ANALOG-11.14.21

EE23BTECH11006 - Ameen Aazam*

Question : You are riding in an automobile of mass 3000 kg. Assuming that you are examining the oscillation characteristics of its suspension system. The suspension sags 15 cm when the entire automobile is placed on it. Also, the amplitude of oscillation decreases by 50

(a) The spring constant K
(b) The damping constant b for the spring and shock absorber system of one wheel, assuming that each wheel supports 750 kg.

Solution :

Part-a: We know 15 cm = 0.15 m. Initially, the normal reaction on each of the wheels,

$$N = Kx \tag{1}$$

$$\Rightarrow 750g = 0.15 \cdot K \quad \text{(The suspension sags 15 cm)} \tag{2}$$

$$\Rightarrow K = \frac{750 \cdot 9.8}{0.15}\ \text{N/m} \quad (g = 9.8\ \text{m/s}^2) \tag{3}$$

$$\Rightarrow K = 4.9 \times 10^4\ \text{N/m} \tag{4}$$

Part-b: Now, as the weight is evenly distributed over the four wheels, we can consider each wheel-suspension system as a spring-mass system with mass, $m = 750$ kg, and $K = 4.9 \times 10^4$ N/m. So the time period of oscillation will be close to $T = \frac{\pi}{2}\sqrt{\frac{m}{K}}$.
Now for any point in time, if the amplitude is A with initial amplitude A_0, then we have,

$$A = A_0 e^{-(\beta t)} \quad (\beta = \frac{b}{2m}) \tag{5}$$

$$\Rightarrow \beta = \frac{\ln(2)}{2\pi}\sqrt{\frac{K}{m}} \tag{6}$$

$$\Rightarrow b = 1337.53\ \text{kg/s} \tag{7}$$

Answer :

Part-a: The spring constant, $K = 4.9 \times 10^4$ N/m.
Part-b: The damping constant, $b = 1337.53$ kg/s.