1349.2870
## -----
##
## Term: (Intercept)
## Sum of squares and products for the hypothesis:
         V10
              V12
## V10 211.1186 202.5865
## V12 202.5865 194.3992
## Multivariate Tests: (Intercept)
    Df test stat approx F num Df den Df Pr(>F)
                1 0.2238320 71.37428 2 495 < 2.22e-16 ***
## Pillai
## Wilks
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## -----
##
## Term: V70
##
## Sum of squares and products for the hypothesis:
         V10 V12
## V10 0.39455168 0.051264474
## V12 0.05126447 0.006660842
## Multivariate Tests: V70
               Df test stat approx F num Df den Df Pr(>F)
               1 0.0005540 0.1371941 2 495 0.87183
## Pillai
## Wilks
                1 0.9994460 0.1371941
                                        2 495 0.87183
## Hotelling-Lawley 1 0.0005543 0.1371941 2 495 0.87183 
## Roy 1 0.0005543 0.1371941 2 495 0.87183
##
```

```
##
## Term: V71
##
## Sum of squares and products for the hypothesis:
          V10
                   V12
## V10 1.917898 1.3260897
## V12 1.326090 0.9168963
## Multivariate Tests: V71
##
                 Df test stat approx F num Df den Df Pr(>F)
## Pillai
                  1 0.0023719 0.5884476 2 495 0.55558
                                           2 495 0.55558
2 495 0.55558
                  1 0.9976281 0.5884476
## Wilks
## Hotelling-Lawley 1 0.0023776 0.5884476
## Roy 1 0.0023776 0.5884476
                                           2 495 0.55558
##
## -----
##
## Term: V70:V71
## Sum of squares and products for the hypothesis:
              V10
                         V12
## V10 0.0004718059 0.02218056
## V12 0.0221805584 1.04275336
## Multivariate Tests: V70:V71
                 Df test stat approx F num Df den Df Pr(>F)
## Pillai
                  1 0.0009384 0.2324634 2 495 0.79267
                  1 0.9990616 0.2324634
                                            2 495 0.79267
## Wilks 1 0.9990616 0.2324634
## Hotelling-Lawley 1 0.0009392 0.2324634
                                           2 495 0.79267
## Roy
                   1 0.0009392 0.2324634 2 495 0.79267
##
## Type III Sums of Squares
              df
                    V10
                                   V12
## (Intercept) 1 2.1112e+02 1.9440e+02
             1 3.9455e-01 6.6608e-03
## V70
              1 1.9179e+00 9.1690e-01
## V71
              1 4.7181e-04 1.0428e+00
## V70:V71
## residuals 496 8.1558e+02 1.3493e+03
##
## F-tests
                V10 V12
## (Intercept) 128.39 71.46
## V70
       0.24 0.00
## V71
              1.17 0.34
## V70:V71
              0.00 0.38
##
## p-values
              V10 V12
##
## (Intercept) < 2.22e-16 3.1717e-16
        0.62446
## V70
                      0.96055
## V71
             0.28067
                        0.56180
## V70:V71 0.98649
                        0.53612
```

```
#multivariate results: based on the multivariate results, under a significance level of alpha = 0.05, t
anova(lm(V10 \sim V70*V71, data = data))
## Analysis of Variance Table
## Response: V10
##
             Df Sum Sq Mean Sq F value Pr(>F)
## V70
             1 5.21 5.2062 3.1662 0.07579 .
                 7.01 7.0128 4.2649 0.03943 *
## V71
              1
                 0.00 0.0005 0.0003 0.98649
## V70:V71
              1
## Residuals 496 815.58 1.6443
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
anova(lm(V12 \sim V70*V71, data = data))
## Analysis of Variance Table
## Response: V12
             Df Sum Sq Mean Sq F value Pr(>F)
##
## V70
                 13.92 13.9225 5.1179 0.02411 *
                 0.03 0.0258 0.0095 0.92253
## V71
              1
## V70:V71
             1
                   1.04 1.0428 0.3833 0.53612
## Residuals 496 1349.29 2.7203
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
#univaraite results: when "V10" is the response variable, only "V71" is significant under a significanc
#3
#3
#RUN LINE BELOW TO MAKE SURE CONTRASTS ARE SET CORRECTLY - this returns things to their default level
options(contrasts = c("contr.treatment", "contr.poly"))
#Make sure TRTCOMB is a factor
data$V72 <- as.factor(data$V72)</pre>
#Fit two way MANOVA model
dataaMAOV2 <- lm(cbind(V10, V12) ~ V72,
               data = data)
#Fit one way ANOVA model just for ASQRT
dataaASQRT <- lm(V10 ~ V72,</pre>
               data = data)
contrasts(data$V72)
    2 3 4 5 6 7 8
## 1 0 0 0 0 0 0 0
## 2 1 0 0 0 0 0 0
## 3 0 1 0 0 0 0 0
## 4 0 0 1 0 0 0 0
## 5 0 0 0 1 0 0 0
## 6 0 0 0 0 1 0 0
## 7 0 0 0 0 0 1 0
## 8 0 0 0 0 0 0 1
```

```
levels(data$V72)
## [1] "1" "2" "3" "4" "5" "6" "7" "8"
#Get multivariate contrast for 1 vs 2 - notice that 1 is the reference level
linearHypothesis(dataaMAOV2, "V722+V723+V724+V725- V726 - V727- V728= 0")
##
## Sum of squares and products for the hypothesis:
              V10
                        V12
## V10 0.004578635 0.07473129
## V12 0.074731289 1.21974469
##
## Sum of squares and products for error:
##
           V10
                    V12
## V10 801.7941 463.602
## V12 463.6020 1341.792
## Multivariate Tests:
##
                   Df test stat approx F num Df den Df Pr(>F)
                    1 0.0010615 0.2608767
                                               2
## Pillai
                                                    491 0.77048
## Wilks
                    1 0.9989385 0.2608767
                                                2
                                                    491 0.77048
## Hotelling-Lawley 1 0.0010626 0.2608767
                                                2 491 0.77048
                     1 0.0010626 0.2608767
                                              2 491 0.77048
linearHypothesis(dataaASQRT, "V722+V723+V724+V725- V726 - V727- V728= 0")
## Linear hypothesis test
##
## Hypothesis:
## V722 + V723 + V724 + V725 - V726 - V727 - V728 = 0
## Model 1: restricted model
## Model 2: V10 ~ V72
##
   Res.Df
              RSS Df Sum of Sq
##
                                     F Pr(>F)
## 1
       493 801.80
       492 801.79 1 0.0045786 0.0028 0.9577
since for p value is 0.9577 so the model1 is better since model2 is not significant.
#4'
options(contrasts = c("contr.sum", "contr.poly"))
### Default is: options(contrasts = c("contr.treatment", "contr.poly"))
#Fit the model
dataaMod2 <- lm(cbind(V10, V12) ~ V70*V71+V64,</pre>
                data = data)
#Multivariate results and univariate results with with type 3 Sum of squares
summary(Anova(dataaMod2, type = 3), univariate = T)
## Type III MANOVA Tests:
##
```

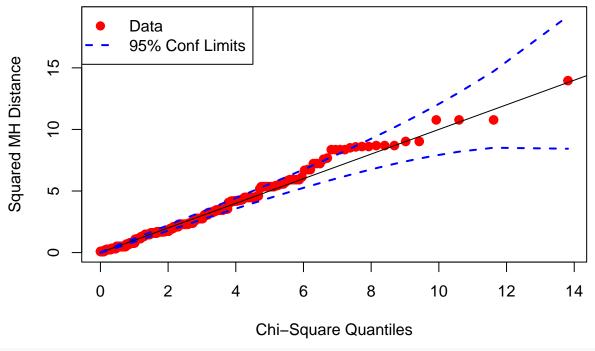
```
## Sum of squares and products for error:
##
          V10 V12
## V10 803.9033 464.5396
## V12 464.5396 1349.2639
## -----
## Term: (Intercept)
##
## Sum of squares and products for the hypothesis:
## V10
                V12
## V10 139.3511 149.0269
## V12 149.0269 159.3745
## Multivariate Tests: (Intercept)
     Df test stat approx F num Df den Df Pr(>F)
##
## Pillai 1 0.1697794 50.51128 2 494 < 2.22e-16 ***
## Wilks 1 0.8302206 50.51128 2 494 < 2.22e-16 ***
## Hotelling-Lawley 1 0.2044991 50.51128 2 494 < 2.22e-16 ***
                    1 0.2044991 50.51128 2 494 < 2.22e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## -----
##
## Term: V70
##
## Sum of squares and products for the hypothesis:
            V10
                       V12
## V10 0.5702664 0.06587120
## V12 0.0658712 0.00760875
##
## Multivariate Tests: V70
                  Df test stat approx F num Df den Df Pr(>F)
## Pillai
                   1 0.0008215 0.203073 2 494 0.81629
## Wilks
## Wilks 1 0.9991785 0.203073 2 494 0.81629
## Hotelling-Lawley 1 0.0008222 0.203073 2 494 0.81629
## Roy 1 0.0008222 0.203073 2 494 0.81629
##
## -----
##
## Term: V71
## Sum of squares and products for the hypothesis:
           V10
## V10 1.364720 1.1053034
## V12 1.105303 0.8951987
##
## Multivariate Tests: V71
         Df test stat approx F num Df den Df Pr(>F)
## Pillai 1 0.0017625 0.4361062 2 494 0.6468
## Wilks 1 0.9982375 0.4361062 2 494 0.6468
## Hotelling-Lawley 1 0.0017656 0.4361062 2 494 0.6468
                    1 0.0017656 0.4361062 2 494 0.6468
## Roy
```

```
##
## -----
##
## Term: V64
## Sum of squares and products for the hypothesis:
         V10
## V10 11.6771558 0.51952728
## V12 0.5195273 0.02311424
## Multivariate Tests: V64
              Df test stat approx F num Df den Df Pr(>F)
               1 0.0172947 4.346962 2 494 0.013445 *
## Pillai
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## -----
##
## Term: V70:V71
##
## Sum of squares and products for the hypothesis:
## V10 V12
## V10 0.05140557 -0.2284059
## V12 -0.22840587 1.0148558
## Multivariate Tests: V70:V71
              Df test stat approx F num Df den Df Pr(>F)
## Pillai
               1 0.0012614 0.3119656 2 494 0.73215
               1 0.9987386 0.3119656
## Wilks
                                    2 494 0.73215
## Hotelling-Lawley 1 0.0012630 0.3119656 2 494 0.73215
               1 0.0012630 0.3119656 2 494 0.73215
## Type III Sums of Squares
## df V10
## (Intercept) 1 139.351107 1.5937e+02
## V70
             1 0.570266 7.6088e-03
## V71
            1 1.364720 8.9520e-01
## V64
            1 11.677156 2.3114e-02
## V70:V71
            1 0.051406 1.0149e+00
## residuals 495 803.903348 1.3493e+03
##
## F-tests
            V10 V12
##
## (Intercept) 85.80 58.47
      0.35 0.00
## V70
## V71
           0.84 0.33
           7.19 0.01
## V64
## V70:V71
           0.03 0.37
##
## p-values
           V10 V12
##
```

```
## (Intercept) < 2.22e-16 1.0828e-13
## V70
              0.5537396 0.9578857
## V71
              0.3597515 0.5668520
## V64
              0.0075752 0.9266669
## V70:V71
              0.8588647 0.5420241
#Fit the model
dataaMod3 <- lm(V10 ~ V70*V71+V64,</pre>
               data = data)
#Multivariate results and univariate results with with type 3 Sum of squares
summary(Anova(dataaMod3, type = 3), univariate = T)
##
       Sum Sq
                                          F value
                                                             Pr(>F)
## Min. : 0.0514
                                             : 0.03165
                                                                 :0.000000
                           : 1.00
                                       Min.
                                                         Min.
                      Min.
   1st Qu.: 0.7689
                      1st Qu.: 1.00
                                       1st Qu.: 0.35114
                                                         1st Qu.:0.007575
##
## Median : 6.5209
                      Median: 1.00
                                       Median : 0.84032
                                                         Median :0.359752
                                             :18.84362
## Mean
         :159.4863
                      Mean
                            : 83.33
                                       Mean
                                                         Mean
                                                                :0.355986
## 3rd Qu.:107.4326
                      3rd Qu.: 1.00
                                       3rd Qu.: 7.19016
                                                         3rd Qu.:0.553740
## Max.
          :803.9033
                      Max.
                             :495.00
                                       Max.
                                             :85.80484
                                                         Max.
                                                                :0.858865
                                                         NA's
##
                                       NA's
                                              :1
                                                                :1
#Fit the model
dataaMod4 <- lm( V12~ V70*V71+V64,
               data = data)
#Multivariate results and univariate results with with type 3 Sum of squares
summary(Anova(dataaMod4, type = 3), univariate = T)
                                                              Pr(>F)
##
       Sum Sq
                             \mathsf{Df}
                                           F value
## Min.
         :
              0.0076
                            : 1.00
                                             : 0.00279
                                                                 :0.0000
                       Min.
                                       Min.
                                                          Min.
  1st Qu.:
              0.2411
                       1st Qu.: 1.00
                                        1st Qu.: 0.00848
                                                          1st Qu.:0.5420
## Median: 0.9550
                       Median: 1.00
                                      Median : 0.32842
                                                          Median :0.5669
## Mean
         : 251.7632
                       Mean : 83.33
                                       Mean
                                              :11.83624
                                                          Mean
                                                                 :0.5987
## 3rd Qu.: 119.7846
                       3rd Qu.: 1.00
                                        3rd Qu.: 0.37232
                                                          3rd Qu.:0.9267
## Max. :1349.2639
                       Max.
                              :495.00
                                        Max.
                                               :58.46921
                                                          Max.
                                                                 :0.9579
##
                                        NA's
                                                          NA's
                                               :1
                                                                  :1
source("http://www.reuningscherer.net/Multivariate/R/CSQPlot.r.txt")
```

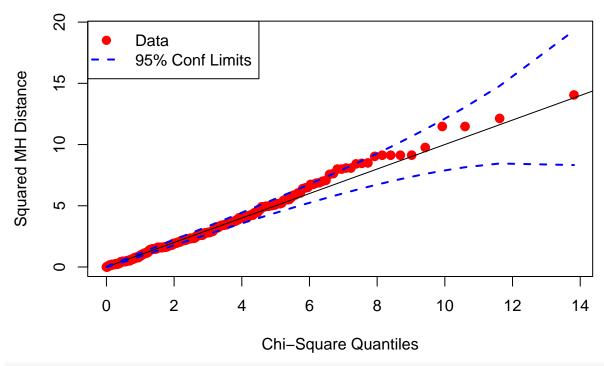
CSQPlot(model\$residuals, label = "Residuals from Env. Survey MANOVA")

## Chi-Square Quantiles for Residuals from Env. Survey MANOVA



CSQPlot(dataaMod2\$residuals, label = "Residuals from Env. Survey MANOVA")

# Chi-Square Quantiles for Residuals from Env. Survey MANOVA



#since the model assumptions of residuals: #multivariate normal distribution (which we expect will be true based on normality in each group)

```
#we can tell from the plots that two models both have normality property.
#Run a multi-response permutation procedure on the survey data
#install.packages("vegan")
library(vegan)
## Loading required package: permute
##
## Attaching package: 'permute'
## The following object is masked from 'package:DiscriMiner':
##
##
       getWithin
## Loading required package: lattice
## Registered S3 methods overwritten by 'vegan':
##
     method
                 from
##
     plot.rda
                 klaR
##
    predict.rda klaR
    print.rda
                 klaR
## This is vegan 2.5-7
##
## Attaching package: 'vegan'
## The following object is masked from 'package:klaR':
##
##
       rda
(mrpp1 <- mrpp(data[,c("V10", "V12")], data$V71))</pre>
##
## Call:
## mrpp(dat = data[, c("V10", "V12")], grouping = data$V71)
## Dissimilarity index: euclidean
## Weights for groups: n
## Class means and counts:
##
##
               2
                     3
         1
## delta 2.519 2.603 3.119
         461
               31
## n
## Chance corrected within-group agreement A: 0.001191
## Based on observed delta 2.534 and expected delta 2.537
## Significance of delta: 0.215
## Permutation: free
## Number of permutations: 999
\# The MRPP test is run on response variables "V10" and "V12" and the independent variable "V71". The de
```