

Perfect Numbers

Greek mathematicians took a special interest in numbers that are equal to the sum of their **proper divisors**, which is simply any divisor less than the number itself. They called such numbers **perfect numbers**. For example, 6 is a perfect number because it is the sum of 1, 2, and 3, which are integers less than 6 that divide evenly into 6. Similarly, 28 is a perfect number because it is sum of 1, 2, 4, 7, and 14.

Write a predicate function `isPerfect` that takes an unsigned integer `n` and returns true if `n` is perfect, and false otherwise. Test your implementation by writing a main program in C++ that uses the `isPerfect` function to check for perfect numbers in the range 1 to 9999 by testing each number in turn. When a perfect number is found, your program displays it on stdout and also displays its divisors. The first two lines of the output should be `6 = 1 + 2 + 3` and `28 = 1 + 2 + 4 + 7 + 14`. Your program should find two other perfect numbers in the range as well.

You can name your source/header files anything you want as far as they have proper extensions: `.cc` for source files and `.h` for header files. Guard the statements in your header file using the following format. (This is necessary because you don't want the statements in a header file are processed more than once.)

```
#ifndef CONSTANT-VALUE // which is not defined any place else
#define CONSTANT-VALUE // same const value as for ifndef directive
// put all statements for your header file here
#endif
```

Include all system header files (that you need in your program) in your header files. For example, to gain access to the `iostream` library, which defines a set of simple I/O operations, insert the line `#include <iostream>` in your header files, and at the top of each source file, insert corresponding header files by the following statement: `#include "header-file.h"`. Define the constant value 9999 as an unsigned integer and put its definition in the program header file. Also put the prototype of the predicate function `isPerfect` in the header file as well.

Each perfect number `n` should be displayed as $n = d_1 + d_2 + \dots + d_m$, where d_1, d_2, \dots, d_m are the divisors of `n` with $d_1 = 1$. Generate such sequence as a C++ string by a `divisors` function. To use the strings in your program, you need to insert the line `#include <string>` in your header file, and to convert each divisor (an integer) to a string, you can use the conversion function `to_string` from the C++ library. You also need to include the prototype of `divisors` function in your header file.

To compile your source file and link its object file with the system library routines, you need to create a `makefile`. Insert the statements in this file in the following format, where the first line defines a macro that includes several options we use for the C++ compiler, and in the rest each entry consists of a line containing a colon (the dependency line), and one/more command lines beginning with a tab. To the left of the colon on the

dependency line is a target (an executable file); to the right of the colon are the target's prerequisites. For target, you can choose any valid name, and the advantages of using a makefile will be discussed in class. After creating this file, simply execute the UNIX make command without any arguments.

```
OPT = -std=c++11 -c -g -Wall -Wextra
```

```
program-executable-file.exe: program-object-file.o  
    g++ -o program-executable-file.exe program-object-file.o
```

```
program-object-file.o: program-source-file.cc program-header-file.h  
    g++ ${OPT} program-source-file.cc
```

```
execute:  
    program-executable-file.exe | tee program-output-file
```

```
clean:  
    /bin/rm -f *.o *.exe
```

For a final test of your program, execute it as: `make execute`. When the execution is successful, you will see the four perfect numbers on your computer screen and the output will also be stored in the output file `program-output-file`. You can find the correct output in file `prog2.out`, which is in directory: `~cs689/progs/16s/p2`. After you are done, you don't need the object and executable files any more. To delete them, execute: `make clean`.

Submit your source and header files to your TA by executing: `mail_prog program-source-file.cc program-header-file.h`.