

Amey Thakur

SE-Comps B-50

Practice Test AM-IV

Class: SE B - 50

Date: 08/05/2020

Time: 10 AM to 11AM

Q.01 Find all basic, feasible and degenerate solutions of the equations

$$2x_1 + 6x_2 + 2x_3 + x_4 = 3, 6x_1 + 4x_2 + 4x_3 + 6x_4 = 2$$

Q.18 A certain injection administered to 12 patients resulted in the following changes of blood pressure: 5, 2, 8, -1, 3, 0, 6, -2, 1, 5, 0, 4. Can it be concluded that the injection will be in general accompanied by an increase in Blood pressure ?

Q.1.Solⁿ:

$$2x_1 + 6x_2 + 2x_3 + x_4 = 3$$

$$6x_1 + 4x_2 + 4x_3 + 6x_4 = 2$$

Since there are four variables and 2 constraints
there are $4C_2 = 6$ basic solution

No. of basic sol ⁿ .	No. of basic Variable	Basic Variables	Eq ⁿ & the values of basic variables	Is sol ⁿ . feasible	degenerate
1	$x_3 = 0$ $x_4 = 0$	x_1, x_2	$2x_1 + 6x_2 = 3$ $6x_1 + 4x_2 = 2$ $x_1 = 0$ $x_2 = 1/2$	Yes	Yes
2	$x_2 = 0$ $x_4 = 0$	x_1, x_3	$2x_1 + 2x_3 = 3$ $6x_1 + 4x_3 = 2$ $x_1 = -2$ $x_3 = 7/2$	No	No
3	$x_1 = 0$ $x_4 = 0$	x_2, x_3	$6x_2 + 2x_3 = 3$ $4x_2 + 4x_3 = 2$ $x_2 = 1/2$ $x_3 = 0$	Yes	Yes
4	$x_1 = 0$ $x_3 = 0$	x_2, x_4	$6x_2 + x_4 = 3$ $4x_2 + 6x_4 = 2$ $x_2 = 1/2$ $x_4 = 0$	Yes	Yes

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5	$x_2 = 0$ $x_3 = 0$	x_1, x_4	$2x_1 + 4x_4 = 3$ $6x_1 + 4x_4 = 2$ $x_1 = 8/3$ $x_2 = -7/3$	No	No
6	$x_1 = 0$ $x_2 = 0$	x_3, x_4	$2x_3 + x_4 = 3$ $4x_3 + 6x_4 = 2$ $x_3 = 2$ $x_4 = -1$	No	No

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Q. 18

Solⁿ

$N = 12$ ($< 30, 20$ it is a small sample)

Change in blood pressure
(d_i)

d_i^2

5

25

2

4

8

64

-1

1

3

9

0

0

6

36

-2

4

1

1

5

25

0

0

4

16

Total

31

185

Step 1:

Null Hypothesis (H_0): $\mu_1 = 0$

(i.e. the injection is not accompanied by an increase in blood pressure)

Alternative Hypothesis: $\mu_1 < 0$

(i.e. the injection is accompanied by an increase in blood pressure)

(One test failed)

Step 2:

L.O.S = 5% (Two failed test)

L.O.S = 10% (One failed test)

$$\begin{aligned}\text{Degree of freedom} &= n - 1 \\ &= 12 - 1 \\ &= 11\end{aligned}$$

Critical Value (t_{α}) = 1.796

Step 3:

Since sample is small: $\bar{d} = \frac{\sum d_i}{n} = \frac{31}{12} = 2.5833$

$$S = \sqrt{\frac{\sum d_i^2}{n} - \left(\frac{\sum d_i}{n}\right)^2}$$

$$= \sqrt{\left(\frac{185}{12}\right) - \left(\frac{31}{12}\right)^2}$$

$$= 2.9569$$

$$S.E. = \frac{S}{\sqrt{n-1}} = \frac{2.9569}{\sqrt{11}} = 0.8915$$

Step 4 :

$$\text{Test statistic } t_{cal} = \frac{\bar{d}_i - \mu}{S.E.}$$

$$= \frac{2.5833 - 0}{0.8915}$$

$$= 2.8976$$

Step 5 :

Decision $t_{cal} > t_{\alpha}$

Since $|t_{cal}| > t_{\alpha}$ H_0 is rejected

* The injection will be in general accompanied by an increase in blood pressure