

VISVESVARAYA TECHNOLOGICAL UNIVERSITY

“JnanaSangama”, Belgaum -590014, Karnataka.



LAB REPORT

on

Artificial Intelligence (23CS5PCAIN)

Submitted by

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in partial fulfillment for the award of the degree of

BACHELOR OF ENGINEERING

in

COMPUTER SCIENCE AND ENGINEERING



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Department of Computer Science and Engineering



CERTIFICATE

This is to certify that the Lab work entitled “Artificial Intelligence (23CS5PCAIN)” carried out by Ameena Yasmeen (1BM23CS027), who is a bona fide student of **B.M.S. College of Engineering**. It is in partial fulfillment for the award of **Bachelor of Engineering in Computer Science and Engineering** of the Visvesvaraya Technological University, Belgaum. The Lab report has been approved as it satisfies the academic requirements in respect of an Artificial Intelligence (23CS5PCAIN) work prescribed for the said degree.

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Github Link:

<https://github.com/Ameena1BM23CS27/AI-LAB>



CERTIFICATE OF ACHIEVEMENT

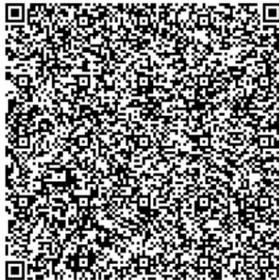
The certificate is awarded to

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for successfully completing

Artificial Intelligence Foundation Certification

on November 25, 2025



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Congratulations! You make us proud!

Satheesh B.N.

Satheesh B. Nanjappa
Senior Vice President and Head
Education, Training and Assessment
Infosys Limited

Program 1

Implement Tic - Tac - Toe Game

Implement vacuum cleaner agent

Algorithm:

Artificial Intelligence

PAGE NO. / /
DATE / /

Lab 1
A Implementation of Tic-tac-toe game.

→ Pseudocode

```
def print_board(board):
    for row in board:
        print(" ".join(row))

def check_winner(board, player):
    # Check all rows
    for row in board:
        if row == [player] * 3:
            return True
    # Check all columns
    for col in range(3):
        if [row[col] for row in board] == [player] * 3:
            return True
    # Check both diagonals
    if [board[i][i] for i in range(3)] == [player] * 3 or [board[i][2-i] for i in range(3)] == [player] * 3:
        return True
    return False

def check_draw(board):
    return True if not any([cell == " " for row in board for cell in row]) else False

def player_move(board):
    while True:
        row = int(input("Enter row (0, 1, 2): "))
        col = int(input("Enter column (0, 1, 2): "))
        if board[row][col] == " ":
            board[row][col] = "X"
            break
        else:
            print("Cell is already occupied. Try again.")
```

<pre> PAGE NO. / / DATE / / def get_available_moves(board): return all((row, col) where cell is empty) </pre> <pre> def try_move(board, row, col, player): place player's mark temporarily check winner undo move return result </pre> <pre> def system_move(board): print("System's move:") for each available cell: if move makes "O" win: place "O" there print("Winning move") return </pre> <pre> for each available cell: if move makes "X" win: place "O" there print("Blocking move") return </pre> <pre> pick random empty cell place "O" there print("Random move") </pre> <pre> def main(): create empty 3x3 board </pre>	<pre> PAGE NO. / / DATE / / print("Welcome! You are X, System is O") print_board(board) while True: player_move(board) print_board(board) if check_winner(board, "X"): print("You Win!") break if check_draw(board): print("It is a draw!") break system_move(board) print_board(board) if check_winner(board, "O"): print("System wins!") break if check_draw(board): print("It's a draw!") break </pre> <pre> if __name__ == "__main__": main() </pre>
--	---

Output: Welcome to tic-tac-toe! You are X, System is O.

	X	
X		

Enter your move as row, col (1-3 for both): 1, 2.

	X	
X		

System's move!

System placed an 'O' at 3, 1 (random move)

	X	
O		

Sg Enter your move as row, col (1-3 for both): 1, 3

	X	X
O		

System's move

System place an 'O' at (1, 1) (blocking move)

O	X	X
O		

Enter your move as row, col (1-3 for both): 2, 2

O	X	X
O	X	
O		

System's move

System placed an 'O' at 2, 1 (winning move)

O	X	X
O	X	
O		

System wins! Better luck next time.

Code:

TIC-TAC-TOE :

Program:

```
def print_board(board):
    print("\n  0  1  2")
    for i in range(3):
        print(f" {i} {board[i][0]} | {board[i][1]} | {board[i][2]}")
        if i < 2:
            print(" -----")
    print()

def check_winner(board):      # Check
    rows      for row in board:      if row[0]
    == row[1] == row[2] != '-':
        return row[0]

    # Check columns      for col in range(3):      if
    board[0][col] == board[1][col] == board[2][col] != '-':
        return board[0][col]

    # Check diagonals      if board[0][0] == board[1][1]
    == board[2][2] != '-':
        return board[0][0]      if board[0][2] ==
    board[1][1] == board[2][0] != '-':
        return board[0][2]

    return None

def is_board_full(board):
    for row in board:      if
    '-' in row:      return
    False
    return True

def is_valid_move(board, row, col):
    return 0 <= row < 3 and 0 <= col < 3 and board[row][col] == '-'

def get_player_move(player):
    while True:      try:
        move = input(f"Player {player}, enter your move (row col): ")
```

```

        row, col = map(int, move.split())
return row, col      except (ValueError,
IndexError):
    print("Invalid input! Please enter row and column as two numbers (0-2).")

def play_tic_tac_toe():
# Initialize empty board
    board = [['-' for _ in range(3)] for _ in range(3)]
current_player = 'X'

    print("Welcome to Tic-Tac-Toe!")
print("Enter moves as 'row col' ")
print("Positions are numbered 0, 1, 2")

    # Main game loop
while True:
    print_board(board)

    # Get player move
    row, col = get_player_move(current_player)

    # Check if move is valid      if
is_valid_move(board, row, col):
    # Make the move
    board[row][col] = current_player

    # Check for winner
winner = check_winner(board)
if winner:
    print_board(board)
print(f" Player {winner} wins!")
    break

    # Check for tie
if is_board_full(board):
    print_board(board)
print(" It's a tie!")
    break

    # Switch players      current_player = 'O' if
current_player == 'X' else 'X'      else:
    print("Invalid move! That position is taken or out of bounds.")

def main():
while True:

```

```

play_tic_tac_toe()

# Ask to play again      play_again = input("\nDo you want to
play again? (y/n): ").lower()      if play_again != 'y':
    print("Thanks for playing!")
    break

# Run the game  if __name__ ==
== "__main__":    main()

```

Output:

```

Welcome to Tic-Tac-Toe!
Enter moves as 'row col' (e.g., '1 2')
Positions are numbered 0, 1, 2
      0   1   2
0 - | - | -
-----
1 - | - | -
-----
2 - | - | -
Player X, enter your move (row col):  0 1
      0   1   2
0 - | X | -
-----
1 - | - | -
-----
2 - | - | -
Player O, enter your move (row col):  1 1
      0   1   2
0 - | X | -
-----
1 - | O | -
-----
2 - | - | -
Player X, enter your move (row col):  0 0
      0   1   2
0 X | X | -
-----
1 - | O | -
-----
2 - | - | -
Player O, enter your move (row col):  1 1
Invalid move! That position is taken or out of bounds.
      0   1   2
0 X | X | -
-----
1 - | O | -
-----
2 - | - | -
Player O, enter your move (row col):  2 2
      0   1   2
0 X | X | X
-----
1 - | O | -
-----
2 - | - | O
Player X, enter your move (row col):  0 2
      0   1   2
0 X | X | X
-----
1 - | O | -
-----
2 - | - | O
 Player X wins!
Do you want to play again? (y/n):  n
Thanks for playing!

```

Vacuum cleaner

```
import random

# Function to clean a room
def clean_room(rooms, position):
    if rooms[position] == 1:
        print(f"Room {position+1} is Dirty. Cleaning...")
        rooms[position] = 0
        print(f"Room {position+1} is now Clean.")
    else:
        print(f"Room {position+1} is already Clean.")

# Function to move to the next room
def move(position, total_rooms):
    position = (position + 1) % total_rooms
    print(f"Moving to Room {position+1}")
    return position

# Function to run the vacuum cleaner
def run(rooms, steps):
    position = 0 # start at first room
    for _ in range(steps):
        clean_room(rooms, position)
        position = move(position, len(rooms))
    print("Final Room Status:", rooms)

# Initialize 4 rooms randomly (0 = clean, 1 = dirty)
rooms = [random.choice([0, 1]) for _ in range(4)]
print("Initial Room Status:", rooms)

# Run for 8 steps
run(rooms, 8)
```

```
Initial Room Status: [0, 1, 0, 1]
Room 1 is already Clean.
Moving to Room 2
Room 2 is Dirty. Cleaning...
Room 2 is now Clean.
Moving to Room 3
Room 3 is already Clean.
Moving to Room 4
Room 4 is Dirty. Cleaning...
Room 4 is now Clean.
Moving to Room 1
Room 1 is already Clean.
Moving to Room 2
Room 2 is already Clean.
Moving to Room 3
Room 3 is already Clean.
Moving to Room 4
Room 4 is already Clean.
Moving to Room 1
Final Room Status: [0, 0, 0, 0]
```

Program 2

Implement 8 puzzle problems using Depth First Search (DFS)

Implement Iterative deepening search algorithm

Algorithm:

Lab-2.

1. 8 puzzle - Misplaced tiles

function A-start-Misplaced(start, goal):
OPEN = priority queue ordered by $f = g + h$
CLOSED = empty set

$g(\text{start}) = 0$
 $h(\text{start}) = \text{Misplaced}(\text{start}, \text{goal})$
push(f , start, path = [start]) into OPEN

while OPEN not empty:
(f , state, path) = pop lowest f from OPEN
if state == goal:
return path

add state to CLOSED

for neighbor in Expand(state):
if neighbor not in CLOSED:
 $g(\text{neighbor}) = g(\text{state}) + h$
 $h(\text{neighbor}) = \text{misplaced}(\text{neighbor}, \text{goal})$
 $f(\text{neighbor}) = g(\text{neighbor}) + h(\text{neighbor})$
push(f , neighbor, path + {neighbor})
into OPEN

return "No solution"

function Misplaced(state, goal):
count = 0
for i in 0...8:
if ($\text{state}[i] \neq 0$ and $\text{state}[i] \neq \text{goal}[i]$):
count = count + 1

2. Iterative Deepening Depth First search

Algorithm

1. set the initial depth limit $L=0$
2. start a loop that will increment L in each iteration
3. Inside the loop perform a depth-limited DFS from the start node, with the current depth limit L .
4. The depth limit DFS function works as follows:
 - If the current node is the goal node, return the path to this node
 - If the current depth is equal to the depth limit stop exploring this path.
 - For each unvisited child of the current node recursively call the depth-limited DFS function for the child with the depth increased by 1.
5. If the depth-limited DFS returns a solution, the IDDFS algorithm terminates and returns the solution.
6. If the depth-limited DFS completes without finding a solution increment the depth limit $L=L+1$ and repeat from step 3.
7. If the search space is finite and a solution exists, the algorithm is guaranteed to find it.

Pseudocode:

Function IDDFS (start-node, goal-node)

depth = 0

loop forever:

result = DLS (start-node, goal-node, depth)

if result is a solution:
return resH

if resH is "cutoff":
depth = depth + 1

else:

return "failure"

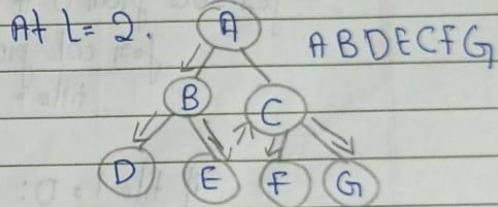
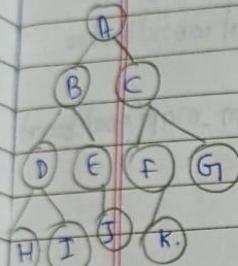
Opt(A):-

A = start

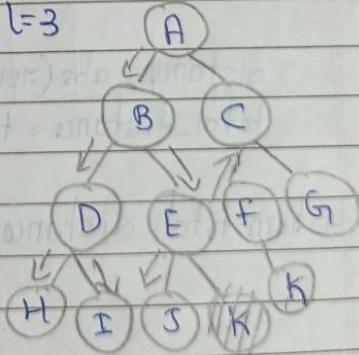
K = goal

Iteration:- At L=0 (A) - A

At L=1 = (A) - ABC



At L=2



ABDHI EJCFK

Code:

Misplaced Tiles – 8 puzzle import
heapq

```

# ----- Heuristic: Misplaced Tiles ----- def
misplaced_tiles(state, goal):
    """Count number of misplaced tiles (ignores blank 0)."""
    return sum(1 for i in range(len(state)) if state[i] != 0 and state[i] != goal[i])

# ----- Puzzle Neighbors ----- def
get_neighbors(state):
    neighbors = []    idx = state.index(0) # position of blank    x, y = divmod(idx, 3)

    moves = [(-1,0),(1,0),(0,-1),(0,1)] # up, down, left, right
    for dx, dy in moves:
        nx, ny = x + dx, y + dy      if 0 <= nx < 3 and 0 <= ny < 3:
            new_idx = nx * 3 + ny      new_state = list(state)
            new_state[idx], new_state[new_idx] = new_state[new_idx], new_state[idx]
            neighbors.append(tuple(new_state))
    return neighbors

# ----- A* Search ----- def
a_star_misplaced(start, goal):
    open_list = []    heapq.heappush(open_list, (misplaced_tiles(start, goal), 0, start, [start]))    closed = set()

    while open_list:
        f, g, state, path = heapq.heappop(open_list)

        if state == goal:
            return path # solution found

        if state in closed:
            continue
        closed.add(state)

        for neighbor in get_neighbors(state):
            if neighbor not in closed:
                g_new = g + 1      h_new =
                misplaced_tiles(neighbor, goal)      f_new =
                g_new + h_new
                heapq.heappush(open_list, (f_new, g_new, neighbor, path + [neighbor]))    return None # no solution found

# ----- Run Example ----- if
__name__ == "__main__":
    start = (1, 2, 3,
             4, 5, 6,

```

```
(0, 7, 8)
```

```
goal = (1, 2, 3,  
        4, 5, 6,  
        7, 8, 0)
```

```
solution = a_star_misplaced(start, goal)
```

```
if solution:  
    print("Solution found in", len(solution)-1, "moves.")  
for step in solution:      for i in range(0, 9, 3):  
    print(step[i:i+3])      print("----")  else:  
    print("No solution found.") Output:
```

```
Solution found in 2 moves.  
(1, 2, 3)  
(4, 5, 6)  
(0, 7, 8)  
----  
(1, 2, 3)  
(4, 5, 6)  
(7, 0, 8)  
----  
(1, 2, 3)  
(4, 5, 6)  
(7, 8, 0)  
----
```

```
Manhattan distance – 8 puzzle import  
heapq
```

```
# ----- Heuristic: Manhattan Distance ----- def  
manhattan_distance(state, goal):  
    """Sum of Manhattan distances of each tile from its goal position.""""  
    distance = 0    for i, tile in enumerate(state):      if tile != 0: # skip the  
    blank          goal_pos = goal.index(tile)          distance += abs(i // 3 -  
    goal_pos // 3) + abs(i % 3 - goal_pos % 3)    return distance  
  
# ----- Puzzle Neighbors ----- def  
get_neighbours(state):
```

```

neighbors = []    idx = state.index(0)
# blank position  x, y = divmod(idx,
3)

    moves = [(-1,0),(1,0),(0,-1),(0,1)] # up, down, left, right
    for dx, dy in moves:
        nx, ny = x + dx, y + dy      if
        0 <= nx < 3 and 0 <= ny < 3:
            new_idx = nx * 3 + ny      new_state = list(state)
            new_state[idx], new_state[new_idx] = new_state[new_idx], new_state[idx]
            neighbors.append(tuple(new_state))  return neighbors

# ----- A* Search -----
def
a_star_manhattan(start, goal):
    open_list = []    heapq.heappush(open_list, (manhattan_distance(start, goal),
0, start, [start]))  closed = set()

    while open_list:
        f, g, state, path = heapq.heappop(open_list)

        if state == goal:
            return path # solution found

            if state in closed:
                continue
                closed.add(state)

            for neighbor in get_neighbors(state):
                if neighbor not in closed:
                    g_new = g + 1      h_new =
                    manhattan_distance(neighbor, goal)      f_new =
                    g_new + h_new
                    heapq.heappush(open_list, (f_new, g_new, neighbor, path + [neighbor]))  return
None # no solution found

# ----- Run Example -----
if
__name__ == "__main__":
    start = (1, 2, 3,
4, 5, 6,
0, 7, 8)

    goal = (1, 2, 3,
4, 5, 6,
7, 8, 0)

```

```

solution = a_star_manhattan(start, goal)

if solution:
    print("Solution found in", len(solution)-1, "moves.")
for step in solution:      for i in range(0, 9, 3):
print(step[i:i+3])      print("----")  else:
    print("No solution found.")

```

Output:

```

Solution found in 2 moves.
(1, 2, 3)
(4, 5, 6)
(0, 7, 8)
-----
(1, 2, 3)
(4, 5, 6)
(7, 0, 8)
-----
(1, 2, 3)
(4, 5, 6)
(7, 8, 0)
-----

```

Iterative Deepening Depth First Search # -

----- Depth Limited Search -----

```
def DLS(graph, node, goal, limit, visited):
```

```
if node == goal:
```

```
    return True
```

```
if limit == 0:
```

```
return False
```

```
visited.add(node)  for neighbor in graph.get(node,
[]):      if neighbor not in visited:      if
DLS(graph, neighbor, goal, limit - 1, visited):
```

```
    return True
```

```
return False
```

```
# ----- IDDFS ----- def IDDFS(graph,
start, goal, max_depth):  for depth in
range(max_depth + 1):      visited = set()
if DLS(graph, start, goal, depth, visited):
    return True
```

```

return False

# ----- Example Run ----- if
__name__ == "__main__":
graph = {
    'A': ['B', 'C'],
    'B': ['D', 'E'],
    'C': ['F'],
    'D': [],
    'E': ['F'],
    'F': []
}

start = 'A'
goal = 'F'

if IDDFS(graph, start, goal, max_depth=3):
    print(f"Goal {goal} found within depth limit.")  else:
    print(f"Goal {goal} not found within depth limit.")

```

Output:

```

if __name__ == "__main__":
graph = {
    'A': ['B', 'C'],
    'B': ['D', 'E'],
    'C': ['F'],
    'D': [],
    'E': ['F'],
    'F': []
}

start = 'A'
goal = 'F'

if IDDFS(graph, start, goal, max_depth=3):
    print(f"Goal {goal} found within depth limit.")
else:
    print(f"Goal {goal} not found within depth limit.")

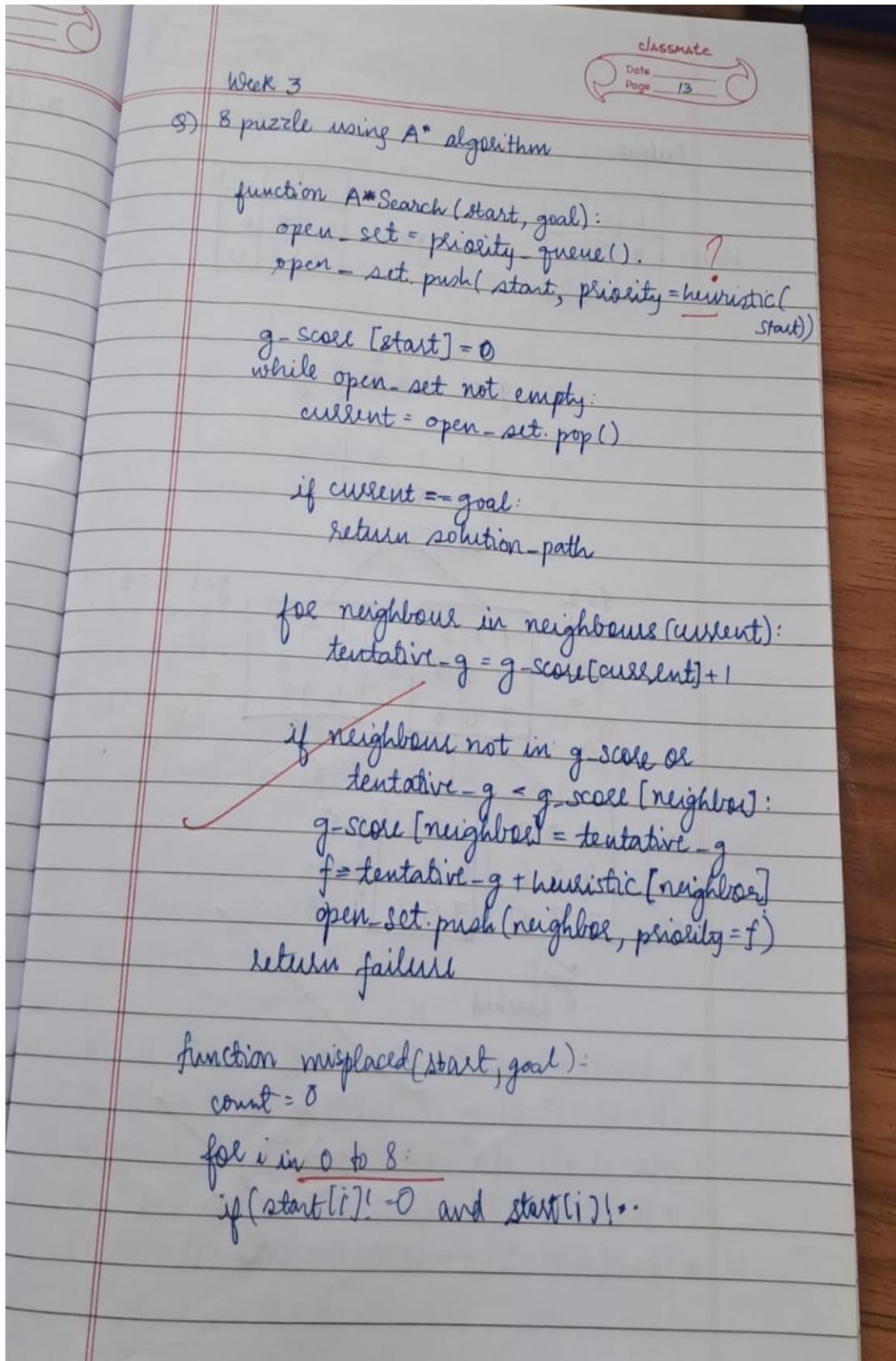
```

Goal F found within depth limit.

Program 3 Implement A*

search algorithm

Algorithm:



Output:

1	2	3
4	5	6
0	7	8

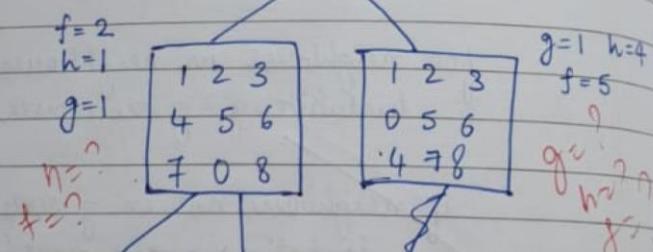
start =

1	2	3
4	5	6
7	8	0

goal =

$$g=0 \quad h=\frac{2}{3} \quad f=g+h$$

1	2	3
4	5	6
0	7	8



$f=2$	1 2 3	1 2 3	$f=5$
$g=2$	4 5 6	4 0 6	$g=2$
$h=0$	7 8 0	7 5 8	$h=3$

goal reached

STOP
 VOTE

 Week 4
 N Queens

Cost calc

Initial
Queens

Board

Cost f
same

check

- 1) Q1 (
 - 2) Q1 (
 - 3) Q1 (
 - 4) Q2 (
 - 5) Q2 (
 - 6) Q3 (
- Jot

```

Code: import
heapq

# Goal state for the 8 puzzle
goal_state = [[1, 2, 3],
              [4, 5, 6],
              [7, 8, 0]] # 0 is the blank space

# Directions: up, down, left, right
moves = [(1, 0), (-1, 0), (0, 1), (0, -1)]


def manhattan_distance(state):
    """Calculate Manhattan distance heuristic for a given state."""
    distance = 0
    for i in range(3):
        for j in range(3):
            value = state[i][j]
            if value != 0:
                target_x = (value - 1) // 3
                target_y = (value - 1) % 3
                distance += abs(i - target_x) + abs(j - target_y)
    return distance


def find_blank(state):
    """Find the position of blank (0) in the puzzle."""
    for i in range(3):
        for j in range(3):
            if state[i][j] == 0:
                return i, j


def state_to_tuple(state):
    """Convert list state to tuple (for hashing in sets)."""
    return tuple(tuple(row) for row in state)


def a_star(start_state):
    """A* algorithm to solve 8-puzzle."""
    start_h = manhattan_distance(start_state)
    pq = [(start_h, 0, start_state, [])] # (f, g, state, path)
    visited = set()

    while pq:
        f, g, state, path = heapq.heappop(pq)

        if state == goal_state:
            return path + [state]

```

```

visited.add(state_to_tuple(state))
x, y = find_blank(state)

for dx, dy in moves:
    new_x, new_y = x + dx, y + dy
    if 0 <= new_x < 3 and 0 <= new_y < 3:
        new_state = [row[:] for row in state] # deep copy
        # Swap blank with neighbor
        new_state[x][y], new_state[new_x][new_y] =
        new_state[new_x][new_y], new_state[x][y]

        if state_to_tuple(new_state) not in visited:           h
= manhattan_distance(new_state)           heapq.heappush(pq,
(g + 1 + h, g + 1, new_state, path +
[state])))

return None # No solution found

# Example usage:
start_state = [[1, 2, 3],
               [4, 5, 6],
               [0, 7, 8]]

solution = a_star(start_state)

print("Steps to reach the goal:")
for step in solution:   for row
in step:      print(row)
print()

```

Output:

```

Steps to reach the goal:
[1, 2, 3]
[4, 5, 6]
[0, 7, 8]

[1, 2, 3]
[4, 5, 6]
[7, 0, 8]

[1, 2, 3]
[4, 5, 6]
[7, 8, 0]

```

Program 4

Implement Hill Climbing search algorithm to solve N-Queens problem

Algorithm:

Week 4

N Queens using Hill Climbing search

Cost calculation -

			Q
		Q	
Q			

Initial state -

Queens at col 0, row 3
C₁, R₁
C₂, R₃
C₃, R₀

Board = [3, 1, 2, 0]

Cost functions:
same row / column / diagonal
 $\hookrightarrow |\text{row diff}| = |\text{col diff}|$

Check pairs -

- 1) Q₁(3, 0) and Q₂(1, 1)
 $|3-1| \neq |0-1| \times$
- 2) Q₁(3, 0) and Q₃(2, 2) $\rightarrow |3-2| = |0-2| \times$
- 3) Q₁(3, 0) and Q₄(0, 3) $\rightarrow |3-0| = |0-3| = 3 \checkmark$
- 4) Q₂(1, 1) and Q₃(2, 2) $\rightarrow |1-2| = |1-2| = 1 \checkmark$
- 5) Q₂(1, 1) and Q₄(0, 3) $\rightarrow |1-0| \neq |1-3| \times$
- 6) Q₃(2, 2) and Q₄(0, 3) $\rightarrow |2-0| = |2-3| \times$

Jot. conflicts = 2

generate neighbors
 Move queen to other rows for each col
 Q1 at row 4, column 1
 Move to row 1 → [1, 2, 3,]
 [0, 1, 2, 0]
 row 2 → [1, 1, 2, 0]
 row 3 → [2, 1, 2, 0]

Evaluate cost for neighbors -

	Cost
[0, 1, 2, 0]	2
[1, 1, 2, 0]	2
[2, 1, 2, 0]	2
[3, 0, 2, 0]	2
[3, 2, 2, 0]	1 ✓
[3, 3, 2, 0]	2
[3, 1, 0, 0]	2
[3, 1, 1, 0]	2
[3, 1, 3, 0]	2
[3, 1, 2, 1]	2
[3, 1, 2, 2]	2
[3, 1, 2, 3]	2

Update state

Best neighbor = [3, 2, 2, 0] (cost = 1)

Algorithm -

```
def random_restart ( N , max ) :  
    for i in 1 to max :  
        current ← random_board ( n )  
    while true :  
        neighbours ← generate_neighbours ( current )  
        best_neighbour ← neighbour in neighbours  
        with min_conflicts ( neighbour )  
        if evaluate ( best_neighbour ) >= evaluate  
            ( current ) :  
            break  
        else :  
            current ← best_neighbour  
        if evaluate ( current ) == 0 :  
            return current  
    return failure
```

~~Output:~~

Enter number of queens : 4

Enter initial state as row positions for each column.

For N = 4

Initial state : 3 1 2 0

Cost = 2

Final state : [3, 2, 2, 0]

Cost = 1

8 8
8

Code:
import random

```

# Heuristic: number of pairs of queens attacking each other
def calculate_cost(state):
    cost = 0
    n = len(state)
    for i in range(n):
        for j in range(i + 1, n):
            if state[i] == state[j] or abs(state[i] - state[j]) == abs(i - j):
                cost += 1
    return cost

```

```

# Generate all neighbors of the current state
def get_neighbors(state):
    neighbors = []
    n = len(state)
    for col in range(n):
        for row in range(n):
            if state[col] != row: # move queen in col to new row
                neighbor = state.copy()
                neighbor[col] = row
                neighbors.append(neighbor)
    return neighbors

```

```

# Hill climbing algorithm
def hill_climb(initial_state):
    current = initial_state
    current_cost = calculate_cost(current)

    print(f"Initial state: {current}, Cost = {current_cost}")

    while True:
        neighbors = get_neighbors(current)
        best_neighbor = None
        best_cost = current_cost

        # Find the best neighbor
        for neighbor in neighbors:
            cost = calculate_cost(neighbor)
            if cost < best_cost:
                best_cost = cost
                best_neighbor = neighbor

        # If no better neighbor is found → stop      if
        best_neighbor is None:          print(f"Final state: {current},
                                         Cost = {current_cost}")      return current, current_cost

        # Move to the better neighbor      current,
        current_cost = best_neighbor, best_cost
        print(f"Move to: {current}, Cost = {current_cost}")

```

```

# Example usage if
__name__ == "__main__":
    n = int(input("Enter number of queens (N): "))
    print("Enter initial state as space-separated row positions for each column.")
    print("Example for N=4: '1 3 0 2' means queen at (0,1), (1,3), (2,0), (3,2.)")

    initial_state = list(map(int, input("Initial state: ").split()))

    if len(initial_state) != n:
        print("Invalid input: Length of initial state must be N.")
    else:
        solution, cost = hill_climb(initial_state)

        if cost == 0:
            print("Goal state reached!")
        else:
            print("Stuck in local minimum.")

```

Output:

```

Enter number of queens (N): 4
Enter initial state as space-separated row positions for each column.
Example for N=4: '1 3 0 2' means queen at (0,1), (1,3), (2,0), (3,2).
Initial state: 3 1 2 0
Initial state: [3, 1, 2, 0], Cost = 2
Final state: [3, 1, 2, 0], Cost = 2

```

Program 5

Simulated Annealing to Solve 8-Queens problem

Algorithm:

Simulated Annealing - 4 Queens

Algorithm:

```
def annealing(board):
    current ← initial state
    T ← a large value
    while T > 0 do:
        next ← a random neighbor
        ΔE ← current cost - next cost
        if ΔE > 0 then
            current ← next
        else
            current ← next with prob  $p = e^{-\frac{\Delta E}{T}}$ 
        end if
        decrease T
    end while
    return current
```

~~Stuck~~

Output:

Initial state: [1 2 0 2]

Final state: [1, 3, 0, 2]

Cost = 0

Board:

.	.	Q	.
Q	.	.	.
.	.	.	Q
.	Q	.	.

Code:

```

import random
import math

def cost(state, N):
    """Compute number of attacking queen pairs."""
    conflicts = 0
    for i in range(N):
        for j in range(i+1, N):
            if state[i] == state[j] or abs(state[i] - state[j]) == abs(i - j):
                conflicts += 1
    return conflicts

def random_neighbor(state, N):
    """Generate a neighbor by moving one queen to another row in a random column."""
    neighbor = state.copy()
    col = random.randrange(N)
    new_row = random.randrange(N-1)
    if new_row >= neighbor[col]:
        new_row += 1
    neighbor[col] = new_row
    return neighbor

def simulated_annealing(N, T0=5.0, alpha=0.995, Tmin=1e-6, max_iters=50000):
    """Solve N-Queens using simulated annealing."""
    # Random initial state: one queen per column
    state = [random.randrange(N) for _ in range(N)]
    current_cost = cost(state, N)
    T = T0
    it = 0

    while T > Tmin and it < max_iters and current_cost != 0:
        neighbor = random_neighbor(state, N)
        neighbor_cost = cost(neighbor, N)
        delta = neighbor_cost - current_cost

        if delta <= 0 or random.random() < math.exp(-delta / T):
            state, current_cost = neighbor, neighbor_cost

        T *= alpha
        it += 1

    return state, current_cost

def print_board(state, N):
    """Pretty-print the board with row and column numbers."""
    print(" " + " ".join(str(c) for c in range(N))) # column indices
    for r in range(N):
        row = f" {r} " # row index
        for c in range(N):
            if state[c] == r:
                row += "Q"
            else:
                row += "."
        print(row)

```

```

        row += "Q " if state[c] == r else ". "
print(row)
    print()

# -----
# User input
# -----
N = int(input("Enter number of queens (N):"))

solution, c = simulated_annealing(N)

print(f"\nFinal state (col -> row): {solution}")
print("Cost:", c)
print("Board:")
print_board(solution, N)

```

Output:

```

Enter number of queens (N): 5

Final state (col -> row): [4, 1, 3, 0, 2]
Cost: 0

Board:
  0 1 2 3 4
0 . . . Q .
1 . Q . . .
2 . . . . Q
3 . . Q . .
4 Q . . .

```

Program 6

Create a knowledge base using propositional logic and show that the given query entails the knowledge base or not.

Algorithm:

15/10/25 Week 5

Create a knowledge base using propositional logic and show that the given query entails the knowledge base or not.

Example:
If it is raining, the ground gets wet.
 $P \rightarrow Q$

If the ground is wet, the grass is slippery.
 $Q \rightarrow R$

It is raining
Is the grass slippery? (α)

P: Raining
Q: Ground is wet
R: Grass is slippery

Knowledge base (KB):
1. $P \rightarrow Q$
2. $Q \rightarrow R$
3. P

Query (α): R

Check: $KB \models \alpha$

Truth table enumeration -

P	Q	R	$P \rightarrow Q$	$Q \rightarrow R$	$KB = (P \rightarrow Q) \wedge (Q \rightarrow R) \wedge P$	Entails R?
T	T	T	T	T	T	True
T	T	F	T	F	F	
T	F	T	F	T	F	
T	F	F	F	T	F	
F	T	T	T	T	F	
F	T	F	T	F	F	
F	F	T	T	T	F	
F	F	F	T	T	F	

Check how where KB is true.

$\therefore KB \models R$

Algorithm:

```
def entails (KB, query):
    symbols = extract_symbols(KB + [query])
    return tt-check-all(KB, query, symbols, {})
```

```
def tt-check-all (KB, query, symbols, model):
```

```
    if not symbols:
```

```
        if all(eval_formula(s, model) for s in KB):
            return eval_formula(query, model)
```

```
    else:
```

```
        return true
```

```
    else:
```

```
        P = symbols[0]
```

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rest = symbols[1:]
 return tt-check-all(KB, query, rest,
 {**model, P: True}) and
 tt-check-all(KB, query, rest, {**model,
 P: False}))

i) KB:
 $Q \rightarrow P$
 $P \rightarrow \neg Q$

QVR

$\emptyset' + P$

					QVR	
			$Q \rightarrow P$		$P \rightarrow \neg Q$	$\emptyset' + P$
			T	F	T	X
i)	P	Q	T	T	F	T
		R	T	F	F	X
			T	T	T	X
			F	T	T	X
			F	F	F	X
			F	T	T	X
			F	F	T	✓
			F	F	F	X

KB is true in models:

($P=T, Q=F, R=T$) ?

($P=F, Q=F, R=T$)

ii) Does KB entail R?

$R = \text{True in both models}$

$\therefore KB \models R$

$$Q \rightarrow P$$

$$\bar{Q} + P$$

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iii) Does KB entail $R \rightarrow P$?

Model	R	P	$R \rightarrow P$
1	T	T	T
2	T	F	(F)
\therefore KB $\models (R \rightarrow P)$			

iv) Does KB entail $Q \rightarrow R$?

Model	Q	R	$Q \rightarrow R$
1	F	T	T
2	F	T	T
\therefore KB $\models (Q \rightarrow R)$			

Both true

\therefore KB $\models (Q \rightarrow R)$

✓
OK
15/10/15

Code:

```
from itertools import product
```

```

# Define propositional logic operations def
implies(a, b):
    return (not a) or b

# Knowledge Base sentences def
KB(P, Q, R):
    s1 = implies(Q, P) # Q → P  s2 =
    implies(P, not Q) # P → ¬Q
    s3 = Q or R # Q ∨ R
    return s1 and s2 and s3 # KB is true only if all hold

# All combinations of truth values for P, Q, R
values = list(product([False, True], repeat=3))

print("P\tQ\tR\tQ→P\tP→¬Q\tQ∨R\tKB") print("-"*50)

models = [] for P, Q,
R in values:
    s1 = implies(Q, P)
    s2 = implies(P, not Q)
    s3 = Q or R
    kb_val = s1 and s2 and s3
    print(f"\t{P}\t{Q}\t{R}\t{s1}\t{s2}\t{s3}\t{kb_val}")
    if kb_val:
        models.append((P, Q, R))

print("\n Models where KB is True:", models)

# Check entailments entails_R = all(R for P, Q, R in
models) entails_R_imp_P = all((not R) or P for P, Q, R in
models)
entails_Q_imp_R = all((not Q) or R for P, Q, R in models)

print("\nEntailments:") print("KB ⊨ R :",
entails_R) print("KB ⊨ R → P :",
entails_R_imp_P) print("KB ⊨ Q → R :",
entails_Q_imp_R)

```

Output:

P	Q	R	$Q \rightarrow P$	$P \rightarrow \neg Q$	$Q \vee R$	KB
<hr/>						
False	False	False	True	True	False	False
False	False	True	True	True	True	True
False	True	False	False	True	True	False
False	True	True	False	True	True	False
True	False	False	True	True	False	False
True	False	True	True	True	True	True
True	True	False	True	False	True	False
True	True	True	True	False	True	False

Models where KB is True: [(False, False, True), (True, False, True)]

Entailments:

$KB \vDash R : \text{True}$

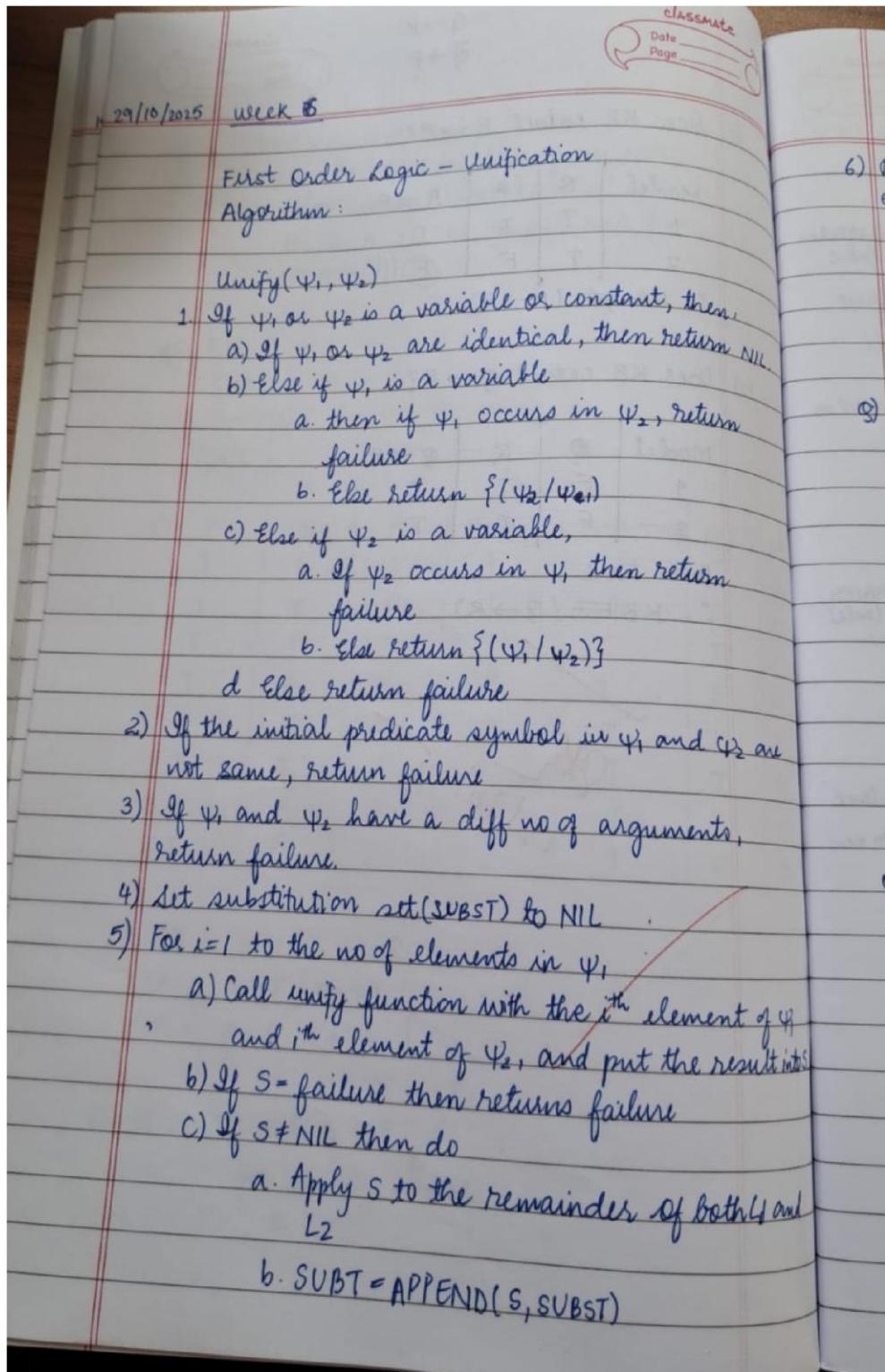
$KB \vDash R \rightarrow P : \text{False}$

$KB \vDash Q \rightarrow R : \text{True}$

Program 7

Implement unification in first order logic.

Algorithm:



Code:

```
def unify(x, y, substitutions=None):
if substitutions is None:
    substitutions = { }

        # If both are identical
if x == y:
    return substitutions

        # If x is a variable    if isinstance(x,
str) and x.islower():
            return
unify_var(x, y, substitutions)

        # If y is a variable    if isinstance(y,
str) and y.islower():
            return
unify_var(y, x, substitutions)

        # If both are compound expressions (like lists or tuples)
if isinstance(x, tuple) and isinstance(y, tuple):
    if x[0]
!= y[0] or len(x) != len(y):
        return None    for a,
b in zip(x[1:], y[1:]):
            substitutions = unify(a, b, substitutions)
if substitutions is None:
    return None
return substitutions

return None

def unify_var(var, x, substitutions):
if var in substitutions:
    return unify(substitutions[var], x, substitutions)
elif x in substitutions:
    return unify(var, substitutions[x], substitutions)
elif occurs_check(var, x, substitutions):
    return None
else:
    substitutions[var] = x
return substitutions
```

```

def occurs_check(var, x, substitutions):
    if var == x:      return True      elif
    isinstance(x, tuple):
        return any(occurs_check(var, arg, substitutions) for arg in x[1:])      elif isinstance(x, str)
    and x in substitutions:
        return occurs_check(var, substitutions[x], substitutions)
    return False

# Example expr1 = ("Eats",
" x", "Apple")
expr2 = ("Eats", "Riya", "y")

result = unify(expr1, expr2)
print("Unification:", result)

```

Output:

```
Unification: {'x': 'Riya', 'y': 'Apple'}
```

Program 8

Create a knowledge base consisting of first order logic statements and prove the given query using forward reasoning.

Algorithm:

Code:

```
def forward_chaining(KB, query):
inferred = set()    new_inferred =
True

    while new_inferred:
new_inferred = False      for
rule in KB:
        premises, conclusion = rule      if all(p in inferred or p in KB for p in
premises) and conclusion not in inferred:
            inferred.add(conclusion)
new_inferred = True      if
conclusion == query:
            return True
return False

# Example Knowledge Base
KB = [
    ("American(Robert)", "Weapon(x)", "Sells(Robert, x, A)", "Hostile(A)"),
    "Criminal(Robert)",
    ("Missile(x)", "Weapon(x)",),
    ("Owns(A, x)", "Missile(x)", "Sells(Robert, x, A)"),
    ("Enemy(A, America)", "Hostile(A)")
]

facts = {
    "American(Robert)",
    "Enemy(A, America)",
    "Owns(A, T1)",
    "Missile(T1)"
}
# Add base facts to KB
for fact in facts:
    KB.append(([ ], fact))
# Query query =
"Criminal(Robert)"
print("Is Robert a criminal?", forward_chaining(KB, query)) Output:
```

Is Robert a criminal? False

Program 9

Create a knowledge base consisting of first order logic statements and prove the given query using Resolution.

Algorithm:

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Create a knowledge base consisting of first order logic statements and prove the query using resolution -

Logical statement to CNF -

- 1) Eliminate \leftrightarrow replacing $\alpha \leftrightarrow \beta$ with $(\alpha \Rightarrow \beta) \wedge (\beta \Rightarrow \alpha)$
- 2) Eliminate \Rightarrow replacing $\alpha \Rightarrow \beta$ with $\neg \alpha \rightarrow \beta$
- 3) Move \neg inwards
 - $\neg(\forall x p) \equiv \exists x \neg p$
 - $\neg(\exists x p) \equiv \forall x \neg p$
 - $\neg(\alpha \vee \beta) \equiv \neg \alpha \wedge \neg \beta$
 - $\neg(\alpha \wedge \beta) \equiv \neg \alpha \vee \neg \beta$
 - $\neg \neg \alpha \equiv \alpha$
- 4) Standardize variables by renaming them.
- 5) Skolemize : each variable replaced by a Skolem constant. $\exists x \text{Rich}(x)$ becomes $\text{Rich}(\text{g1})$
- 6) Drop universal quantifiers
 - $\forall x \text{Person}(x)$ becomes $\text{Person}(x)$
- 7) Distribute \wedge over \vee
$$(\alpha \wedge \beta) \vee \gamma \equiv (\alpha \vee \gamma) \wedge (\beta \vee \gamma)$$

12/11/25

FOL-Resolution (KB, Query):

clauses \leftarrow convertToCNF (KB)negated_query \leftarrow negate (Query)clauses \leftarrow clauses \cup ConvertToCNF (negated_query)new $\leftarrow \{ \}$

repeat:

for each pair (c_i, c_j) in clauses:resolvents \leftarrow Resolve (c_i, c_j)if $\{ \} \in$ resolvents:

return True

new \leftarrow new \cup resolventsif new \subseteq clauses:

return False

clauses \leftarrow clauses \cup new

until contradiction found or no new clause

possible

Output:

Query: Likes (John, Peanuts)

Knowledge Base + Negated Query:

- 1) $[\neg \text{Food}(x), \text{Likes}(\text{John}, x)]$
 - 2) $[\text{Food}(\text{Apple})]$ 3) $[\text{Food}(\text{Vegetables})]$
 - 4) $[\text{Eats}(\text{Anil}, \text{Peanut})]$ 5) $[\text{Alive}(\text{Anil})]$
 - 6) $[\neg \text{Alive}(x), \neg \text{Eats}(x, y), \text{Food}(y)]$
 - 7) $[\neg \text{Eats}(\text{Anil}, y), \text{Eats}(\text{Harry}, y)]$
 - 8) $[\neg \text{Likes}(\text{John}, \text{Peanuts})]$
- $[\text{Eats}(\text{Anil}, \text{Peanuts})] \quad [\neg \text{Eats}(\text{Anil}, \text{Peanut})] \rightarrow []$
- contradiction found

Code:

import copy

```

# -----
# Predicate Structure
# -----
class Predicate:
    def __init__(self, name, args, negated=False):
        self.name = name      self.args = args if
        isinstance(args, tuple) else tuple(args)      self.negated =
        negated

    def __eq__(self, other):
        return (self.name == other.name and
                self.args == other.args and
                self.negated == other.negated)

    def __hash__(self):
        return hash((self.name, self.args, self.negated))

    def __repr__(self):
        neg = "~" if self.negated else ""
        args_str = ",".join(str(a) for a in self.args)
        return f"{neg}{self.name}({args_str})"

    def negate(self):
        return Predicate(self.name, self.args, not self.negated)

    def substitute(self, theta):
        """Apply substitution theta to this predicate"""
        new_args = tuple(substitute_term(arg, theta) for arg in self.args)
        return Predicate(self.name, new_args, self.negated)

    def substitute_term(term, theta):
        """Apply
        substitution to a term"""
        if isinstance(term, str) and
        term.islower(): # variable      if term in theta:
            return substitute_term(theta[term], theta)      return
            term    elif isinstance(term, tuple):
                return tuple(substitute_term(t, theta) for t in term)
        return term

# -----
# Unification Algorithm
# -----
def unify(x, y, theta=None):
    if theta is None:    theta =
    {}    if theta == "FAIL":
        return "FAIL"    elif x == y:    return theta
    elif isinstance(x, str) and x.islower(): # variable
        return unify_var(x, y, theta)    elif isinstance(y,

```

```

str) and y.islower()): # variable      return
unify_var(y, x, theta)    elif isinstance(x, tuple)
and isinstance(y, tuple):      if len(x) != len(y):
return "FAIL"      theta = unify(x[0], y[0], theta)
if theta == "FAIL":      return "FAIL"
return unify(x[1:], y[1:], theta)  else:
                           return "FAIL"

def unify_var(var, x, theta):
if var in theta:
    return unify(theta[var], x, theta)  elif
isinstance(x, str) and x.islower() and x in theta:
    return unify(var, theta[x], theta)
elif occurs_check(var, x, theta):
    return "FAIL"
else:
    new_theta = copy.deepcopy(theta)
new_theta[var] = x
    return new_theta

def occurs_check(var, x, theta):  if var == x:
return True  elif isinstance(x, str) and x.islower()
and x in theta:
    return occurs_check(var, theta[x], theta)
elif isinstance(x, tuple):
    return any(occurs_check(var, xi, theta) for xi in x)
return False

# -----
# Variable Standardization
# -----
var_counter = 0

def standardize_variables(clause):
    """Rename all variables in a clause to unique names"""
    global var_counter    mapping = {}    new_clause = []

        for pred in clause:
    new_args = []      for
    arg in pred.args:
        if isinstance(arg, str) and arg.islower(): # variable
        if arg not in mapping:
            mapping[arg] = f"{arg} {var_counter}"
            var_counter += 1
        new_args.append(mapping[arg])      else:

```

```

        new_args.append(arg)
new_clause.append(Predicate(pred.name, new_args, pred.negated))

    return new_clause

# -----
# Resolution Algorithm
# ----- def
resolve(ci, cj):
    """Resolve two clauses using FOL resolution"""
    ci = standardize_variables(ci)
    cj = standardize_variables(cj)

    resolvents = []

    for i, pi in enumerate(ci):
        for j, pj in enumerate(cj):
            # Check if predicates can be resolved (opposite signs, same name)
            if pi.negated != pj.negated and pi.name == pj.name:
                # Try to unify the arguments
                theta = unify(pi.args, pj.args)
                if
theta != "FAIL":
                    # Create resolvent by removing resolved predicates and applying substitution
                    new_clause = []

                    # Add literals from ci except pi
                    for k, pred in enumerate(ci):
                        if k != i:
                            new_clause.append(pred.substitute(theta))

                    # Add literals from cj except pj
                    for k, pred in enumerate(cj):
                        if k != j:
                            new_clause.append(pred.substitute(theta))

                    # Remove duplicates
                    new_clause = list(set(new_clause))
resolvents.append(new_clause)

    return resolvents

def fol_resolution(kb, query):
    """FOL resolution algorithm"""
    # Negate query and add to KB

```

```

clauses = [clause[:] for clause in kb] # deep copy
clauses.append([query.negate()])

print(f"\nKnowledge Base + Negated Query:")
for i, clause in enumerate(clauses):
    print(f" {i+1}. {clause}")
    print()

iteration = 0
while True:
    iteration += 1      n = len(clauses)      pairs = [(clauses[i],
clauses[j]) for i in range(n) for j in range(i + 1, n)]

    new_clauses = []
    for (ci, cj) in pairs:
        resolvents = resolve(ci, cj)

        for resolvent in resolvents:
            if len(resolvent) == 0:
                print(f"Iteration {iteration}: Derived empty clause from:")
                print(f" {ci}")          print(f" {cj}")          print(" → []")
                (Contradiction found!)")      return True

            # Check if this is a new clause
            if resolvent not
in clauses and resolvent not in new_clauses:
                new_clauses.append(resolvent)

        if not new_clauses:
            print(f"Iteration {iteration}: No new clauses derived. Query cannot be proved.")
            return False

    print(f"Iteration {iteration}: Generated {len(new_clauses)} new clause(s)")
    for clause in new_clauses:      clauses.append(clause)

# -----
# Example Usage
# -----
if __name__ == "__main__":
    # Define knowledge base
    kb = [
        # John likes all food: Food(x) => Likes(John, x)
        [Predicate("Food", ("x",), negated=True), Predicate("Likes", ("John", "x"))],

        # Food(Apple)
        [Predicate("Food", ("Apple",))],
```

```

# Food(Vegetables)
[Predicate("Food", ("Vegetables",))],

# Eats(Anil, Peanuts)
[Predicate("Eats", ("Anil", "Peanuts"))],

# Alive(Anil)
[Predicate("Alive", ("Anil",))],

# If alive and eats something, that thing is food: Alive(x) ∧ Eats(x,y) => Food(y)
[Predicate("Alive", ("x",), negated=True),
 Predicate("Eats", ("x", "y"), negated=True),
 Predicate("Food", ("y",))],

# Harry eats everything Anil eats: Eats(Anil,y) => Eats(Harry,y)
[Predicate("Eats", ("Anil", "y"), negated=True),
 Predicate("Eats", ("Harry", "y"))]
]

# Query: Does John like Peanuts?
query = Predicate("Likes", ("John", "Peanuts"))

print("=" * 60)
print("FIRST-ORDER LOGIC RESOLUTION THEOREM PROVER")
print("=" * 60) print(f"\nQuery: {query}")
print("-" * 60)

result = fol_resolution(kb, query)

print("\n" + "=" * 60)
if result:
    print("⚡Query is PROVED using resolution!")
else:
    print("✗Query CANNOT be proved.")
print("=" * 60)

```

Output:

```
=====
FIRST-ORDER LOGIC RESOLUTION THEOREM PROVER
=====

Query: Likes(John,Peanuts)
-----

Knowledge Base + Negated Query:
1. [~Food(x), Likes(John,x)]
2. [Food(Apple)]
3. [Food(Vegetables)]
4. [Eats(Anil,Peanuts)]
5. [Alive(Anil)]
6. [~Alive(x), ~Eats(x,y), Food(y)]
7. [~Eats(Anil,y), Eats(Harry,y)]
8. [~Likes(John,Peanuts)]

Iteration 1: Generated 8 new clause(s)
Iteration 2: Generated 16 new clause(s)
Iteration 3: Derived empty clause from:
[Eats(Anil,Peanuts)]
[~Eats(Anil,Peanuts)]
→ [] (Contradiction found!)

=====
 Query is PROVED using resolution!
=====
```

Program 10 Implement Alpha-Beta Pruning.

Algorithm:

12/11/25 Week #8

Alpha beta pruning

function ALPHA-BETA-SEARCH (state) returns an action

$v \leftarrow \text{MAX-VALUE}(\text{state}, -\infty, +\infty)$

return the action in ACTIONS(state) with value v

function MAX-VALUE (state, α , β) returns a utility value

if TERMINAL-TEST (state) then return UTILITY (state)

$v \leftarrow -\infty$

for each a in ACTIONS(state) do

$v \leftarrow \text{MAX}(v, \text{MIN-VALUE}(\text{RESULT}(s, a), \alpha, \beta))$

if $v \geq \beta$ then return v

$\alpha \leftarrow \text{MAX}(\alpha, v)$

return v

function MIN-VALUE (state, α , β) returns a utility value

if TERMINAL-TEST (state) then return UTILITY (state)

$v \leftarrow \infty$

for each a in ACTIONS(state) do :

$v \leftarrow \text{MIN}(v, \text{MAX-VALUE}(\text{RESULT}(s, a), \alpha, \beta))$

if $v \leq \alpha$ then return v

$\beta \leftarrow \text{MIN}(\beta, v)$

return v

MIN MAX algorithm

Output:

Leaf Node Values: [3, 5, 6, 9, 1, 2, 0, -1]

Optimal value at Root Node: 5

Best path (Node Indices): [0, 0, 0, 1]

Pruned Nodes: [(1, 'Right'), (1, 'Right')]

~~8, 9, 11~~

```

import math

# Alpha-Beta Pruning Algorithm def alpha_beta(depth, node_index, maximizing_player,
values, alpha, beta, max_depth, path, pruned):
    # Base case: leaf node
    if depth == max_depth:
        return values[node_index], [node_index]

    if maximizing_player:
        best = -math.inf
        best_path = []
        for i in range(2): # two children per node           val, child_path = alpha_beta(depth +
                           node_index * 2 + i, False, values, alpha, beta, max_depth, path, pruned)      if val >
                           best:
            best = val           best_path =
            [node_index] + child_path
            alpha = max(alpha, best)
        if beta <= alpha:
            pruned.append((node_index, "Right" if i == 0 else "Left"))
            break
        return best, best_path
    else:
        best = math.inf
        best_path = []   for
        i in range(2):
            val, child_path = alpha_beta(depth + 1, node_index * 2 + i, True, values, alpha, beta,
                                           max_depth, path, pruned)   if val < best:
                best = val           best_path =
                [node_index] + child_path       beta = min(beta,
                best)   if beta <= alpha:
                    pruned.append((node_index, "Right" if i == 0 else "Left"))
                    break
        return best, best_path

# Example usage if
__name__ == "__main__":
    # Example game tree (leaf node values)
    values = [3, 5, 6, 9, 1, 2, 0, -1]

    print("Leaf Node Values:", values)
    path = []
    pruned = []

    max_depth = 3   result, best_path = alpha_beta(0, 0, True, values, -math.inf, math.inf,
                                                   max_depth, path, pruned)

```

```
print("\nOptimal Value at Root Node:", result)
print("Best Path (Node Indices):", best_path)
print("Pruned Nodes:", pruned) Output:

Leaf Node Values: [3, 5, 6, 9, 1, 2, 0, -1]

Optimal Value at Root Node: 5
Best Path (Node Indices): [0, 0, 0, 1]
Pruned Nodes: [(1, 'Right'), (1, 'Right')]
```