# Graph-theoretic Models, Lecture 3, Segment 2

John Guttag

MIT Department of Electrical Engineering and Computer Science

#### Class Node

```
class Node(object): basically same as "object", but is useful for later revise
    def __init__(self, name):
        """Assumes name is a string"""
        self.name = name
    def getName(self):
        return self.name
    def __str__(self):
        return self.name
```

## Class Edge

```
class Edge(object):
     def __init__(self, src, dest):
          """Assumes src and dest are nodes"""
          self.src = src
          self.dest = dest
 def getSource(self):
    return self.src
def getDestination(self):
    return self.dest
                                        make edge have directions
     def __str__(self):
          return self.src.getName() + '->'\
                    + self.dest.getName()
```

#### Common Representations of Digraphs

- •Adjacency matrix
  - Rows: source nodes
  - Columns: destination nodes
  - Cell[s, d] = 1 if there is an edge from s to d0 otherwise
- Adjacency list
  - Associate with each node a list of destination nodes

#### Class Digraph, part 1

```
class Digraph(object): adjacency dict
    """edges is a dict mapping each node to a list of
    its children""
    def ___init___(self):
        self.edges = {}
    def addNode(self, node):
        if node in self.edges:
            raise ValueError('Duplicate node')
        else:
            self.edges[node] = []
    def addEdge(self, edge):
        src = edge.getSource()
        dest = edge.getDestination()
        if not (src in self.edges and dest in self.edges):
            raise ValueError('Node not in graph')
        self.edges[src].append(dest)
                                 value
                  key
```

6.00.2X LECTURE 3

### Class Digraph, part 2

```
def childrenOf(self, node):
    return self.edges[node]
def hasNode(self, node):
    return node in self.edges
def getNode(self, name):
                                     make sure name is correctly added
    for n in self.edges:
        if n.getName() == name:
            return n
    raise NameError(name)
def __str__(self):
    result = '
    for src in self.edges:
        for dest in self.edges[src]:
             result = result + src.getName() + '->'\
                      + dest.getName() + '\n'
    return result[:-1] #omit final newline
```

#### Class Graph

```
class Graph(Digraph):
    def addEdge(self, edge):
        Digraph.addEdge(self, edge)
        rev = Edge(edge.getDestination(), edge.getSource())
        Digraph.addEdge(self, rev)
```

- •Why is Graph a subclass of digraph?
- •Remember the substitution rule from 6.00.1x?
  - If client code works correctly using an instance of the supertype, it should also work correctly when an instance of the subtype is substituted for the instance of the supertype
- •Any program that works with a Digraph will also work with a Graph (but not vice versa)

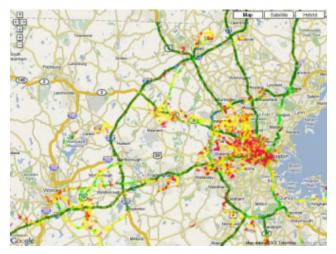
#### A Classic Graph Optimization Problem

- Shortest path from n1 to n2
  - Shortest sequence of edges such that
    - Source node of first edge is n1
    - Destination of last edge is n2
    - For edges, e1 and e2, in the sequence, if e2 follows e1 in the sequence, the source of e2 is the destination of e1
- Shortest weighted path
  - Minimize the sum of the weights of the edges in the path

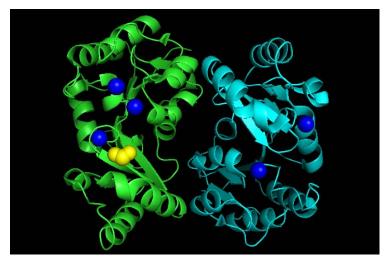
#### Some Shortest Path Problems

- Finding a route from one city to another
- Designing communication networks
- •Finding a path for a molecule through a chemical labyrinth

•••

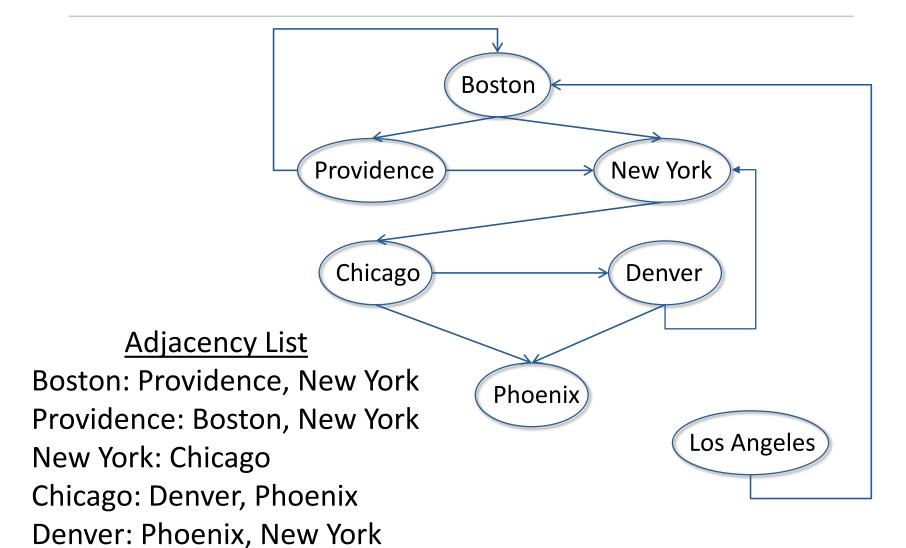


www.google.com



CC-BY Juliaytsai94

#### An Example



Los Angeles: Boston

#### **Build the Graph**

```
def buildCityGraph():
    g = Digraph()
    for name in ('Boston', 'Providence', 'New York', 'Chicago',
                 'Denver', 'Phoenix', 'Los Angeles'): #Create 7 nodes
        g.addNode(Node(name))
    g.addEdge(Edge(g.getNode('Boston'), g.getNode('Providence')))
    g.addEdge(Edge(g.getNode('Boston'), g.getNode('New York')))
    q.addEdge(Edge(g.getNode('Providence'), g.getNode('Boston')))
    g.addEdge(Edge(g.getNode('Providence'), g.getNode('New York')))
    g.addEdge(Edge(g.getNode('New York'), g.getNode('Chicago')))
    g.addEdge(Edge(g.getNode('Chicago'), g.getNode('Denver')))
    g.addEdge(Edge(g.getNode('Denver'), g.getNode('Phoenix')))
    g.addEdge(Edge(g.getNode('Denver'), g.getNode('New York')))
    g.addEdge(Edge(g.getNode('Chicago'), g.getNode('Phoenix')))
    g.addEdge(Edge(g.getNode('Los Angeles'), g.getNode('Boston')))
```

## Coming Up

Solutions to shortest path problem

12