# Machine Leaning COMP4702/COMP7703

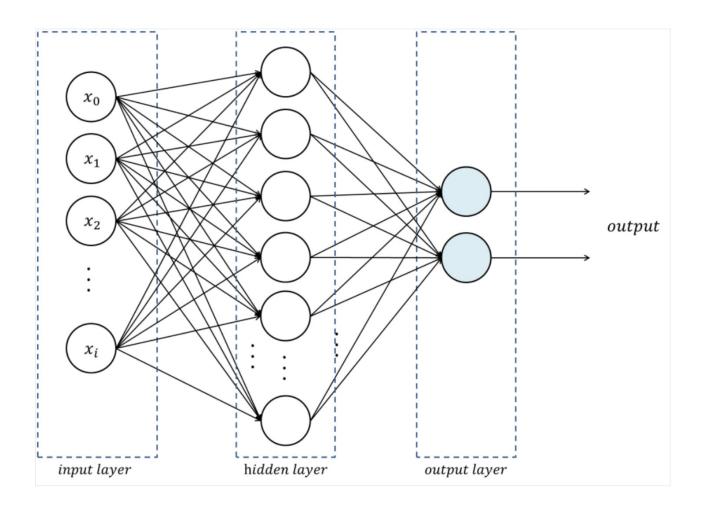
Prac 7

Amelia Qiu

https://github.com/Amelia-Tong/MachineLearning\_COMP4702/blob/main

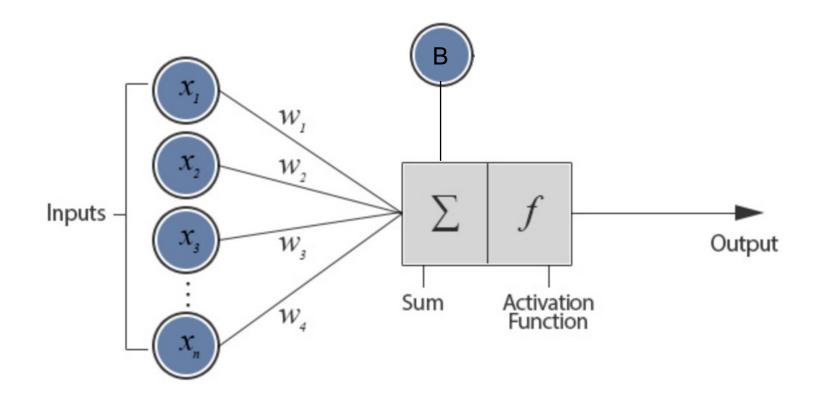


## Model Architecture (Multi-later Perceptron)





### Model Architecture (Perceptron/Neuron)

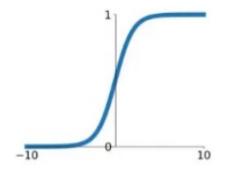


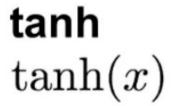


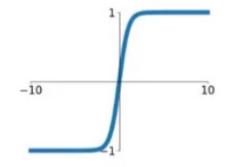
### **Activation Functions**

### **Sigmoid**

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

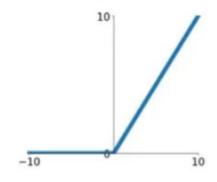




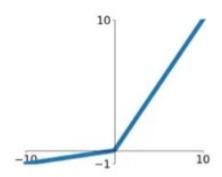


### ReLU

$$\max(0, x)$$



# Leaky ReLU max(0.1x, x)





### Learning Mechanism

MLPs performs a forward pass and a backward pass through the neural net:

- the forward pass propagates information from the input neurons to the output neurons to compute the outputs of all neurons.
- the backward pass propagates information from the output neurons to the input neurons to compute derivatives and adjust the weights.
  - Loss functions: to compare the predictions and the true values
  - Optimizers: to minimize the loss



### **Loss Function**

- Mean Squared Error:

$$ext{MSE} = rac{1}{n} \sum_{i=1}^n (Y_i - \hat{Y}_i)^2$$

Cross-Entropy/Binary Cross-Entropy:

$$egin{aligned} ext{CE} &= -\sum_{i=1}^n Y_i \cdot \log(\hat{Y}_i) \ ext{BCE} &= -rac{1}{n} \sum_{i=1}^n [Y_i \cdot \log(\hat{Y}_i) + (1-Y_i) \cdot \log(1-\hat{Y}_i)] \end{aligned}$$

Dice Loss:

$$ext{Dice Loss} = 1 - rac{2 imes\sum_{i=1}^n Y_i\hat{Y}_i}{\sum_{i=1}^n Y_i + \sum_{i=1}^n \hat{Y}_i}$$



### **Optimizer**

- **Gradient Descent**: The simplest optimizer that updates weights in the network by taking a step proportional to the negative of the gradient of the loss function.

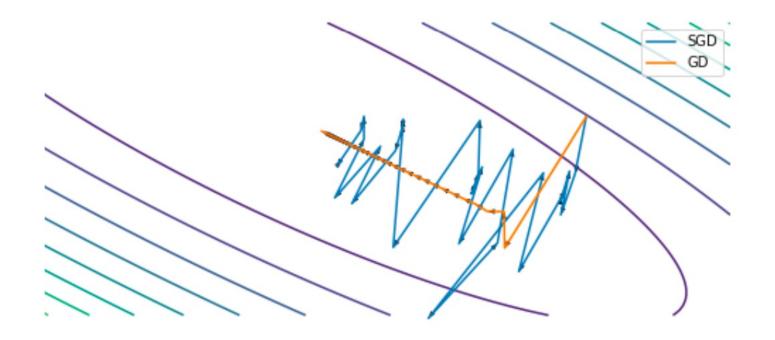
$$\mathbf{w}_{t+1} = \mathbf{w}_t - \eta_t \, 
abla \, f(\mathbf{w}_t)$$
 $f(\mathbf{w}) = rac{1}{n} \sum_i f_i(\mathbf{w})$ 

- **Stochastic Gradient Descent (SGD)**: A variant of gradient descent, it updates weights using only a single sample or a batch of samples which makes the computation much faster.

$$\mathbf{w}_{t+1} = \mathbf{w}_t - \eta_t \tilde{\mathbf{g}}_t, \ ilde{\mathbf{g}}_t = rac{1}{|\mathcal{S}|} \sum_{i \in \mathcal{S}} 
abla f_i(\mathbf{w})$$



### Optimizer



- Although SGD can jump around in the solution space, it is often computationally attractive when the dataset is very large.



### **Optimizer**

- **Gradient Descent**: The simplest optimizer that updates weights in the network by taking a step proportional to the negative of the gradient of the loss function.
- **Stochastic Gradient Descent (SGD)**: A variant of gradient descent, it updates weights using only a single sample or a batch of samples which makes the computation much faster.
- Adam (Adaptive Moment Estimation): Combines momentum (like RMSProp) and adaptive learning rate (like AdaGrad), which often leads to faster and more stable convergence.