

# Efficient Photorealistic Rendering via Ray-Tracing on GPUs



Candidate Number: 1023011

University of Oxford

Computer Science 4th Year Project Report

Supervised by: Joe Pitt-Francis

Trinity 2020

# Abstract

One of the ultimate goals of the field of computer graphics is to synthesize images that are indistinguishable from photographs. This task, often referred to as photorealistic rendering, is known for being extremely costly, due to the need of a physically-correct simulation of the transport of light in the scene. This project explores methods to accelerate rendering by utilizing the massively parallel computing architectures of GPUs, and creates a renderer whose performance tops some of the best renderers in the academia.

This project focuses on the widely-used simulation algorithm known as path-tracing. The project studies how to maximize the performance of path-tracing on GPUs, and implements state-of-the-art algorithms for the construction and traversal of the data structures used by this algorithm. Besides the standard path-tracing algorithm, the project also implements a newly emerged variant, where reinforcement learning is used to guide the the selection of light paths. The resulting renderer can robustly handle a variety of real-world materials, complex scene geometry, and difficult lighting situations. Moreover, comprehensive benchmarking indicates that the efficiency of this GPU renderer significantly exceeds other CPU implementations, and is even noticeably faster compared to one of the most academically renowned GPU renderer.

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# 1 Introduction

## 1.1 Motivation

May it be glorious space battles with lasers blasting around, or a mountain-high gorilla wrestling a even bigger lizard, modern rendering technologies present our craziest fantasies to our eyes as if they are happening right in front of us. The contemporary film and television industry is highly dependent on this ability of rendering photorealistic images, and alongside the pursuit of wilder stories and imaginations, the scenes to be rendered are becoming increasingly complex and arbitrary.

Despite its importance, the task of photorealistic rendering has a computational cost that is matched by few others. As an example, recent Disney title films could require hundreds of CPU hours just to synthesize a single frame[3]. This immense cost is explained by the fact that there are complex interactions between light rays and scene geometry, and the rendering algorithm must comprehensively and accurately simulate these interactions in order to obtain a realistic image.

This project studies two orthogonal approaches that both boost the efficiency of rendering. Firstly, this project utilizes GPUs, whose massively parallel architectures allow a large amount of pixels to be processed at the same time. Secondly, from an algorithmic perspective, the project explores how reinforcement learning can be used to guide the algorithm to focus on the “important” parts of the scene. The project shows that both methods are indeed effective ways of improving rendering efficiency.

## 1.2 Related Work

The study of computer graphics began almost as soon as computers with screens are manufactured. In 1980, Whitted[17] proposed the algorithm known as *ray-tracing*, which is the algorithmic foundation of almost all photorealistic rendering algorithms used today. However, the version of ray-tracing described by Whitted was not based on a physically plausible model of light, and consequently the images generated was not yet photorealistic.

The age of photorealism began in 1986 with the visionary work of Kaijiya[8]. This paper introduced an integral equation known as *the rendering equation*, which models the power carried by light rays in a physically correct manner. Programs that produce images by computing solutions to this equation are called physically based renderers, and this method have since become the focus of decades of rendering research. In addition, Kaijiya’s paper also described a variant of the ray-tracing algorithm known as *path tracing*, which solves the rendering equation using the technique of Monte-Carlo integration. This algorithm is still the core of most of the photorealistic renderers developed and used today, including the renderer implemented in this project.

Path-tracing is a powerful algorithm, but it is too costly<sup>1</sup> to be used for real-time rendering applications such as video games. As a result, real-time applications take a fundamentally different approach to rendering known as rasterization. Modern rasterization-based rendering pipelines can be very-fast: they can render tens or even hundreds of frames per second. However, despite the fact that a range of algorithms[6][15][7] exist that aims to make rasterization based algorithms as physically-correct as possible, the images produced by these renderers are still easily recognizable as computer generated. Thus, when the need for image quality dominates that for rendering speed, path-tracing is still the better choice. Notice that however, modern GPUs are designed to optimize for rasterization-based pipelines<sup>2</sup> and not for ray-tracing algorithms.

In a ray tracing algorithm, one of the most costly operations is ray-scene intersection. Intuitively, this is the task of finding the first intersection point between a light ray and the geometries in the scene. A naive linear search across all geometries is of course unacceptably slow, and a range of accelerating data structures have been created. This project employs the data structure of Bounding Volume Hierarchies (BVH), which recursively divides the scene into a tree of axis-aligned bounding boxes. Due to their recursive nature, the construction and traversal of these structures are difficult tasks on GPUs. For this reason, this project studied and implemented a series of GPU BVH techniques published by NVIDIA[9][10][1].

Ever since the introduction of path-tracing, a variety of algorithms that builds on top of patch-tracing have emerged. The most famous ones include bi-direction path-tracing[16], Metropolis light transport[16][11], energy redistribution path-tracing[4], and gradient-domain path-tracing [12]. One particularly interesting variant, which

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<sup>1</sup>until perhaps, very recently. See NVIDIA RTX.

<sup>2</sup>this is beginning to change with NVIDIA RTX

uses reinforcement learning to guide the generation of light rays[5], is studied and implemented in this project.

One renderer of particular value to the graphics community is the **pbrt** renderer. Not only is this renderer open-source, it is also accompanied by an entire book[14] which happens to be the most authoritative textbook of physically based rendering. Moreover, because of its popularity, there is a large collection of beautiful scenes defined using **pbrt**'s input file format. For these reasons, this project decided to support **pbrt**'s scene definition files, which allows this project to be benchmarked and compared against **pbrt**.

Most of the ray-tracing renderers used today, including **pbrt**, runs on the CPU. However, there is a GPU ray-tracing system known as OptiX[13], which is becoming increasingly popular. Developed by the GPU manufacturer NVIDIA, OptiX is heavily optimized, and provides a friendly ray-tracing library for developers. One famous renderer which uses OptiX as a backbone<sup>3</sup> is the **Mitsuba** renderer. The GPU rendering routines of this project is implemented from scratch, and its performance will be compared against **Mitsuba** (and therefore OptiX).

## 1.3 Project Outline

This project focuses on the GPU parallelization of ray-tracing algorithms for the efficient rendering of photorealistic images. A fully-featured GPU renderer is created, which supports a wide range of geometries, materials, and light sources. At the heart of the renderer are efficient implementations of two algorithms: the original path-tracing algorithm, and a variant of path-tracing guided by reinforcement learning.

In order to efficiently implement path-tracing, this project implemented state-of-the-art methods of performing ray-scene intersection detection. These includes algorithms for constructing BVH trees in parallel, optimizing the structure of constructed BVHs, and recursion-free methods of tree traversal. The project also makes numerous optimizations that reduces control flow divergences and memory access latencies, so that the resulting implementation maximally utilize the parallel architecture of GPUs.

This project made the observation that in certain lighting scenarios, the original path-tracing algorithm struggled to converge to a noiseless solution. To alleviate this problem, the project implements a variant of path-tracing, where reinforcement

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<sup>3</sup>There is also an upcoming 4th version of **pbrt**, which also supports GPU via OptiX. However, the beta version is still unstable at the time this thesis is written

learning is used to guide the selection of light rays. The project investigates how the architecture of the GPU interacts with various aspects of the reinforcement learning routine, and implements a version that allows tens of thousands of GPU threads to efficiently cooperate during learning.

The renderer created by this project is named *Cavalry*<sup>4</sup>. It is created mainly using the C++ programming language on the CPU side, and the CUDA language for GPU computing. With a total of over 7 thousand lines, the complete source code of the software can be found at <https://github.com/AmesingFlank/Cavalry>, along with some additional information and screenshots.

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<sup>4</sup>The name is inspired by a character in a video game called Overwatch. The character goes by the name “Tracer”, and refers to herself as the “Cavalry”.

## 2 Physically Based Rendering

In order to generate photorealistic images, renderers must find accurate solutions to the *rendering equation*. This chapter explains the meaning and intuition behind the equation, and describes how it can be solved by the path-tracing algorithm.

### 2.1 The Rendering Equation

The rendering equation describes the “strength” of light at each point in space and in each direction. To formalize the notion of strength, this section begins by introducing a few concepts from the study of radiometry.

#### 2.1.1 Radiometry

In radiometry, there is a hierarchy of quantities that measures the strength of light in different contexts. The first quantity is *radiant flux*, which measures the total energy that travels through a region of space per unit time in the form of electromagnetic radiation. Radiant flux is often denoted by  $\Phi$ , and its unit of measure is Watts( $W$ ).

In almost all regions in any scene, the radiant flux is not uniformly distributed, and thus one important quantity is the density of radiant flux with respect to area. This quantity is named *irradiance*, which is denoted by  $E$ , and measured in power per unit area ( $W \cdot m^{-2}$ ). Intuitively, irradiance measures the amount of light received by a single point in space. For this reason, for a region of space  $S$ , integrating the irradiance of each point in  $S$  gives the total flux through  $S$ :

$$\Phi(S) = \int_S E(p) dp \quad (2.1)$$

For any point  $p$ , the irradiance  $E(p)$  is not uniform across all directions, and thus it is also important to consider the density of irradiance in each direction  $\omega$ . This quantity,  $L(p, \omega)$ , is called *radiance*, and its unit of measure for radiance is power per unit area per unit solid angle ( $W \cdot m^{-2} \cdot sr^{-1}$ ). Radiance is an especially important quantity, because it is a measure of the strength of a single ray of light, identified by



its direction  $\omega$  and a point  $p$  which it passes through. Consequently, radiance is the physical quantity that ray-tracing algorithms constantly operates in.

In rendering, radiance often appears in the form  $L_o(p, \omega)$  or  $L_i(p, \omega)$ , which mean radiance going out from the point  $p$  or entering into it, respectively. More precisely,  $L_o(p, \omega)$  represents the radiance that travels from  $p$  and outwards in the direction  $\omega$ , and  $L_i(p, \omega)$  represents the incoming radiance that travels towards to  $p$  in the direction  $-\omega$ . The convention  $L_i(p, \omega)$  might appear slightly counter-intuitive, since  $\omega$  points in the opposite direction as the propagation of energy. However, the convenience of this notation will become apparent when the ray-tracing algorithm is formulated.

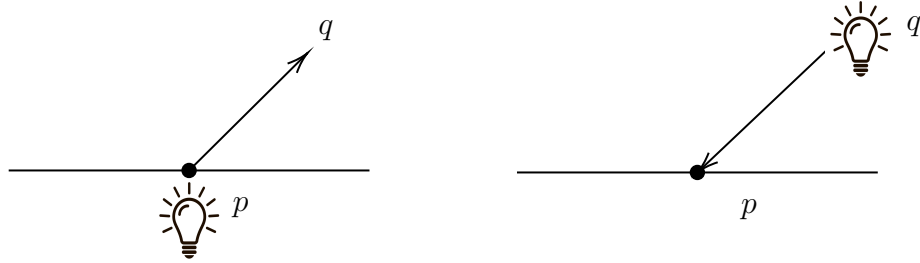


Figure 2.1: Example: consider two points  $p$ ,  $q$ , and  $\omega = \frac{q-p}{|q-p|}$ . On the left, the radiance sent from  $p$  to  $q$  is  $L_o(p, \omega)$ . On the right, the radiance received by  $p$  from  $q$  is  $L_i(p, \omega)$ .

Similar to equation 2.1, which expresses flux as an integral of irradiance, it's also possible to obtain the incoming irradiance  $E(p)$  by an integral across the incoming radiance from each direction. More precisely, the following relationship holds:

$$E(p) = \int_{\Omega} L_i(p, \omega_i) \cos \theta_i d\omega_i \quad (2.2)$$

Here, the support  $\Omega$  is often a sphere or hemisphere of possible incoming direction, and the angle  $\theta_i$  represents the angle between  $\omega_i$  and the surface normal. The cosine term accounts for the fact that for incoming rays that are not perfectly perpendicular to the surface, the differential area illuminated by the ray is multiplied by a factor  $\frac{1}{\cos \theta_i}$ , and thus the contribution per unit area should be multiplied by  $\cos \theta_i$ .

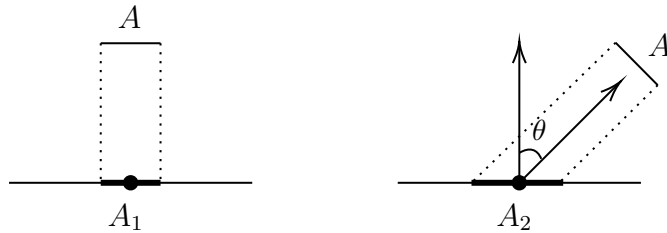


Figure 2.2: Example: on the right, the differential area  $A_2$  illuminated by the ray is larger, because the ray is not perpendicular to the plane.

### 2.1.2 The BRDF

In order to accurately model the incoming and outgoing radiances at each point, it is essential to take into account the fact that surfaces can reflect incoming light. That is, for any direction  $\omega_i$ , the incoming radiance  $L_i(p, \omega_i)$  can contribute to the outgoing radiance  $L_o(p, \omega_o)$  of another direction  $\omega_o$ . For each surface point, this relationship is captured by the bi-directional reflectance distribution function (BRDF), written as  $f_r(p, \omega_o, \omega_i)$ . Formally, the BRDF is defined as

$$f_r(p, \omega_o, \omega_i) = \frac{dL_o(p, \omega_o)}{dE(p, \omega_i)} \quad (2.3)$$

where  $dE(p, \omega_i)$  represents the differential incoming irradiance in the direction  $\omega_i$ .

Using equation 2.2, it can be derived that

$$dE(p, \omega_i) = L_i(p, \omega_i) \cos \theta_i d\omega_i \quad (2.4)$$

which allows equation 2.3 to be re-written as

$$f_r(p, \omega_o, \omega_i) = \frac{dL_o(p, \omega_o)}{L_i(p, \omega_i) \cos \theta_i d\omega_i} \quad (2.5)$$

From this, it's straightforward to show that

$$L_o(p, \omega_o) = \int_{\Omega} f_r(p, \omega_o, \omega_i) L_i(p, \omega_i) \cos \theta_i d\omega_i + C \quad (2.6)$$

for some  $C$ .

Equation 2.6 shows that, given the incident radiances and the BRDF, the portion of outgoing radiances caused by reflections can be computed. As a result, the BRDF of a surface completely decides how the surface reflects light, which is a crucial factor of its appearances when viewed by a camera. Different materials in the real world have drastically different BRDFs, and it's vital for a physically based renderer to accurately implement these functions, if photorealistic images are to be rendered. A family of BRDFs known for their physical accuracy are the Microfacet BRDFs, which are well implemented by this project. Unfortunately, due to the complexity of these models, details of these BRDFs could not be described here.

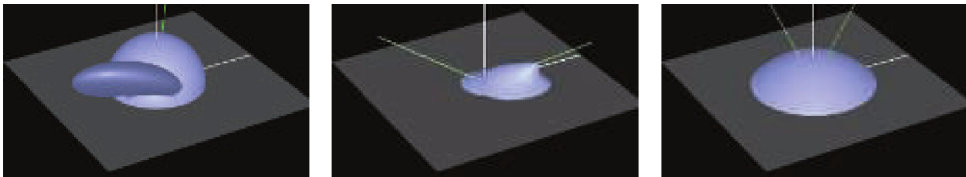


Figure 2.3: Shapes of example BRDFs. Image credit[2]

In order to fully model  $L_o(p, \omega_o)$ , it remains to describe the term  $C$  in equation 2.6. Surfaces in the real world send outgoing radiances for two reasons only: they might emit light actively, and they reflect incoming light. Equation 2.6 already includes the reflected radiances, and thus it only remains to include actively emitted light. Writing  $L_e(p, \omega_o)$  for the emitted radiance from  $p$  towards the direction  $\omega_o$ , the following equation completely describes  $L_o$ :

$$L_o(p, \omega_o) = L_e(p, \omega_o) + \int_{\Omega} f_r(p, \omega_o, \omega_i) L_i(p, \omega_i) \cos \theta_i d\omega_i \quad (2.7)$$

This is indeed the famous rendering equation, originally proposed by Kaijiya[8]. Finding solutions to this equation is the ultimate goal of rendering, because the job of any renderer is to compute the amount of radiance received by a hypothetical camera placed in the scene. In other words, for each point  $p$  that is visible from the camera, the rendering algorithm must compute  $L_o(p, \omega_o)$ , where  $\omega_o$  points from  $p$  towards the camera.

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