STAT135: Confidence intervals and more cars

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Chapter 17 in a nutshell

- The distribution of sample means is less variable than the distribution of the underlying population
- The distribution of sample means is more normal than the distribution of the underlying population

Confidence intervals for a proportion

 $SE(\hat{p}) =$

Constructing a confidence interval:

Interpreting a confidence interval:

Example 1: Each of the 110 students in a statistics class selects a different random sample of 35 Quiz scores from a population of 5000 scores they are given. Using their data, each student constructs a 90% confidence interval for μ , the average Quiz score of the 5000 students. Which of the following conclusions is correct?

- a) About 10% of the sample means will not be included in the confidence intervals.
- b) About 90% of the confidence intervals will contain μ .
- c) It is probable that 90% of the confidence intervals will be identical.
- d) About 10% of the raw scores in the samples will not be found in these confidence intervals.

Example 2: Suppose two researchers want to estimate the proportion of American college students who favor abolishing the penny. They both want to have about the same margin of error to estimate this proportion. However, Researcher 1 wants to estimate with 99% confidence and Researcher 2 wants to estimate with 95% confidence. Which researcher would need more students for her study in order to obtain the desired margin of error?

- a) Researcher 1.
- b) Researcher 2.
- c) Both researchers would need the same number of subjects.
- d) It is impossible to obtain the same margin of error with the two different confidence levels.

More cars

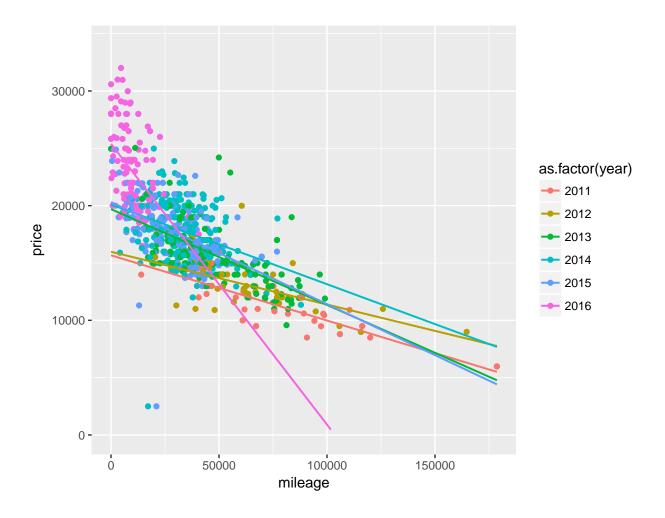
```
ds <- read_csv("carscollated2017.csv")
ds <- ds %>%
  mutate(price = readr::parse_number(price))
```

year ## 2007 2010 2011 2012 2013 2014 2015 2016 2017 Total 2 237 201 126 831 5 37 45 176 tally(~ location, margins=TRUE, data=ds) ## location ## 40202 Bangor, ME Baton Rouge Boston Atlanta ## 40 40 40 40 Cleveland Dallas Los Angeles ## Buffalo Chicago ## 40 41 26 41 40 ## Minneapolis New Orleans NYC Phoenix Portland ## 33 40 40 40 59 Richmond Salt Lake City San Diego Seattle ## San Francisco ## 40 40 39 39 33 ## Tampa Total ## 40 831 ds <- filter(ds, year > 2010, year < 2017) # drop new cars and really old cars gf_point(price ~ mileage, color = ~ as.factor(year), data = ds) %>% gf_lm() %>%

Warning: Removed 34 rows containing missing values (geom_lm).

tally(~ year, margins=TRUE, data=ds)

 $gf_{lims}(y = c(0, 34000))$



a) interpret what insights you can make from the scatterplot SOLUTION:

```
options(scipen=5, show.signif.stars=FALSE, digits=4)
mod <- lm(price ~ location + mileage + as.factor(year) + mileage*as.factor(year), data=ds)
msummary(mod)</pre>
```

```
##
                                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                              17061.06938
                                           868.85620
                                                       19.64 < 2e-16
## locationAtlanta
                              -1638.41488
                                           462.55755
                                                       -3.54 0.00042
## locationBangor, ME
                              -1689.69743
                                           463.90469
                                                       -3.64 0.00029
## locationBaton Rouge
                               -745.21252
                                           474.32078
                                                       -1.57 0.11656
## locationBoston
                               -563.64808
                                           460.06933
                                                       -1.23 0.22089
## locationBuffalo
                                                       -1.20 0.23008
                              -581.60744
                                           484.23517
## locationChicago
                              -2237.49897
                                           456.49750
                                                       -4.90 1.2e-06
```

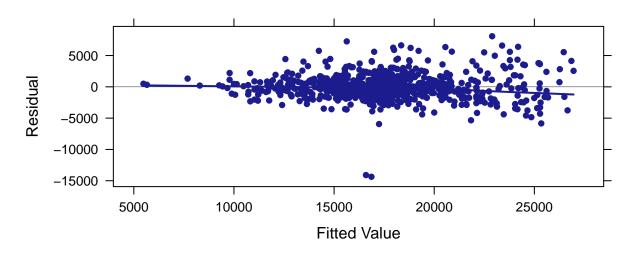
```
## locationCleveland
                               -1491.58656
                                             520.87678
                                                         -2.86 0.00430
## locationDallas
                                                         -2.33
                               -1078.11128
                                             462.04754
                                                                0.01988
## locationLos Angeles
                               2319.67933
                                             460.04752
                                                         5.04
                                                                5.7e-07
## locationMinneapolis
                               -622.89582
                                             423.72233
                                                         -1.47
                                                                0.14194
## locationNew Orleans
                               -573.29737
                                             498.84387
                                                         -1.15
                                                                0.25080
## locationNYC
                                                         -1.30
                               -594.56186
                                             458.89342
                                                                0.19548
## locationPhoenix
                               -325.96320
                                                         -0.70
                                             463.81240
                                                                0.48239
## locationPortland
                                  65.24543
                                             461.66827
                                                         0.14
                                                                0.88765
## locationRichmond
                               -744.32172
                                             461.18604
                                                         -1.61
                                                                0.10694
## locationSalt Lake City
                                                         -3.95
                               -1954.04693
                                             494.67997
                                                                8.5e-05
## locationSan Diego
                                257.69790
                                             461.97731
                                                          0.56
                                                                0.57713
## locationSan Francisco
                                                          3.42
                                                                0.00066
                               1578.28190
                                             461.39289
## locationSeattle
                                2136.54194
                                             463.06079
                                                          4.61
                                                                4.6e-06
## locationTampa
                                                         -4.66
                               -2152.29736
                                             462.16712
                                                                3.8e-06
## mileage
                                               0.00950
                                                         -6.38
                                                                3.0e-10
                                  -0.06065
## as.factor(year)2012
                                -251.31079
                                            1135.10846
                                                         -0.22
                                                                0.82484
## as.factor(year)2013
                                                          3.62
                                                                0.00032
                                3237.23166
                                             894.68539
## as.factor(year)2014
                                3140.19070
                                             888.34344
                                                          3.53
                                                                0.00043
                                             885.30630
## as.factor(year)2015
                                3252.51391
                                                          3.67
                                                                0.00026
## as.factor(year)2016
                                8208.61054
                                            874.47684
                                                          9.39
                                                                < 2e-16
## mileage:as.factor(year)2012
                                  0.01709
                                              0.01436
                                                          1.19 0.23445
## mileage:as.factor(year)2013
                                  -0.01797
                                               0.01215
                                                         -1.48
                                                                0.13939
## mileage:as.factor(year)2014
                                  -0.00343
                                                         -0.25
                                                                0.80603
                                               0.01396
## mileage:as.factor(year)2015
                                  -0.00989
                                               0.01393
                                                         -0.71
                                                                0.47777
## mileage:as.factor(year)2016
                                  -0.18186
                                               0.02754
                                                         -6.60 7.3e-11
## Residual standard error: 2040 on 790 degrees of freedom
## Multiple R-squared: 0.736, Adjusted R-squared: 0.726
## F-statistic: 71.2 on 31 and 790 DF, p-value: <2e-16
```

b) interpret the regression results

SOLUTION:

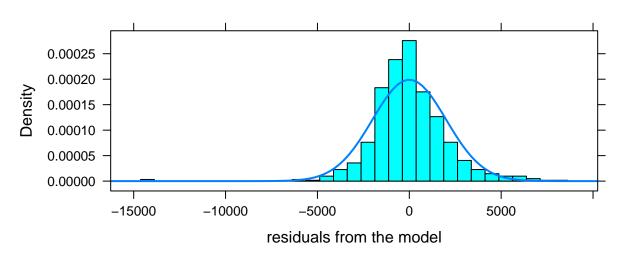
```
mplot(mod, which=1) # Figure 1
```

Residuals vs Fitted



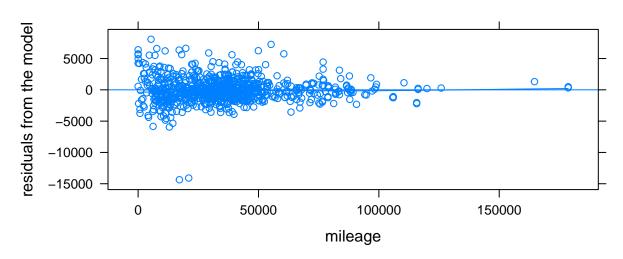
histogram(~ resid(mod), fit="normal", width=750, main="Figure 2", xlab="residuals from the model")





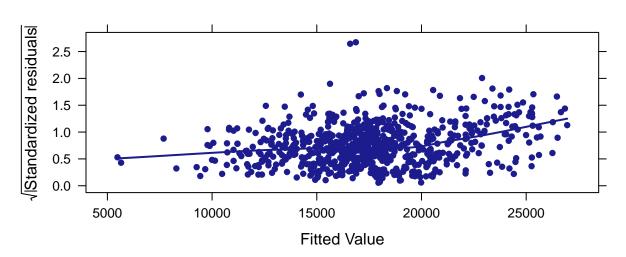
xyplot(resid(mod) ~ mileage, type=c("p", "r", "smooth"), ylab="residuals from the model",
 main="Figure 3", data=ds)

Figure 3



mplot(mod, which=3) # Figure 4

Scale-Location



c) interpret the regression diagnostics

(be sure to specify which assumption is being verified using which figure) SOLUTION:

```
carfun <- makeFun(mod)</pre>
carfun(year=2016, mileage=1000, location='Tampa')
##
       1
## 22875
carfun(year=2016, mileage=1000, location='Tampa') -
carfun(year=2016, mileage=1001, location='Tampa')
##
## 0.2425
carfun(year=2012, mileage=1000, location='Tampa') -
carfun(year=2012, mileage=1001, location='Tampa')
## 0.04355
ds <- mutate(ds, fitted = predict(mod), resid = resid(mod))</pre>
filter(ds, resid(mod) < -10000)</pre>
## # A tibble: 2 x 8
##
            car model price year mileage location fitted resid
           <chr> <chr> <dbl> <int> <dbl>
                                               <chr> <dbl> <dbl>
## 1 Toyota Prius four 2500 2014
                                     17152 Chicago 16865 -14365
## 2 Toyota Prius four 2500 2015 21027 Chicago 16593 -14093
```

d) what might we conclude about the large residuals?

SOLUTION: