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Steel Buildings
BMEEHSA-A1

Checking the Buckling Stability of a Frame Using the Reduction Method and the General Method

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1. Initial data:

Span of the main frame:	$l := 14.4 \text{ m}$
Corner height of main frame:	$h := 5.2 \text{ m}$
Slope of the roof:	$\alpha_{inc} := 7 \text{ deg}$
Cross section of columns:	HEA400
Cross-section of beams:	IPE500
Number of purlins on one beam:	$n_p := 4$
Number of wall-beams on one column:	$n_w := 5$
Design load acting on the beams:	$p_d := 13 \frac{\text{kN}}{\text{m}} \quad \gamma_G := 1.35$
Characteristic load acting on the beams:	$p_k := \frac{p_d}{\gamma_G} = 9.63 \frac{\text{kN}}{\text{m}}$
Wind pressure:	$w_{pd} := 2.5 \frac{\text{kN}}{\text{m}}$
Wind suction:	$w_{sd} := 1 \frac{\text{kN}}{\text{m}}$
Characteristic wind loads on the columns:	$\gamma_Q := 1.5$
	$w_{pk} := \frac{w_{pd}}{\gamma_Q} = 1.667 \frac{\text{kN}}{\text{m}}$
	$w_{sk} := \frac{w_{sd}}{\gamma_Q} = 0.667 \frac{\text{kN}}{\text{m}}$

2. Data of used materials

2.1 Beam section data, section IPE 500:

Height of cross-section:	$h_b := 500 \text{ mm}$
Width of a flange :	$b_b := 200 \text{ mm}$
Thickness of web:	$t_{w.b} := 10.2 \text{ mm}$
Thickness of flange:	$t_{f.b} := 16 \text{ mm}$
Radius of rounding of web:	$r_b := 21 \text{ mm}$
Cross-sectional area:	$A_b := 11600 \text{ mm}^2$
Inertia around the strong axis:	$I_{y.b} := 48017 \text{ cm}^4$
Inertia around the weak axis:	$I_{z.b} := 2141 \text{ cm}^4$
Torsional inertia:	$I_{t.b} := 89.6 \text{ cm}^4$

Warping modulus:

$$I_{w,b} := I_{z,b} \cdot \frac{(h_b - t_{f,b})^2}{4} = (1.254 \cdot 10^6) \text{ cm}^6$$

Plastic cross-sectional modulus around the strong axis:

$$W_{pl,y,b} := 2200 \text{ cm}^3$$

$$\text{Radius of gyration around the strong axis: } i_{y,b} := \sqrt{\frac{I_{y,b}}{A_b}} = 20.346 \text{ cm}$$

$$\text{Radius of gyration around the weak axis: } i_{z,b} := \sqrt{\frac{I_{z,b}}{A_b}} = 4.296 \text{ cm}$$

$$\frac{h_b}{b_b} = 2.5 > 1.2, \quad t_{f,b} = 16 \text{ mm} < 40 \text{ mm}$$

Buckling curve for FB for buckling around the strong axis: curve "a"

Buckling curve for FB for buckling around the weak axis: curve "b"

$$\frac{h_b}{b_b} = 2.5 > 2 \text{ Buckling curve for LT buckling: curve "b"}$$

2.1 Column section data, section HEA400:

Height of cross-section:	$h_c := 390 \text{ mm}$
Width of a flange: :	$b_c := 300 \text{ mm}$
Thickness of web:	$t_{w.c} := 11 \text{ mm}$
Thickness of flange:	$t_{f.c} := 19 \text{ mm}$
Radius of rounding of web:	$r_c := 27 \text{ mm}$
Cross-sectional area:	$A_c := 15900 \text{ mm}^2$
Inertia around the strong axis:	$I_{y.c} := 45070 \text{ cm}^4$
Inertia around the weak axis:	$I_{z.c} := 8564 \text{ cm}^4$
Torsional inertia:	$I_{t.c} := 189 \text{ cm}^4$

Warping modulus:
$$I_{w.c} := I_{z.c} \cdot \frac{(h_c - t_{f.c})^2}{4} = (2.947 \cdot 10^6) \text{ cm}^6$$

Plastic cross-sectional modulus around the strong axis:

$$W_{pl.y.c} := 2562 \text{ cm}^3$$

Radius of gyration around the strong axis:
$$i_{y.c} := \sqrt{\frac{I_{y.c}}{A_c}} = 16.836 \text{ cm}$$

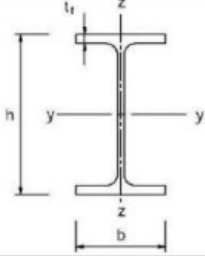
Radius of gyration around the weak axis:
$$i_{z.c} := \sqrt{\frac{I_{z.c}}{A_c}} = 7.339 \text{ cm}$$

$$\frac{h_c}{b_c} = 1.3 > 1.2, \quad t_{f.c} = 19 \text{ mm} < 40 \text{ mm}$$

Buckling curve for FB for buckling around the strong axis: curve "b"

Buckling curve for FB for buckling around the weak axis: curve "c"

$$\frac{h_c}{b_c} = 1.3 < 2 \text{ Buckling curve for LT buckling: curve "a"}$$

Cross section		Limits	Buckling about axis	Buckling curve	
				S 235 S 275 S 355 S 420	S 460
Rolled sections		$h/b > 1,2$	$t_f \leq 40 \text{ mm}$	y-y z-z	a a ₀
			$40 \text{ mm} < t_f \leq 100$	y-y z-z	b c
		$h/b \leq 1,2$	$t_f \leq 100 \text{ mm}$	y-y z-z	b c
			$t_f > 100 \text{ mm}$	y-y z-z	d e

Buckling curve	α Imperfection factor
a ₀	0,13
a	0,21
b	0,34
c	0,49
d	0,76

Table 10.3. Imperfection factors for buckling curves

Cross-section type	restriction	Buckling curve
Hot-rolled I-section	$h/b \leq 2$	a
	$h/b > 2$	b
Welded I-section	$h/b \leq 2$	c
	$h/b > 2$	d
Other		d

2.3 Data of the used steel:

Modulus of elasticity: $E := 210 \text{ GPa}$

Steel grade: S275 $f_y := 275 \text{ MPa}$

Slenderness limit: $\lambda_1 := \pi \cdot \sqrt{\frac{E}{f_y}} = 86.815$

$$\varepsilon := \sqrt{\frac{235}{f_y}} \text{ MPa} = 0.924$$

Partial factor for the resistance: $\gamma_{m1} := 1$

Poisson ratio of : $\nu_a := 0.3$

Shear modulus of steel: $G := \frac{E}{2 \cdot (1 + \nu_a)} = 80.769 \text{ GPa}$

3. Classifications of the cross-sections:

3.1. Beam section, section IPE 500:

Flanges classification:

$$c_{f.b} := \frac{b_b - t_{w.b} - 2 \cdot r_b}{2} = 73.9 \text{ mm}$$

$$\frac{c_{f.b}}{t_{f.b}} = 4.619 < 9 \cdot \varepsilon = 8.32$$

The flange is of class 1

Web classification:

$$c_{w.b} := h_b - 2 \cdot t_{f.b} = 468 \text{ mm}$$

$$\frac{c_{w.b}}{t_{w.b}} = 45.882 < 72 \cdot \varepsilon = 66.558$$

The web is of class 1

From this cross-section is of class 1

3.2. Column section, section HEA 400:

Flanges classification:

$$c_{f.c} := \frac{b_c - t_{w.c} - 2 \cdot r_c}{2} = 117.5 \text{ mm}$$

$$\frac{c_{f.c}}{t_{f.c}} = 6.184 < 9 \cdot \varepsilon = 8.32$$

The flange is of class 1

Web classification:

$$c_{w.c} := h_c - 2 \cdot t_{f.c} = 352 \text{ mm}$$

$$\frac{c_{w.c}}{t_{w.c}} = 32 < 72 \cdot \varepsilon = 66.558$$

The web is of class 1

From this cross-section is of class 1

4. Column stability checks using the reduction factor method:

4.1. Flexural buckling check:

$$c := \min\left(\frac{I_{y,c}}{I_{y,b}} \cdot l, 10\right) = 2.599$$

$$\alpha := \min\left(4 \cdot \frac{I_{y,c}}{l^2 \cdot A_c}, 0.2\right) = 5.468 \cdot 10^{-4}$$

Buckling length factor (pinned base connection):

$$\nu_y := \sqrt{4 + 1.4 \cdot (c + 6 \cdot \alpha) + 0.02 \cdot (c + 6 \cdot \alpha)^2} = 2.789$$

$$\nu'_z := 1.0 \quad (\text{for hinged})$$

$$\nu_z := \frac{\nu'_z}{n_w - 1} = 0.25$$

$$\text{Column slenderness around the strong axis: } \lambda_y := \frac{\nu_y \cdot h}{i_{y,c}} = 86.143$$

$$\lambda_y = 86.143 < \lambda_1 = 86.815$$

yielding of the cross-section

$$\text{Column slenderness around the weak axis: } \lambda_z := \frac{\nu_z \cdot h}{i_{z,c}} = 17.713$$

$$\lambda_z = 17.713 < \lambda_1 = 86.815$$

yielding of the cross-section

critical normal force around the strong axis:

$$N_{cr,y} := \pi^2 \cdot E \cdot \frac{A_c}{\lambda_y^2} = (4.441 \cdot 10^3) \text{ kN}$$

critical normal force around the weak axis:

$$N_{cr,z} := \pi^2 \cdot E \cdot \frac{A_c}{\lambda_z^2} = (1.05 \cdot 10^5) \text{ kN}$$

$$\text{Cross-sectional resistance: } N_{pl,Rk} := A_c \cdot f_y = (4.373 \cdot 10^3) \text{ kN}$$

$$\text{Relative slenderness around the strong axis: } \lambda'_y := \frac{N_{pl,Rk}}{N_{cr,y}} = 0.985$$

$$\text{Relative slenderness around the weak axis: } \lambda'_z := \frac{N_{pl,Rk}}{N_{cr,z}} = 0.042$$

$$\text{Imperfection factor around the strong axis (curve a): } \alpha_y := 0.21$$

$$\phi_y := 0.5 \cdot (1 + \alpha_y \cdot (\lambda'_y - 0.2)) + \lambda'^2_y = 1.552$$

Imperfection factor around the weak axis (curve b): $\alpha_z := 0.34$

$$\phi_z := 0.5 \cdot (1 + \alpha_z \cdot (\lambda'_z - 0.2)) + \lambda'^2_z = 0.475$$

Reduction factor for buckling around the strong axis:

$$\chi_y := \min \left(\frac{1}{\phi_y + \sqrt{\phi_y^2 - \lambda'^2_y}}, 1 \right) = 0.363$$

Reduction factor for buckling around the weak axis:

$$\chi_z := \min \left(\frac{1}{\phi_z + \sqrt{\phi_z^2 - \lambda'^2_z}}, 1 \right) = 1$$

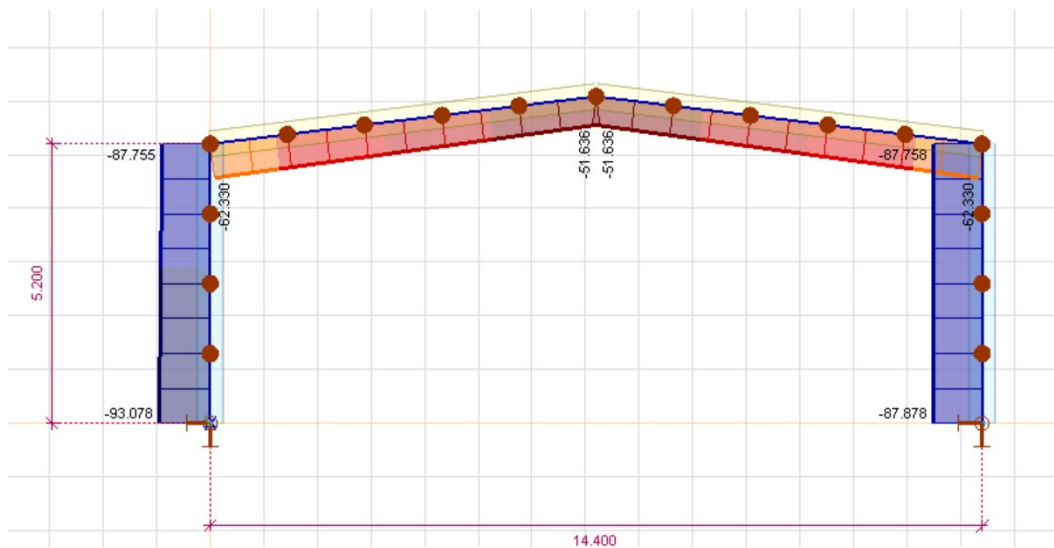
$$\chi := \min(\chi_y, \chi_z) = 0.363$$

Design buckling resistance:

$$N_{b.Rd} := \chi \cdot \frac{N_{pl.Rk}}{\gamma_{m1}} = 1589.28 \text{ kN}$$


$$N_{Ed} := 87.878 \text{ kN (from Axis Vm)}$$

$$\text{Utilisation ratio: } \eta := \frac{N_{Ed}}{N_{b.Rd}} = 0.055 \quad \text{Adequate!}$$



4.2 Lateral torsional buckling check:

$$M_{ed} := 194.607 \text{ kN} \cdot \text{m}$$

Statical system	ψ	k	C_1	C_2	C_3
	0	1,0	1,879	—	0,939
		0,7	2,092		1,473
		0,5	2,150		2,150

$$\psi := 0 \quad C_1 := 1.879 \quad C_2 := 0 \quad C_3 := 0.939 \quad L := h$$

$$k := 1 \quad k_w := 1 \quad z_j := 0 \text{ mm} \quad (\text{double symmetric cross section})$$

$$M_{cr} := C_1 \cdot \frac{\pi^2 \cdot E \cdot I_{z.c}}{(k \cdot L)^2} \cdot \left(\sqrt{\left(\frac{k}{k_w} \right)^2 \cdot \frac{I_{w.c}}{I_{z.c}} + \frac{(k \cdot L)^2 \cdot G \cdot I_{t.c}}{\pi^2 \cdot E \cdot I_{z.c}}} + (0 - C_3 \cdot z_j)^2 - (0 - C_3 \cdot z_j) \right)$$

$$M_{cr} = (2.962 \cdot 10^3) \text{ kN} \cdot \text{m}$$

$$\text{Non-dimensional slenderness:} \quad \lambda'_{LT} := \sqrt{W_{pl.y.c} \cdot \frac{f_y}{M_{cr}}} = 0.488$$

$$M_{pl.y.Rk} := W_{pl.y.c} \cdot f_y = 704.55 \text{ kN} \cdot \text{m}$$

$$\text{reduction factor of curve A:} \quad \chi_{LT} := 0.927852$$

$$\text{Design resistance for LT buckling:} \quad M_{b.Rd} := \chi_{LT} \cdot \frac{M_{pl.y.Rk}}{\gamma_{m1}} = 653.718 \text{ kN} \cdot \text{m}$$

$$\text{Utilization ratio:} \quad \eta := \frac{M_{ed}}{M_{b.Rd}} = 0.298 \quad \text{Adequate!}$$

4.3. FB and LT buckling interaction check:

$$N_{Rk} := N_{pl.Rk} = (4.373 \cdot 10^3) \text{ kN}$$

$$M_{y.Ed} := M_{ed} = 194.607 \text{ kN} \cdot \text{m}$$

$$M_{y.Rk} := f_y \cdot W_{pl.y.c} = 704.55 \text{ kN} \cdot \text{m}$$

$$C_{my} := 0.9$$

$$\psi := 0$$

$$C_{mLT} := 0.6$$

$$k_{yy} := C_{my} \cdot \min \left(1 + (\lambda'_y - 0.2) \cdot \frac{N_{Ed}}{\chi_y \cdot \frac{N_{Rk}}{\gamma_{m1}}}, \left(1 + 0.8 \cdot \frac{N_{Ed}}{\chi_y \cdot \frac{N_{Rk}}{\gamma_{m1}}} \right) \right) = 0.939$$

$$\lambda'_z = 0.042 \quad \square < \square \quad 0.4$$

$$k_{zy} := \max \left(0.6 + \lambda'_z, 1 - \frac{0.1 \cdot \lambda'_y}{(C_{my} - 0.25)} \cdot \frac{N_{Ed}}{\chi_y \cdot \frac{N_{Rk}}{\gamma_{m1}}} \right) = 0.992$$

$$\frac{N_{Ed}}{\chi_y \cdot \frac{N_{Rk}}{\gamma_{m1}}} + k_{yy} \cdot \frac{M_{y.Ed}}{\chi_{LT} \cdot \frac{M_{y.Rk}}{\gamma_{m1}}} = 0.335$$

$$\frac{N_{Ed}}{\chi_z \cdot \frac{N_{Rk}}{\gamma_{m1}}} + k_{zy} \cdot \frac{M_{y.Ed}}{\chi_{LT} \cdot \frac{M_{y.Rk}}{\gamma_{m1}}} = 0.315$$

The member is adequate for flexural buckling and for LTB

5.. Beam stability checks using the reduction factor method:

$$l_{beam} := \frac{l}{\cos(\alpha_{inc})} = 14.508 \text{ m}$$

$$\frac{l_{beam}}{6} = 2.418 \text{ m}$$

$$\nu_y := 1$$

$$\nu'_z := 1.0$$

$$\nu_z := \frac{\nu'_z}{n_p + 2} = 0.167$$

Column slenderness around the strong axis:

$$\lambda_y < \lambda_1$$

$$\lambda_y := \nu_y \cdot \frac{l_{beam}}{i_{y,b}} = 71.309$$

Column slenderness around the weak axis:

$$\lambda_z < \lambda_1$$

$$\lambda_z := \nu_z \cdot \frac{l_{beam}}{i_{z,b}} = 56.284$$

$$N_{cr,y} := \pi^2 \cdot E \cdot \frac{A_b}{\lambda_y^2} = (4.728 \cdot 10^3) \text{ kN}$$

$$N_{cr,z} := \pi^2 \cdot E \cdot \frac{A_b}{\lambda_z^2} = (7.59 \cdot 10^3) \text{ kN}$$

$$N_{pl.Rk} := A_b \cdot f_y = (3.19 \cdot 10^3) \text{ kN}$$

$$\text{Relative slenderness around the strong axis: } \lambda'_y := \frac{N_{pl.Rk}}{N_{cr,y}} = 0.675$$

$$\text{Relative slenderness around the weak axis: } \lambda'_z := \frac{N_{pl.Rk}}{N_{cr,z}} = 0.42$$

$$\text{Imperfection factor around the strong axis (curve a): } \alpha_y := 0.21$$

$$\phi_y := 0.5 \cdot (1 + \alpha_y \cdot (\lambda'_y - 0.2)) + \lambda'^2_y = 1.005$$

$$\text{Imperfection factor around the weak axis (curve b): } \alpha_z := 0.34$$

$$\phi_z := 0.5 \cdot (1 + \alpha_z \cdot (\lambda'_z - 0.2)) + \lambda'^2_z = 0.714$$

Reduction factor for buckling around the strong axis:

$$\chi_y := \min\left(\frac{1}{\phi_y + \sqrt{\phi_y^2 - \lambda'^2_y}}, 1\right) = 0.571$$

Reduction factor for buckling around the weak axis:

$$\chi_z := \min \left(\frac{1}{\phi_z + \sqrt{\phi_z^2 - \lambda_z'^2}}, 1 \right) = 0.774$$

$$\chi := \min(\chi_y, \chi_z) = 0.571$$

Design buckling resistance:

$$N_{b.Rd} := \chi \cdot \frac{N_{pl.Rk}}{\gamma_{m1}} = 1822.898 \text{ kN}$$

$$N_{Ed} := 87.878 \text{ kN (from Axis Vm)}$$

$$\text{Utilisation ratio: } \eta := \frac{N_{Ed}}{N_{b.Rd}} = 0.048 \quad \text{Adequate!}$$

Suggestions for efficient design (100% utilisation):

1. Decreasing the size of the elements. The steel grade can be decreased to utilize 100%.
2. Installing knee bars, especially for the wall beams.
3. Changing the inclination of the roof. A more inclined roof may result in a buckling mode for the beams with a buckling length equal to half of the length of the roof..
4. Changing the number of the lateral supports .

5.2 Lateral torsional buckling check

$$M_{cr} := C_1 \cdot \frac{\pi^2 \cdot E \cdot I_{z.b}}{(k \cdot L)^2} \cdot \left(\sqrt{\left(\frac{k}{k_w} \right)^2 \cdot \frac{I_{w.b}}{I_{z.b}} + \frac{(k \cdot L)^2 \cdot G \cdot I_{t.b}}{\pi^2 \cdot E \cdot I_{z.b}}} + (0 - C_3 \cdot z_j)^2 - (0 - C_3 \cdot z_j) \right)$$

$$L := 2 \cdot \frac{l_{beam}}{(n_p + 2)} = 4.836 \text{ m}$$

$$k = 1$$

$$k_w := 1$$

$$M_{ed.2} := -105.848 \text{ kN} \cdot \text{m}$$

$$M_{ed} := 194.607 \text{ kN} \cdot \text{m}$$

$$\psi := \frac{M_{ed.2}}{M_{ed}} = -0.544$$

$$C_1 := 2.806$$

$$C_2 = 0$$

$$C_3 := 0.864$$

$$M_{cr} = 988.011 \text{ kN} \cdot \text{m}$$

Non-dimensional slenderness:

$$\lambda'_{LT} := \sqrt{W_{pl.y.b} \cdot \frac{f_y}{M_{cr}}} = 0.783$$

$$M_{pl.y.Rk} := W_{pl.y.b} \cdot f_y = 605 \text{ kN} \cdot \text{m}$$

reduction factor of curve B:

$$\chi_{LT} := 0.735$$

Design resistance for LT buckling:

$$M_{b.Rd} := \chi_{LT} \cdot \frac{M_{pl.y.Rk}}{\gamma_{m1}} = 444.675 \text{ kN} \cdot \text{m}$$

Utilization ratio:

$$\eta := \frac{M_{ed}}{M_{b.Rd}} = 0.438 \quad \text{Adequate!}$$

Project

Analysis by Amgalantuul Purevsuren

AxisVM X6 R2b · Registered to Amgalantuul Purevsuren

Model 5.axs

Report

Educational Version

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Model: **Model 5.axs**

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Materials



	Name	Type	National design code	Material code ▼	Model	E_x [N/mm ²]	E_y [N/mm ²]	ν	α_T [1/°C]	ρ [kg/m ³]
1	S 275	Steel	Eurocode-H	10025-2	Linear	210000	210000	0.30	1.2E-5	7850

	Name	Material color	Contour color	Texture	P_1	P_2	P_3
1	S 275				Steel f_y [N/mm ²] = 275.00	f_y [N/mm ²] = 480.00	f_y [N/mm ²] = 255.00

	Name	P_4	P_5	P_6	P_7	P_8	P_9	P_{10}	P_{11}	P_{12}	P_{13}	P_{14}
1	S 275	f_u [N/mm ²] = 410.00										

Name: Material name; **Type:** Type of material; **Model:** Material model; **E_x :** Young's modulus of elasticity in local x direction; **E_y :** Young's modulus of elasticity in local y direction; **ν :** Poisson's ratio; **α_T :** Thermal expansion coefficient; **ρ :** Density; **Contour color:** Material outline color; **$P_1, P_2, P_3, P_4, P_5, P_6, P_7, P_8, P_9, P_{10}, P_{11}, P_{12}, P_{13}, P_{14}$:** Design parameter;

Cross-sections

	Name	Drawing	Process	Shape	h [mm]	b [mm]	tw [mm]	tf [mm]	r_1 [mm]	r_2 [mm]	r_3 [mm]
1	IPE 500		Rolled	I	500.0	200.0	10.2	16.0	21.0	0	0
2	HE 400 A		Rolled	I	390.0	300.0	11.0	19.0	27.0	0	0

	Name	A_x [mm ²]	A_y [mm ²]	A_z [mm ²]	I_x [mm ⁴]	I_y [mm ⁴]	I_z [mm ⁴]	I_{yz} [mm ⁴]	I_1 [mm ⁴]	I_2 [mm ⁴]	α [°]
1	IPE 500	11553.92	5887.51	4968.85	903296.5	4.8208E+8	2.1417E+7	0	4.8208E+8	2.1417E+7	0
2	HE 400 A	15900.68	10298.69	4201.46	1953265.0	4.5077E+8	8.5639E+7	0	4.5077E+8	8.5639E+7	0

	Name	I_ω [mm ⁶]	$W_{1,el,t}$ [mm ³]	$W_{1,el,b}$ [mm ³]	$W_{2,el,t}$ [mm ³]	$W_{2,el,b}$ [mm ³]	$W_{1,pl}$ [mm ³]	$W_{2,pl}$ [mm ³]	i_y [mm]	i_z [mm]
1	IPE 500	1.2346E+12	1928302.0	1928302.0	214172.4	214172.4	2194516.0	335901.4	204.3	43.1
2	HE 400 A	2.8902E+12	2311663.0	2311663.0	570927.7	570927.7	2562282.0	872908.3	168.4	73.4

	Name	H_y [mm]	H_z [mm]	y_G [mm]	z_G [mm]	y_s [mm]	z_s [mm]	β_y [mm]	β_z [mm]	β_w []	S.p.
1	IPE 500	200.0	500.0	100.0	250.0	0	0	0	0	0	9
2	HE 400 A	300.0	390.0	150.0	195.0	0	0	0	0	0	9

Name: Cross-section name; **Process:** Manufacturing process; **h :** Cross-section height; **b :** Cross-section width; **tw :** Web thickness; **tf :** Flange thickness; **r_1, r_2, r_3 :** Rounding radius;

A_x : Cross-section area; **A_y, A_z :** Shear area; **I_x :** Torsional inertia; **I_y, I_z :** Flexural inertia; **I_{yz} :** Centrifugal inertia; **I_1, I_2 :** Principal flexural inertia; **α :** Principal directions; **I_ω :** Warping constant;

$W_{1,el,t}, W_{1,el,b}, W_{2,el,t}, W_{2,el,b}$: Elastic section modulus; **$W_{1,pl}, W_{2,pl}$:** Plastic section modulus; **i_y, i_z :** Radius of inertia; **H_y :** Dimension in local y direction; **H_z :** Dimension in local z direction;

y_G : y coordinate of the center of gravity; **z_G :** z coordinate of the center of gravity; **y_s :** y coordinate of the shear (torsion) center relative to the center of gravity;

z_s : z coordinate of the shear (torsion) center relative to the center of gravity; **$\beta_y, \beta_z, \beta_w$:** Wagner's coefficient; **S.p.:** Stress calculation points;

Project

Analysis by Amgalantuul Purevsuren

Model: **Model 5.axes**

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Spring characteristics

	Name	Type	Degree of freedom	Model	K	K_V	P_I
1	Soft - Translational	N-N	Translational	Linear	1E+0 kN/m	1E+0 kN/m	—
2	Rigid - Translational	N-N	Translational	Linear	1E+10 kN/m	1E+10 kN/m	—
3	Soft - Rotational	N-N	Rotational	Linear	1E+0 kNm/rad	1E+0 kNm/rad	—
4	Rigid - Rotational	N-N	Rotational	Linear	1E+10 kNm/rad	1E+10 kNm/rad	—
5	Complete - inverse	Warping transmission	Warping	Linear	—	—	WF = -1
6	Complete - direct	Warping transmission	Warping	Linear	—	—	WF = 1
7	Rigid	Warping transmission	Warping	Linear	—	—	WF = 0

Name: Name of the spring characteristics; **Model:** Material model; **K:** Initial stiffness; **K_V :** Vibration stiffness; **P_I :** Parameter;

References

	Name	Type	X_1 [m]	Y_1 [m]	Z_1 [m]	X_2 [m]	Y_2 [m]	Z_2 [m]	X_3 [m]	Y_3 [m]	Z_3 [m]
1	R1	8	7.00								

Name: Reference name; **Type:** Type of %;

Nodes

	X [m]	Y [m]	Z [m]	e_x	e_y	e_z	θ_x	θ_y	θ_z
1	0	0	0	f	Con	f	Con	f	Con
2	14.400	0	0	f	Con	f	Con	f	Con
3	0	0	5.200	f	f	f	f	f	f
4	14.400	0	5.200	f	f	f	f	f	f
5	7.200	0	6.084	f	f	f	f	f	f
6	0	0	1.300	f	f	f	f	f	f
7	0	0	2.600	f	f	f	f	f	f
8	0	0	3.900	f	f	f	f	f	f
9	14.400	0	3.900	f	Con	f	Con	f	Con
10	14.400	0	2.600	f	f	f	f	f	f
11	14.400	0	1.300	f	f	f	f	f	f
12	1.440	0	5.377	f	Con	f	Con	f	Con
13	2.880	0	5.554	f	Con	f	Con	f	Con
14	4.320	0	5.730	f	Con	f	Con	f	Con
15	5.760	0	5.907	f	Con	f	Con	f	Con
16	8.640	0	5.907	f	Con	f	Con	f	Con
17	10.080	0	5.730	f	f	f	f	f	f
18	11.520	0	5.554	f	f	f	f	f	f
19	12.960	0	5.377	f	Con	f	Con	f	Con

e_x : Nodal DOF (translation constraint X); **e_y :** Nodal DOF (translation constraint Y); **e_z :** Nodal DOF (translation constraint Z); **θ_x :** Nodal DOF (rotation constraint about X-Axis);

θ_y : Nodal DOF (rotation constraint about Y-Axis); **θ_z :** Nodal DOF (rotation constraint about Z-Axis);

Project

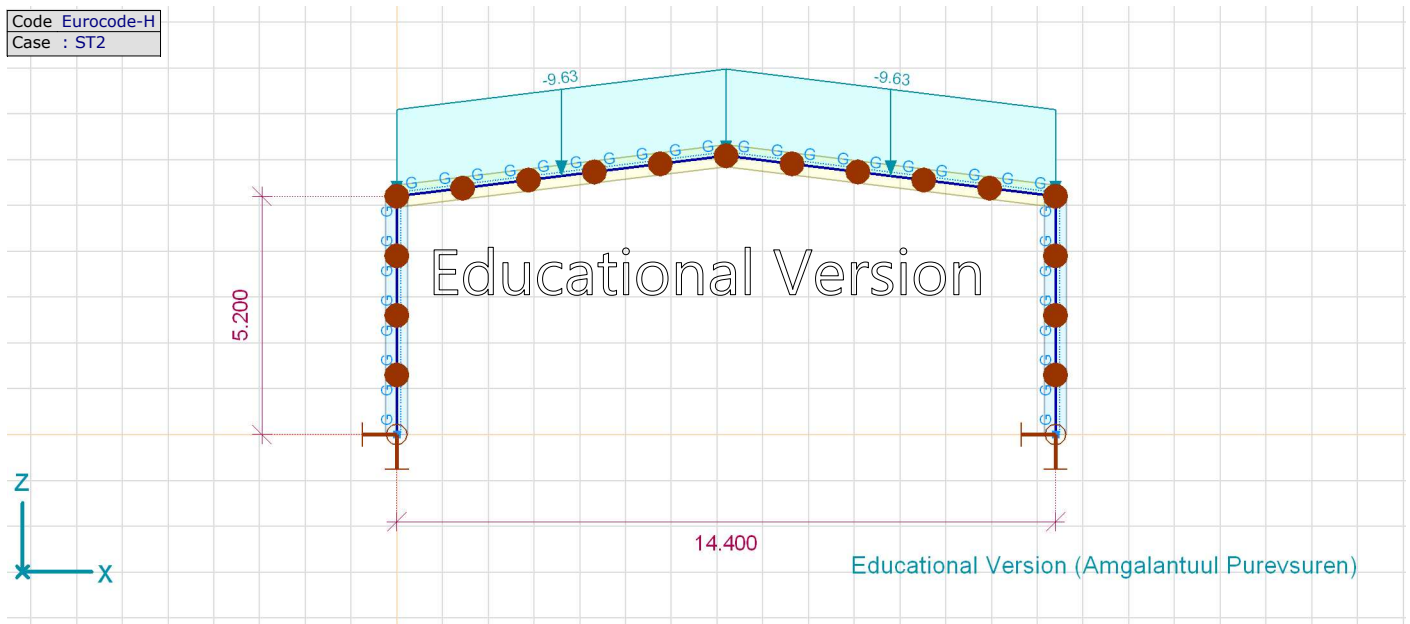
Analysis by Amgalantuul Purevsuren

Model: **Model 5.axs**

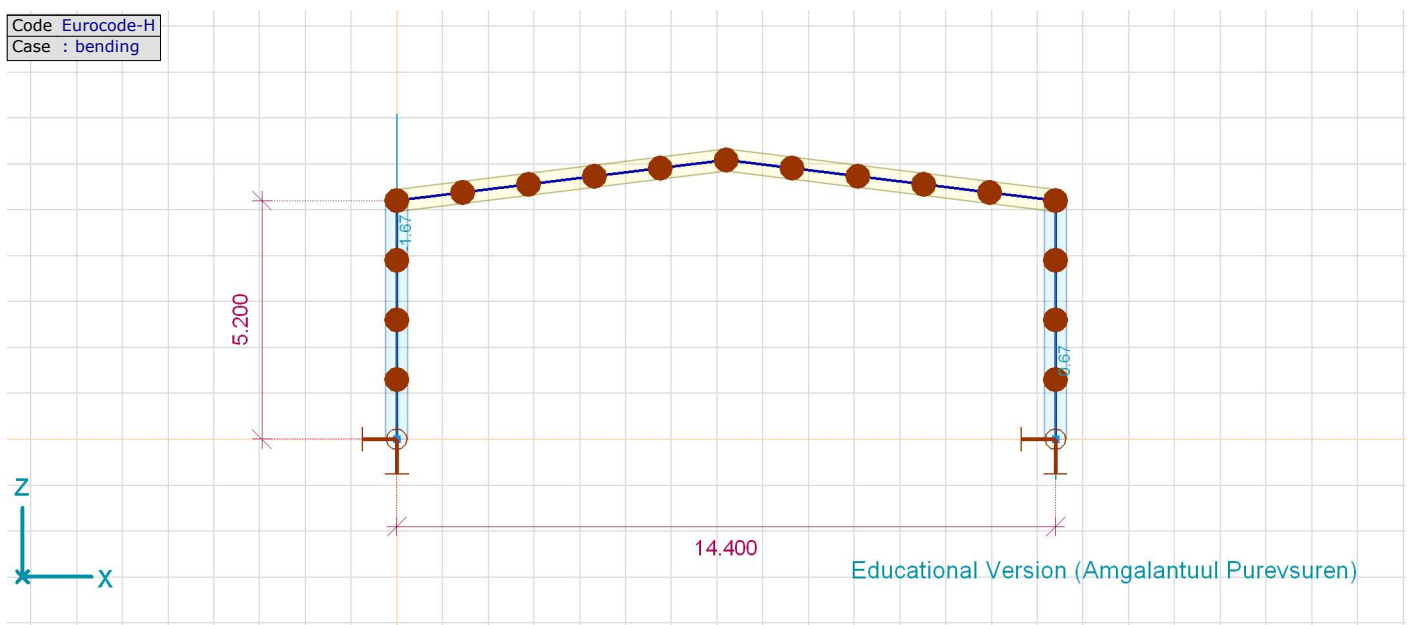
5/15/2022

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Code Eurocode-H
Case : ST2

*ST2, Front view*

Code Eurocode-H
Case : bending

*bending, Front view*

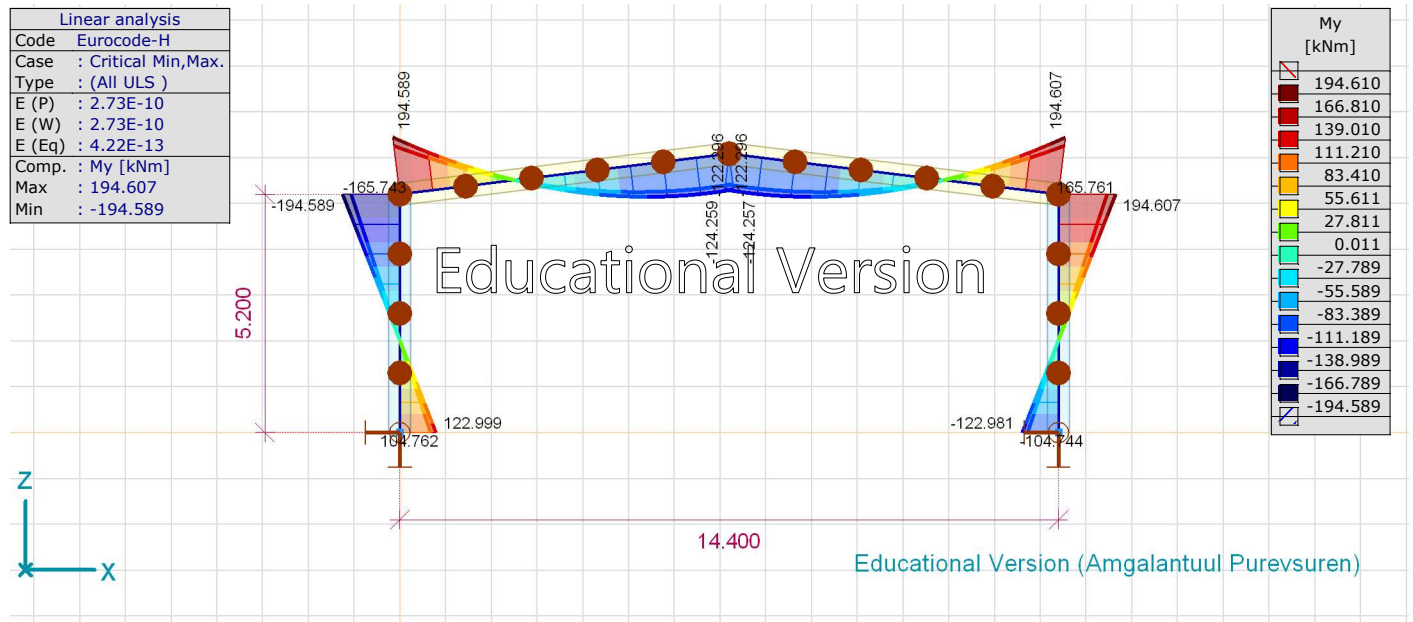
Project

Analysis by Amgalantuul Purevsuren

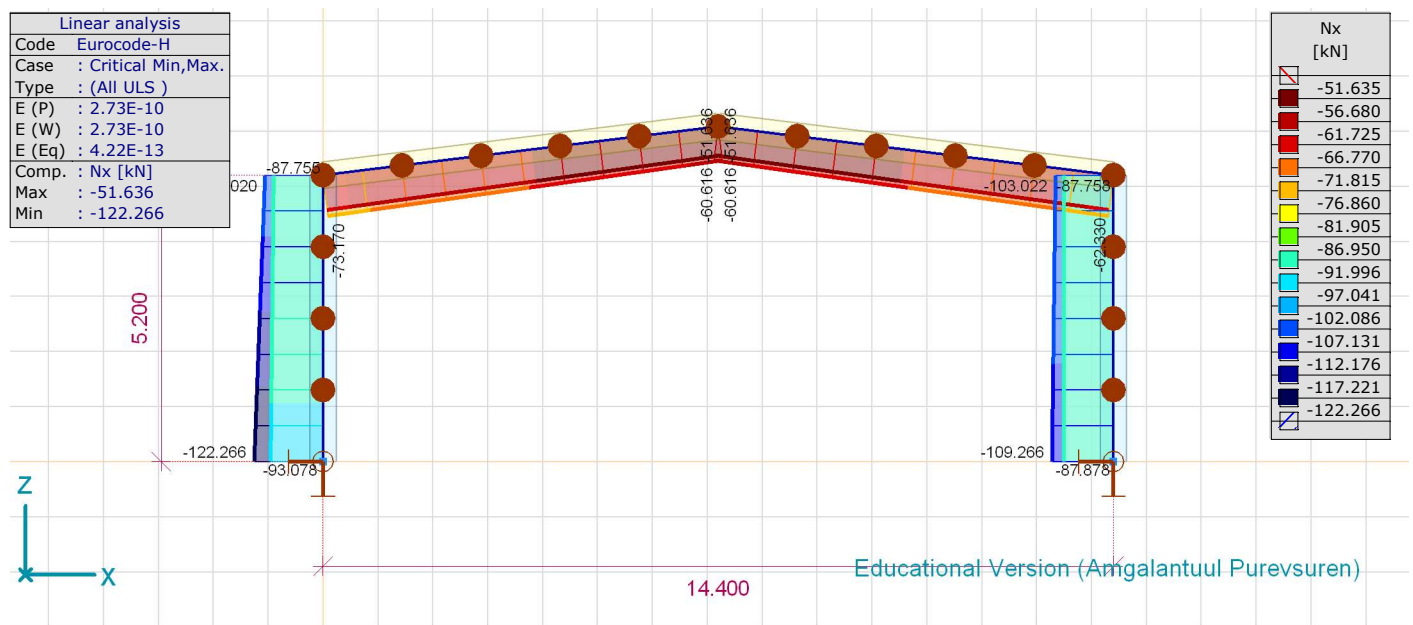
Model: **Model 5.axs**

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[I], Linear,(Auto) Critical, My, Filled diagram, Front view



[I], Linear,(Auto) Critical, Nx, Filled diagram, Front view