## Online Supplement for "Algorithms for Hybrid MILP/CP Models for a Class of Optimization Problems"

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## Data for Scheduling Problems

Table 1: Data for Problem 1

			Cost on Machine		
Order $(i)$	$r_i$	$d_i$	1	2	
1	2	16	10	6	
2	3	13	8	5	
3	4	21	12	7	

		Durations $(p_{im})$		
Order $(i)$	Machine	Set 1	Set 2	
1	1	10	5	
	2	14	7	
2	1	6	3	
	2	8	4	
3	1	11	5	
	2	16	7	

Table 2: Data for Problem 2

			Cost on Machine				
Order $(i)$	$r_i$	$d_{i}$	1	2	3		
1	2	16	10	6	8		
2	3	13	8	5	6		
3	4	21	12	7	10		
4	5	28	10	6	8		
5	10	24	8	5	7		
6	1	28	12	7	10		
7	2	23	12	7	10		

		Durations $(p_{im})$			
Order $(i)$	Machine	Set 1	Set 2		
1	1	10	5		
	2	14	7		
	3	12	6		
2	1	6	3		
	2	8	4		
	3	7	3		
3	1	11	2		
	2	16	4		
	3	13	3		
4	1	6	3		
	2	12	6		
	3	8	4		
5	1	10	2		
	2	16	4		
	3	12	3		
6	1	7	1		
	2	12	3		
	3	10	2		
7	1	10	1		
	2	8	2		
	3	10	1		

Table 3: Data for Problem 3

			Cos	Cost on Machine			
Order $(i)$	$r_i$	$d_i$	1	2	3		
1	2	36	10	6	8		
2	3	33	8	5	6		
3	4	31	12	7	10		
4	5	38	10	6	8		
5	10	34	8	5	7		
6	1	38	12	7	10		
7	2	33	12	10	11		
8	4	25	9	5	7		
9	10	38	10	6	8		
10	1	39	8	5	7		
11	5	30	15	9	12		
12	2	20	13	7	10		

		Durations $(p_{im})$			
Order $(i)$	Machine	Set 1	Set 2		
1	1	10	5		
	2	14	7		
	3	12	6		
2	1	6	3		
	2	8	4		
	3	7	3		
3	1	11	2		
	2	16	4		
	3	13	3		
4	1	6	3		
	2	12	6		
	3	8	4		
5	1	10	2		
	2	16	4		
	3	12	3		
6	1	7	1		
	2	12	3		
	3	10	2		

		Durations $(p_{im})$		
Order $(i)$	Machine	Set 1	Set 2	
7	1	10	1	
	2	13	2	
	3	10	1	
8	1	4	2	
	2	10	5	
	3	8	4	
9	1	2	4	
	2	4	6	
	3	3	6	
10	1	7	3	
	2	14	5	
	3	11	2	
11	1	8	2	
	2	16	3	
	3	12	2	
12	1	3	2	
	2	6	6	
	3	5	4	

Table 4: Data for Problem 4 - I

					3.6	1.		
			C	Cost on Machin				
Order $(i)$	$r_i$	$d_i$	1	2	3	4	5	
1	2	33	10	6	8	9	9	
2	3	34	8	5	6	7	7	
3	4	31	12	7	10	11	10	
4	5	33	10	6	8	9	8	
5	10	34	8	5	6	7	7	
6	1	34	12	7	10	11	10	
7	2	33	12	10	11	12	11	
8	4	25	9	5	7	9	8	
9	10	38	10	6	8	9	8	
10	1	37	8	5	6	7	6	
11	5	30	15	9	12	14	13	
12	2	20	13	7	10	12	11	
13	4	32	9	5	6	8	7	
14	6	20	10	6	8	10	9	
15	2	25	8	5	6	7	7	

Table 5: Data for Problem 4 - II

		Duratio	ons $(p_{im})$				Duratio	ons $(p_{im})$
Order (i)	Machine	Set 1	Set 2		Order $(i)$	Machine	Set 1	Set 2
1	1	10	5		9	1	2	4
	2	14	7			2	4	6
	3	12	6			3	3	6
	4	11	5			4	2	5
	5	13	6			5	3	5
2	1	6	3		10	1	7	2
	2	8	4			2	14	5
	3	7	3			3	11	3
	4	6	3			4	8	2
	5	7	4			5	10	3
3	1	11	2	-	11	1	8	2
	2	16	4			2	16	3
	3	13	3			3	12	2
	4	11	2			4	10	2
	5	12	3			5	11	2
4	1	6	3	-	12	1	3	2
	2	12	6			2	6	6
	3	8	4			3	5	4
	4	7	3			4	4	3
	5	8	4			5	5	3
5	1	10	2		13	1	4	1
	2	16	4			2	10	3
	3	12	3			3	7	3
	4	12	2			4	5	2
	5	13	2			5	6	2
6	1	7	1		14	1	2	2
	2	12	3			2	4	5
	3	10	2			3	4	5
	4	8	2			4	3	2
	5	9	2			5	3	3
7	1	10	1	-	15	1	7	4
	2	13	2			2	14	7
	3	10	1			3	13	6
	4	11	1			4	10	4
	5	12	1			5	11	5
8	1	4	2					
	2	10	5					
	3	8	4					
	4	5	3					
	5	6	3					

Table 6: Data for Problem 5 - I

			Cost on Machine						
Order $(i)$	$r_i$	$d_i$	1	2	3	4	5		
1	2	33	10	6	8	9	9		
2	3	34	8	5	6	7	7		
3	4	31	12	7	10	11	10		
4	5	33	10	6	8	9	8		
5	10	34	8	5	6	7	7		
6	1	34	12	7	10	11	10		
7	2	33	12	10	11	12	11		
8	4	25	9	5	7	9	8		
9	10	38	10	6	8	9	8		
10	1	37	8	5	6	7	6		
11	5	30	15	9	12	14	13		
12	2	20	13	7	10	12	11		
13	4	32	9	5	6	8	7		
14	6	20	10	6	8	10	9		
15	2	25	8	5	6	7	7		
16	3	34	9	5	7	9	8		
17	3	37	10	6	8	9	8		
18	7	38	8	5	6	7	6		
19	6	32	15	9	12	14	13		
20	0	30	13	7	10	12	11		

Table 7: Data for Problem 5 - II

		Dunstis				Dunsti	
O-1 (:)	M1-:		$\frac{\operatorname{ons}(p_{im})}{\operatorname{Cot}(2)}$	0-1(:)	M1-:		ons $(p_{im})$
Order (i)	Machine	Set 1	Set 2	Order (i)	Machine	Set 1	Set 2
1	1	10	5	11	1	8	2
	2	14	7		2	16	3
	3	12	6		3	12	2
	4	11	5		4	10	2
	5	13	6		5	11	2
2	1	6	3	12	1	3	2
	2	8	4		2	6	6
	3	7	3		3	5	4
	4	6	3		4	4	3
	5	7	4		5	5	3
3	1	11	2	13	1	4	1
	2	16	4		2	10	3
	3	13	3		3	7	3
	4	11	2		4	5	2
	5	12	3		5	6	2
4	1	6	3	14	1	2	2
	2	12	6		2	4	5
	3	8	4		3	4	5
	4	7	3		4	3	2
	5	8	4		5	3	3
5	1	10	2	15	1	7	4
	2	16	4		2	14	7
	3	12	3		3	13	6
	4	12	2		4	10	4
	5	13	2		5	11	5
6	1	7	1	16	1	3	2
	2	12	3		2	8	4
	3	10	2		3	7	3
	4	8	2		4	5	2
	5	9	2		5	6	3
7	1	10	1	17	1	6	3
	2	13	2		2	12	6
	3	10	1		3	10	4
	4	11	1		4	7	3
	5	12	1		5	8	4
8	1	4	2	18	1	2	2
	2	10	5		2	8	4
	3	8	4		3	6	3
	4	5	3		4	13	2
	5	6	3		5	4	2
9	1	2	4	19	1	4	1
	2	4	6		2	7	3
	3	3	6		3	6	2
	4	2	5		4	5	2
10	5	3	5	- 00	5	5	2
10	1	7	2	20	1	5	1
	2	14	5		2	7	2
	3	11	3		3	7	1
	4	8	$\frac{2}{3}$		4	6	1 $1$
	5	10	<del></del>		5	6	1