

Q 4.

t	y(t)
1	4
2	6
3	5
4	7
5	10

By least square method

(i) Equation of best line (in the least square)

t	y	t ²	t.y	
1	4	1	4	$\therefore \sum t = 15$
2	6	4	12	$\therefore \sum y = 32$
3	5	9	15	$\therefore \sum t^2 = 55$
4	7	16	28	$\therefore \sum ty = 109$
5	10	25	50	

~~→ By the method of least square~~

$$\bar{T} = \frac{\sum t}{n} = \frac{15}{5} = 3$$

$$\bar{y} = \frac{\sum y}{n} = \frac{32}{5} = 6.4$$

$$\Sigma y = a \Sigma t + b \Sigma t \Rightarrow 32 = a(5) + b(15) \rightarrow \textcircled{1}$$

$$\Sigma ty = a \Sigma t + b \Sigma t^2 \Rightarrow 109 = a(15) + b(55) \rightarrow \textcircled{2}$$

$$\therefore 96 = 15a + 45b \rightarrow \textcircled{3} \text{ (multiplying eq}^n \textcircled{1} \text{ by 3)}$$

$$\therefore 109 = 15a + 55b \rightarrow \textcircled{4} \text{ (multiplying eq}^n \textcircled{2} \text{ by 1)}$$

$$\therefore 10b = 13$$

$$\boxed{b = 1.3}$$

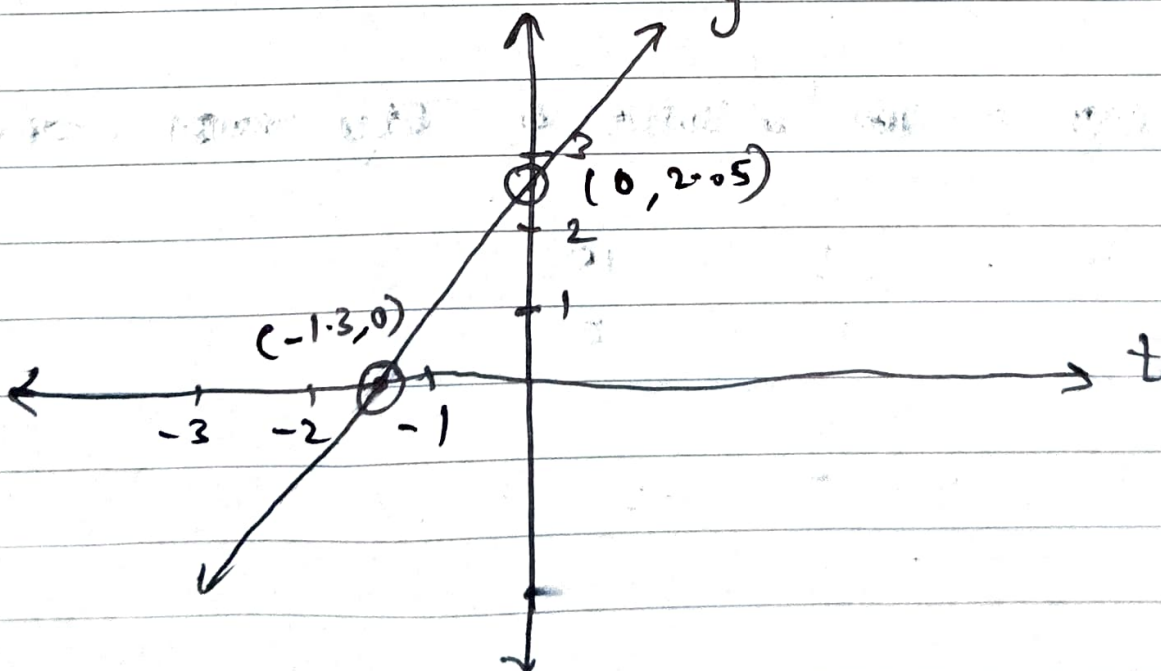
$$96 = 15a + 45(1.3)$$

$$\boxed{a = 2.5}$$

$$y = 1.3t + 2.5$$

Plot graph from eqⁿs.

$$y = 1.3t + 2.5$$



2. Least square error

$$= (3.8 - 5)^2 + (5.1 - 6)^2 + (6.4 - 5)^2 \\ + (7.7 - 7)^2 + (9 - 10)^2$$

$$= 4.1$$

x	y
1	3.8
2	5.1
2	6.4
4	7.7
5	9