

سوال (3)

$$f_1(n) = \Omega(g_1(n)), f_2(n) = \Omega(g_2(n))$$

$$\hookrightarrow f_1(n) \geq c g_1(n) \quad \hookrightarrow f_2(n) \geq c g_2(n)$$

* ایک فریکٹ اے

$$\Rightarrow f_1(n) \cdot f_2(n) \geq c g_1(n) \cdot c g_2(n)$$

$$\Rightarrow f_1(n) \cdot f_2(n) = \Omega(g_1(n) \cdot g_2(n))$$

سوال (4)

$$a) f(N) = 100N^2 + 200N^4 + N^3$$

چون $200N^4$ از بقید بزرگتر اے پس $O(N^4)$

$$b) f(N) = N^2 \log N + N^3 + 1000N^4$$

چون N^3 بزرگتر از بقید اے پس $O(N^3)$

$$c) f(N) = 100N + \frac{N}{2} \log\left(\frac{N}{2}\right) + N/4$$

$$\downarrow$$

$$\log(N) - \log(2)$$

چون $\frac{N}{2} \log N$ از بقید بزرگتر اے پس $O(N \log N)$



$$d) f(N) = \frac{N}{4} + N^{\frac{1}{2}}$$

چوں $\frac{N}{4}$ بزرگتر از بقیه است پس $O(N)$

$$e) f(N) = N \log(N^4) + 3N^2$$

چوں $3N^2$ بزرگتر از بقیه است پس $O(N^2)$

$$p(n) = n^2$$

سوال 5

$$\Rightarrow \log p(n) \Rightarrow \log n^2 \Rightarrow 2 \log n \Rightarrow O(\log n)$$

$$4n \log n + 2n = O(n \log n), 2^b = O(1) \quad \text{سوال 6}$$

$$2^{\log n} \Rightarrow a^{\log n} = b \Rightarrow n \Rightarrow O(n), 4n = O(n)$$

$$3n + 100 \log n = O(n), 2^n = O(2^n)$$

$$n^2 + 10n = O(n^2), n^3 = O(n^3), n \log n = O(n \log n)$$

ترتیب ←

$$2^{10} > 4n = 2^{\log n} = 3n + 100 \log n > 4n \log n + 2n = n \log n$$

$$n^2 + 10n > n^3 > 2^n$$

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$$T(n) = aT(n/b) + f(n)$$

\downarrow
 cn^k

سوال (7) تھو، ستر ←

$$a < b^k$$

$$a = b^k$$

$$a > b^k$$

$$\left. \begin{array}{l} n^k \\ n^k \log(n) \\ n^{\log_b a} \end{array} \right\}$$

Δ لا ت مكن

$$a) T(n) = 3T(n/3) + n^3 \Rightarrow a=3, b=3, k=3.$$

$$\Rightarrow a < b^k \Rightarrow O(n^3)$$

$$b) T(n) = 3T(n/2) + n \Rightarrow a=3, b=2, k=1$$

$$\Rightarrow a > b^k \Rightarrow O(n^{\log_2 3})$$

$$c) T(n) = 2T(n/3) + 3n^2 + n \Rightarrow a=2, b=3, k=2$$

$$\Rightarrow a < b^k \Rightarrow O(n^2)$$

$$d) T(n) = T\left(\frac{2n}{3}\right) + 1 \Rightarrow a=1, b=\frac{3}{2}, k=0$$

$$\Rightarrow a = b^k \Rightarrow O(n^0 \log n) \Rightarrow O(\log n)$$

$$e) T(n) = 8T\left(\frac{n}{2}\right) + n^3 (\log_2 n)^2 \Rightarrow a=8, b=2, k=3$$

$$\Rightarrow a = b^k \Rightarrow O(n^3 \log n)$$



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$$f) T(n) = T\left(\frac{7n}{8}\right) + (\log_2 n)^4 \Rightarrow a=1, b=\frac{8}{7}, k=4$$

$$\Rightarrow a < b^k \Rightarrow O(n^4)$$

$$\text{example 1} \Rightarrow O(n), \text{ example 2} \Rightarrow O\left(\frac{n}{2}\right) \quad (8) \text{ سوال}$$

$$\text{example 3} \Rightarrow O(n^2), \text{ example 4} \Rightarrow O(n)$$

$$\text{example 5} \Rightarrow O(n^3)$$

$$T: T(n) = 7T(n/2) + n^2$$

(10) سوال

$$C: T(n) = aT(n/4) + n^2$$

$$\log_b^a n \Rightarrow \log_4^a n > \log_2^7 n$$

$$\Rightarrow n^{\log_{22}^a} > n^{\log_2^7} \Rightarrow a = 49$$

سوال (11)

$$\sum_{i=1}^n \log i \Rightarrow \log 1 + \log 2 + \log 3 + \dots + \log n$$

$n=3$ $\log n$ n

$$\Rightarrow O(n \log n)$$

$$\text{while loop} \Rightarrow O(n/2)$$

سوال (12)

$$\text{first for loop} \Rightarrow O(n)$$

$$\text{second for loop} \Rightarrow O(n^5)$$

$$\Rightarrow O(n/2 \cdot n \cdot n^5) \Rightarrow O\left(\frac{n^2}{2}\right) \Rightarrow O(n^2)$$



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