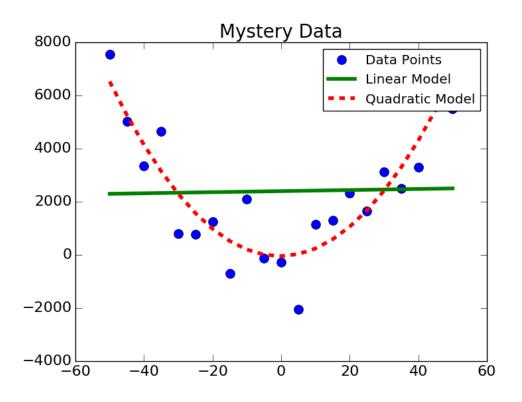
Understanding Experimental Data

How Good Are These Fits



- Relative to each other
- In an absolute sense



Relative to Each Other

accuracy

- •Fit is a function from the independent variable to the dependent variable
- Given an independent value, provides an estimate of the dependent value
- Which fit provides better estimates

Comparing Mean Squared Error

Ave. mean square error for linear model = 9372.73078965 Ave. mean square error for quadratic model = 1524.02044718

In an Absolute Sense

- Mean square error useful for comparing two different models for the same data
- Useful for getting a sense of absolute goodness of fit?Is 1524 good?
- •Hard to know, since there is no upper bound and not scale independent

■Instead we use coefficient of determination, R²,

$$R^{2} = 1 - \frac{\sum_{i} (y_{i} - p_{i})^{2}}{\sum_{i} (y_{i} - \mu_{i})^{2}}$$
mean

SSE(sum of residual squares)

SST(Total sum of squares)

to normalize variability

If You Prefer Code

$$R^{2} = 1 - \frac{\sum_{i} (y_{i} - p_{i})^{2}}{\sum_{i} (y_{i} - \mu)^{2}}$$

```
def rSquared(observed, predicted):
    error = ((predicted - observed)**2).sum()
    meanError = error/len(observed)
    return 1 - (meanError/numpy.var(observed))
```

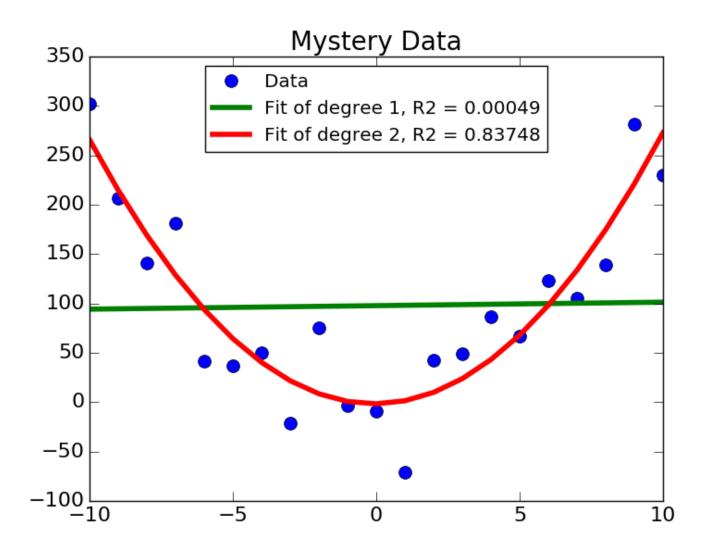
R^2

- ■By comparing the estimation errors (the numerator) with the variability of the original values (the denominator), R² is intended to capture the proportion of variability in a data set that is accounted for by the statistical model provided by the fit
- Always between 0 and 1 when fit generated by a linear regression and tested on training data
- •If $R^2 = 1$, the model explains all of the variability in the data. If $R^2 = 0$, there is no relationship between the values predicted by the model and the actual data. If $R^2 = 0.5$, the model explains half the variability in the data.

Testing Goodness of Fits

```
def genFits(xVals, yVals, degrees):
    models = []
    for d in degrees:
        model = pylab.polyfit(xVals, yVals, d)
        models.append(model)
    return models
def testFits(models, degrees, xVals, yVals, title):
    pylab.plot(xVals, yVals, 'o', label = 'Data')
    for i in range(len(models)):
        estYVals = pylab.polyval(models[i], xVals)
        error = rSquared(yVals, estYVals)
        pylab.plot(xVals, estYVals,
                   label = 'Fit of degree '\
                   + str(degrees[i])\
                   + ', R2 = ' + str(round(error, 5)))
    pylab.legend(loc = 'best')
    pylab.title(title)
```

How Well Fits Explain Variance



Can We Get a Tighter Fit?

