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# **Imfit documentation**

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The Imfit Python package provides a simple, flexible interface to non-linear least-squares optimization, or curve fitting. By default, Imfit uses and builds upon the [Levenberg-Marquardt](#) minimization algorithm from [MINPACK-1](#) as implemented in [scipy.optimize.leastsq](#). Support for other optimization routines is being added. Currently, the [L-BFGS](#) (limited memory Broyden-Fletcher-Goldfarb-Shanno) algorithm as implemented in [scipy.optimize.l\\_bfgs\\_b](#) or the [simulated annealing](#) algorithm as implemented in [scipy.optimize.anneal](#) are both implemented and partially tested, and other optimization routines are being considered. As the Levenberg-Marquardt algorithm is the most tested and appears to be the most robust for finding local minima of well-described models of scientific measurements, parts of this document may assume that it Levenberg-Marquardt algorithm is being discussed.

For any minimization problem, the programmer must provide a function that takes a set of values for the variables in the fit, and produces the residual function to be minimized in the least-squares sense.

The Imfit package allows models to be written in terms of a set of Parameters, which are extensions of simple numerical variables with the following properties:

- Parameters can be fixed or floated in the fit.
- Parameters can be bounded with a minimum and/or maximum value.
- Parameters can be written as simple mathematical expressions of other Parameters. These values will be re-evaluated at each step in the fit, so that the expression is satisfied. This gives a simple but flexible approach to constraining fit variables.

The main advantage to using Parameters instead of fit variables is that the model function does not have to be rewritten for a change in what is varied or what constraints are placed on the fit. The programmer can write a fairly general model, and allow a user of the model to change what is varied and what constraints are placed on the model.

For the Levenberg-Marquardt algorithm, Imfit also calculates and reports the estimated uncertainties and correlation between fitted variables.



# DOWNLOADING AND INSTALLATION

## 1.1 Prerequisites

The lmfit package requires Python, Numpy, and Scipy. Extensive testing on version compatibility has not yet been done. Initial tests work with Python 3.1, but no testing with Python 3.2 has yet been done. No testing has been done with 64-bit architectures, but as this model is pure Python, no significant troubles are expected.

## 1.2 Downloads

The latest stable version is available from a few sources:

Download Option	Python Versions	Location
Source Kit	2.6, 2.7, 3.1	<ul style="list-style-type: none"><li>• <a href="#">lmfit-0.3.tar.gz</a> (PyPI)</li><li>• <a href="#">lmfit-0.3.tar.gz</a> (CARS)</li></ul>
Win32 Installer	2.6	<ul style="list-style-type: none"><li>• <a href="#">lmfit-0.3.win32-py2.6.exe</a> (PyPI)</li><li>• <a href="#">lmfit-0.3.win32-py2.6.exe</a> (CARS)</li></ul>
Win32 Installer	2.7	<ul style="list-style-type: none"><li>• <a href="#">lmfit-0.3.win32-py2.7.exe</a> (PyPI)</li><li>• <a href="#">lmfit-0.3.win32-py2.7.exe</a> (CARS)</li></ul>
Win32 Installer	3.1	<ul style="list-style-type: none"><li>• <a href="#">lmfit-0.3.win32-py3.1.exe</a> (PyPI)</li><li>• <a href="#">lmfit-0.3.win32-py3.1.exe</a> (CARS)</li></ul>
Development Version	all	use <a href="#">lmfit github repository</a>

if you have [Python Setup Tools](#) installed, you can download and install the PyEpics Package simply with:

```
easy_install -U lmfit
```

## 1.3 Development Version

To get the latest development version, use:

```
git clone http://github.com/newville/lmfit-py.git
```

## 1.4 Installation

Installation from source on any platform is:

```
python setup.py install
```

## 1.5 License

The LMFIT-py code is distributed under the following license:

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# GETTING STARTED WITH NON-LINEAR LEAST-SQUARES FITTING

The `lmfit` package is designed to provide a simple way to build complex fitting models and apply them to real data. This chapter describes how to set up and perform simple fits, but does assume some basic knowledge of Python, Numpy, and modeling data.

To model data in the least-squares sense, the most important step is writing a function that takes the values of the fitting variables and calculates a residual function (data-model) that is to be minimized in the least-squares sense

$$\chi^2 = \sum_i^N \frac{[y_i^{\text{meas}} - y_i^{\text{model}}(\mathbf{v})]^2}{\epsilon_i^2}$$

where  $y_i^{\text{meas}}$  is the set of measured data,  $y_i^{\text{model}}(\mathbf{v})$  is the model calculation,  $\mathbf{v}$  is the set of variables in the model to be optimized in the fit, and  $\epsilon_i$  is the estimated uncertainty in the data.

In a traditional non-linear fit, one writes a function that takes the variable values and calculates the residual  $y_i^{\text{meas}} - y_i^{\text{model}}(\mathbf{v})$ , perhaps something like:

```
def residual(vars, x, data):
    amp = vars[0]
    phaseshift = vars[1]
    freq = vars[2]
    decay = vars[3]

    model = amp * sin(x * freq + phaseshift) * exp(-x*x*decay)

    return (data-model)
```

To perform the minimization with `scipy`, one would do:

```
from scipy.optimize import leastsq
vars = [10.0, 0.2, 3.0, 0.007]
out = leastsq(residual, vars, args=(x, data))
```

Though in python, and fairly easy to use, this is not terribly different from how one would do the same fit in C or Fortran.

## 2.1 Using Parameters instead of Variables

As described above, there are several practical challenges in doing least-squares fit with the traditional implementation (Fortran, `scipy.optimize.leastsq`, and most other) in which a list of fitting variables to the function to be minimized. These challenges include:

1. The user has to keep track of the order of the variables, and their meaning – vars[2] is the frequency, and so on.
2. If the user wants to fix a particular variable (*not* vary it in the fit), the residual function has to be altered. While reasonable for simple cases, this quickly becomes significant work for more complex models, and greatly complicates modeling for people not intimately familiar with the code.
3. There is no way to put bounds on values for the variables, or enforce mathematical relationships between the variables.

The lmfit module is designed to void these shortcomings.

The main idea of lmfit is to expand a numerical variable with a `Parameter`, which have more attributes than simply their value. Instead of a pass a list of numbers to the function to minimize, you create a `Parameters` object, add parameters to this object, and pass along this object to your function to be minimized. With this transformation, the above example would be translated to look like:

```
from lmfit import minimize, Parameters

def residual(params, x, data):
    amp = params['amp'].value
    pshift = params['phase'].value
    freq = params['frequency'].value
    decay = params['decay'].value

    model = amp * sin(x * freq + pshift) * exp(-x*x*decay)

    return (data-model)

params = Parameters()
params.add('amp', value=10)
params.add('decay', value=0.007)
params.add('phase', value=0.2)
params.add('frequency', value=3.0)

out = minimize(residual, params, args=(x, data))
```

So far, this simply looks like it replaced a list of values with a dictionary, accessed by name. But each of the named `Parameter` in the `Parameters` object hold additional attributes to modify the value during the fit. For example, Parameters can be fixed or bounded, and this can be done when being defined:

```
params = Parameters()
params.add('amp', value=10, vary=False)
params.add('decay', value=0.007, min=0.0)
params.add('phase', value=0.2)
params.add('frequency', value=3.0, max=10)
```

or later:

```
params['amp'].vary = True
params['decay'].max = 0.10
```

Now the fit will *not* vary the amplitude parameter, and will also impose a lower bound on the decay factor and an upper bound on the frequency. Importantly, our function to be minimized remains unchanged.

An important point here is that the `params` object can be copied and modified to make many user-level changes to the model and fitting process. Of course, most of the information about how your data is modeled goes into the fitting function, but the approach here allows some external control as well.

## 2.2 The Parameter class

**class Parameter** (*value=None*, *vary=True*, *min=None*, *max=None*, *name=None*, *expr=None*)]])  
 create a Parameter object. These are the fundamental extension of a fit variable within Imfit, but you will probably create most of these with the [Parameters](#) class.

### Parameters

- **value** – the numerical value for the parameter
- **vary** (boolean (True/False)) – whether to vary the parameter or not.
- **min** – lower bound for value (None = no lower bound).
- **max** – upper bound for value (None = no upper bound).
- **name** (None or string – will be overwritten during fit if None.) – parameter name
- **expr** (None or string) – mathematical expression to use to evaluate value during fit.

Each of these inputs is turned into an attribute of the same name. As above, one hands a dictionary of Parameters to the fitting routines. The name for the Parameter will be set to be consistent

After a fit, a Parameter for a fitted variable (ie with `vary = True`) will have the `value` attribute holding the best-fit value, and may (depending on the success of the fit) have obtain additional attributes.

### stderr

the estimated standard error for the best-fit value.

### correl

a dictionary of the correlation with the other fitted variables in the fit, of the form:

```
{'decay': 0.404, 'phase': -0.020, 'frequency': 0.102}
```

The `expr` attribute can contain a mathematical expression that will be used to compute the value for the Parameter at each step in the fit. See [Using Mathematical Constraints](#) for more details and examples of this feature.

## 2.3 The Parameters class

### class Parameters

create a Parameters object. This is little more than a fancy dictionary, with the restrictions that

1. keys must be valid Python symbol names (so that they can be used in expressions of mathematical constraints). This means the names must match `[a-z_][a-z0-9_]*` and cannot be a Python reserved word.
2. values must be valid [Parameter](#) objects.

Two methods for provided for convenience of initializing Parameters.

**add** (*name*, *value=None*, *vary=True*, *min=None*, *max=None*, *expr=None*)]])

add a named parameter. This simply creates a [Parameter](#) object associated with the key *name*, with optional arguments passed to [Parameter](#):

```
p = Parameters()
p.add('myvar', value=1, vary=True)
```

**add\_many** (*self*, *paramlist*)

add a list of named parameters. Each entry must be a tuple with the following entries:

```
name, value, vary, min, max, expr
```

That is, this method is somewhat rigid and verbose (no default values), but can be useful when initially defining a parameter list so that it looks table-like:

```
p = Parameters()
#      (Name,   Value,   Vary,   Min,   Max,   Expr)
p.add_many(('amp1',    10,   True, None, None, None),
           ('cen1',    1.2,   True,  0.5,  2.0, None),
           ('wid1',    0.8,   True,  0.1, None, None),
           ('amp2',    7.5,   True, None, None, None),
           ('cen2',    1.9,   True,  1.0,  3.0, None),
           ('wid2',   None, False, None, None, '2*wid1/3'))
```

## 2.4 Simple Example:

Putting it all together, a simple example of using a dictionary of `Parameters` and `minimize()` might look like this:

```
from lmfit import minimize, Parameters

def residual(params, x, data=None):
    amp = params['amp'].value
    shift = params['phase_shift'].value
    omega = params['omega'].value
    decay = params['decay'].value

    model = amp * sin(x * omega + shift) * exp(-x*x*decay)

    return (data-model)

params = Parameters()
params.add('amp', value=10)
params.add('decay', value=0.007, vary=False)
params.add('phase_shift', value=0.2)
params.add('omega', value=3.0)

result = minimize(residual, params, args=(x, data))

print result.chisqr
print 'Best-Fit Values:'
for name, par in params.items():
    print ' %s = %.4f +/- %.4f ' % (name, par.value, par.stderr)
```

# PERFORMING FITS, ANALYZING OUTPUTS

As shown in the previous sections, a simple fit can be performed with the `minimize()` function. For more sophisticated modeling, the `Minimizer` class can be used to gain a bit more control, especially when using complicated constraints.

## 3.1 The `minimize()` function

The `minimize` function takes a function to minimize, a dictionary of `Parameter`, and several optional arguments. See *Writing a Fitting Function* for details on writing the function to minimize.

**`minimize`** (*function*, *params*[, *args*=None[, *kws*=None[, *engine*='leastsq'[, *\*\*leastsq\_kws*]]]])  
find values for the params so that the sum-of-squares of the returned array from function is minimized.

### Parameters

- **function** (*callable*.) – function to return fit residual. See *Writing a Fitting Function* for details.
- **params** (*dict*) – a dictionary of Parameters. Keywords must be strings that match `[a-z_][a-z0-9_]*` and is not a python reserved word. Each value must be `Parameter`.
- **args** (*tuple*) – arguments tuple to pass to the residual function as positional arguments.
- **kws** (*dict*) – dictionary to pass to the residual function as keyword arguments.
- **engine** (*string*) – name of fitting engine to use. See *Choosing Different Fitting Engines* for details
- **leastsq\_kws** (*dict*) – dictionary to pass to `scipy.optimize.leastsq`

**Returns** `Minimizer` object, which can be used to inspect goodness-of-fit statistics, or to re-run fit.

On output, the params will be updated with best-fit values and, where appropriate, estimated uncertainties and correlations. See *Goodness-of-Fit and estimated uncertainty and correlations* for further details.

## 3.2 Writing a Fitting Function

An important component of a fit is writing a function to be minimized in the least-squares sense. Since this function will be called by other routines, there are fairly stringent requirements for its call signature and return value. In

principle, your function can be any python callable, but it must look like this:

```
func(params, *args, **kws) :  
    calculate residual from parameters.
```

#### Parameters

- **params** (*dict*) – parameters.
- **args** – positional arguments. Must match *args* argument to `minimize()`
- **kws** – keyword arguments. Must match *kws* argument to `minimize()`

**Returns** residual array (generally data-model) to be minimized in the least-squares sense.

**Return type** numpy array. The length of this array cannot change between calls.

A common use for the positional and keyword arguments would be to pass in other data needed to calculate the residual, including such things as the data array, dependent variable, uncertainties in the data, and other data structures for the model calculation.

As the function will be passed in a dictionary of `Parameter`s, it is advisable to unpack these to get numerical values at the top of the function. A simple example would look like:

```
def residual(pars, x, data=None):  
    # unpack parameters:  
    # extract .value attribute for each parameter  
    amp = pars['amp'].value  
    period = pars['period'].value  
    shift = pars['shift'].value  
    decay = pars['decay'].value  
  
    if abs(shift) > pi/2:  
        shift = shift - sign(shift)*pi  
  
    if abs(period) < 1.e-10:  
        period = sign(period)*1.e-10  
  
    model = amp * sin(shift + x/per) * exp(-x*x*decay*decay)  
  
    if data is None:  
        return model  
    return (model - data)
```

In this example, `x` is a positional (required) argument, while the `data` array is actually optional (so that the function returns the model calculation if the data is neglected). Also note that the model calculation will divide `x` by the varied value of the 'period' Parameter. It might be wise to make sure this parameter cannot be 0. It would be possible to use the bounds on the `Parameter` to do this:

```
params['period'] = Parameter(value=2, min=1.e-10)
```

but might be wiser to put this directly in the function with:

```
if abs(period) < 1.e-10:  
    period = sign(period)*1.e-10
```

## 3.3 Choosing Different Fitting Engines

By default, the `Levenberg-Marquardt` algorithm is used for fitting. While often criticized, including the fact it finds a *local* minima, this approach has some distinct advantages. These include being fast, and well-behaved for most

curve-fitting needs, and making it easy to estimate uncertainties for and correlations between pairs of fit variables, as discussed in *Goodness-of-Fit and estimated uncertainty and correlations*.

Alternative algorithms can also be used. These include *simulated annealing* which promises a better ability to avoid local minima, and *BFGS*, which is a modification of the quasi-Newton method.

To Select which of these algorithms to use, use the `engine` keyword to the `minimize()` function or use the corresponding method name from the `Minimizer` class as listed in the *Table of Supported Fitting Engines*.

Table of Supported Fitting Engines:

Engine	engine arg to <code>minimize()</code>	Minimizer method
Levenberg-Marquardt	<code>leastsq</code>	<code>leastsq()</code>
Simulated Annealing	<code>anneal</code>	<code>anneal()</code>
L-BFGS-B	<code>lbfgsb</code>	<code>lbfgsb()</code>

## 3.4 Goodness-of-Fit and estimated uncertainty and correlations

On a successful fit using the *leastsq* engine, several goodness-of-fit statistics and values related to the uncertainty in the fitted variables will be calculated. These are all encapsulated in the `Minimizer` object for the fit, as returned by `minimize()`. The values related to the entire fit are stored in attributes of the `Minimizer` object, as shown in *Table of Goodness-of-Fit Statistics* while those related to each fitted variables are stored as attributes of the corresponding `Parameter`.

Table of Goodness-of-Fit Statistics: These statistics are all attributes of the `Minimizer` object returned by `minimize()`.

Minimizer Attribute	Description / Formula
<code>nfev</code>	number of function evaluations
<code>success</code>	boolean (True/False) for whether fit succeeded.
<code>errorbars</code>	boolean (True/False) for whether uncertainties were estimated.
<code>message</code>	message about fit success.
<code>ier</code>	integer error value from <code>scipy.optimize.leastsq</code>
<code>lmdif_message</code>	message from <code>scipy.optimize.leastsq</code>
<code>nvarys</code>	number of variables in fit $N_{\text{varys}}$
<code>ndata</code>	number of data points: $N$
<code>nfree</code>	degrees of freedom in fit: $N - N_{\text{varys}}$
<code>residual</code>	residual array (return of <code>func()</code> ): <code>Resid</code>
<code>chisqr</code>	chi-square: $\chi^2 = \sum_i^N [\text{Resid}_i]^2$
<code>redchi</code>	reduced chi-square: $\chi^2_\nu = \chi^2 / (N - N_{\text{varys}})$

Note that the calculation of chi-square and reduced chi-square assume that the returned residual function is scaled properly to the uncertainties in the data. For these statistics to be meaningful, the person writing the function to function to be minimized must scale them properly.

When possible, standard errors for the fitted variables, and correlations between pairs of fitted variables are automatically calculated after the fit is performed. The standard error (estimated  $1\sigma$  error-bar) go into the `stderr` attribute of the `Parameter`. The correlations with all other variables will be put into the `correl` attribute of the `Parameter` – a dictionary with keys for all other `Parameters` and values of the corresponding correlation.

In some cases, it may not be possible to estimate the errors and correlations. For example, if a variable actually has no practical effect on the fit, it will likely cause the covariance matrix to be singular, so that errors cannot be estimated. Placing bounds on varied `Parameters` makes it more likely that errors cannot be estimated, as being near the maximum or minimum value makes the covariance matrix singular. In these cases, the `errorbars` attribute of the fit result (`Minimizer` object) will be `False`.

## 3.5 Using the `Minimizer` class

For full control of the fitting process, you'll want to create a `Minimizer` object, or at least use the one returned from the `minimize()` function.

**class `Minimizer`** (*function*, *params*[, *fcn\_args*=None[, *fcn\_kws*=None[, *\*\*kws*]]])

creates a `Minimizer`, for fine-grain access to fitting methods and attributes.

### Parameters

- **function** (*callable*.) – function to return fit residual. See [Writing a Fitting Function](#) for details.
- **params** (*dict*) – a dictionary of Parameters. Keywords must be strings that match `[a-z_][a-z0-9_]*` and is not a python reserved word. Each value must be `Parameter`.
- **fcn\_args** (*tuple*) – arguments tuple to pass to the residual function as positional arguments.
- **fcn\_kws** (*dict*) – dictionary to pass to the residual function as keyword arguments.
- **leastsq\_kws** (*dict*) – dictionary to pass to `scipy.optimize.leastsq`

**Returns** `Minimizer` object, which can be used to inspect goodness-of-fit statistics, or to re-run fit.

The `Minimizer` object has a few public methods:

**`leastsq`** (*\*\*kws*)

perform fit with Levenberg-Marquardt algorithm. Keywords will be passed directly to `scipy.optimize.leastsq`. By default, numerical derivatives are used, and the following arguments are set:

leastsq argument	Default Value	Description
<code>xtol</code>	1.e-7	Relative error in the approximate solution
<code>ftol</code>	1.e-7	Relative error in the desired sum of squares
<code>maxfev</code>	1000*(nvar+1)	maximum number of function calls (nvar= # of variables)

**`anneal`** (*\*\*kws*)

perform fit with Simulated Annealing. Keywords will be passed directly to `scipy.optimize.anneal`.

**`lbfgsb`** (*\*\*kws*)

perform fit with L-BFGS-B algorithm. Keywords will be passed directly to `scipy.optimize.fmin_l_bfgs_b`.

**`prepare_fit`** (*\*\*kws*)

prepares and initializes model and Parameters for subsequent fitting. This routine prepares the conversion of `Parameters` into fit variables, organizes parameter bounds, and parses, checks and “compiles” constrain expressions.

This is called directly by the fitting methods, and it is generally not necessary to call this function explicitly. An exception is when you would like to call your function to minimize prior to running one of the minimization routines, for example, to calculate the initial residual function. In that case, you might want to do something like:

```
myfit = Minimizer(my_residual, params, fcn_args=(x,), fcn_kws={'data':data})

myfit.prepare_fit()
init = my_residual(p_fit, x)
pylab.plot(x, init, 'b--')

myfit.leastsq()
```

That is, this method should be called prior to your fitting function being called.



# USING MATHEMATICAL CONSTRAINTS

While being able to fix variables and place upper and lower bounds on their values are key parts of `lmfit`, an equally important feature is the ability to place mathematical constraints on parameters. This section describes how to do this, and what sort of parameterizations are possible.

## 4.1 Overview

Just as one can place bounds on a `Parameter`, or keep it fixed during the fit, so too can one place mathematical constraints on parameters. The way this is done with `lmfit` is to write a `Parameter` as a mathematical expression of the other parameters and a set of pre-defined operators and functions. The constraint expressions are simple Python statements, allowing one to place constraints like:

```
pars = Parameters()
pars.add('frac_curve1', value=0.5, min=0, max=1)
pars.add('frac_curve2', expr='1-frac_curve1')
```

as the value of the `frac_curve1` parameter is updated at each step in the fit, the value of `frac_curve2` will be updated so that the two values are constrained to add to 1.0. Of course, such a constraint could be placed in the fitting function, but the use of such constraints allows the end-user to modify the model of a more general-purpose fitting function.

Nearly any valid mathematical expression can be used, and a variety of built-in functions are available for flexible modeling.

## 4.2 Supported Operators, Functions, and Constants

The mathematical expressions used to define constrained `Parameters` need to be valid python expressions. As you'd expect, the operators '+', '-', '\*', '/', '\*\*', are supported. In fact, a much more complete set can be used, including Python's bit- and logical operators:

```
+, -, *, /, **, &, |, ^, <<, >>, %, and, or,
==, >, >=, <, <=, !=, ~, not, is, is not, in, not in
```

The values for  $e$  (2.7182818...) and  $\pi$  (3.1415926...) are available, as are several supported mathematical and trigonometric function:

```
abs, acos, acosh, asin, asinh, atan, atan2, atanh, ceil, copysign, cos, cosh, degrees, exp,
fabs, factorial, floor, fmod, frexp, fsum, hypot, isinf, isnan, ldexp, log, log10, loglp,
max, min, modf, pow, radians, sin, sinh, sqrt, tan, tanh, trunc
```

In addition, all Parameter names will be available in the mathematical expressions. Thus, with parameters for a few peak-like functions:

```
pars = Parameters()
pars.add('amp_1', value=0.5, min=0, max=1)
pars.add('cen_1', value=2.2)
pars.add('wid_1', value=0.2)
```

The following expression are all valid:

```
pars.add('amp_2', expr='(2.0 - amp_1**2)')
pars.add('cen_2', expr='cen_1 * wid_2 / max(wid_1, 0.001)')
pars.add('wid_2', expr='sqrt(pi)*wid_1')
```

In fact, almost any valid Python expression is allowed. A notable example is that Python's 1-line *if expression* is supported:

```
pars.add('bounded', expr='param_a if test_val/2. > 100 else param_b')
```

which is equivalent to the more familiar:

```
if test_val/2. > 100:
    bounded = param_a
else:
    bounded = param_b
```

## 4.3 Advanced usage of Expressions in Imfit

The expression is converted to a Python [Abstract Syntax Tree](#), which is an intermediate version of the expression – a syntax-checked, partially compiled expression. Among other things, this means that Python's own parser is used to parse and convert the expression into something that can easily be evaluated within Python. It also means that the symbols in the expressions can point to any Python object.

In fact, the use of Python's AST allows a nearly full version of Python to be supported, without using Python's built-in `eval()` function. The `asteval` module included with Imfit actually supports most Python syntax, including for- and while-loops, conditional expressions, and user-defined functions. There are several unsupported Python constructs, most notably the class statement, so that new classes cannot be created, and the import statement, which helps make the `asteval` module safe from malicious use.

This means that you can add domain-specific functions into the `asteval` module for later use in constraint expressions. To do this, you would use the `asteval` attribute of the `Minimizer` class, which contains a complete AST interpreter. As used in Imfit, the `asteval` module uses a flat namespace, implemented as a single dictionary. That means you can preload any Python symbol into the namespace for the constraints:

```
def lorenztian(x, amp, cen, wid):
    "lorenztian function: wid = half-width at half-max"
    return (amp / (1 + ((x-cen)/wid)**2))

fitter = Minimizer()
fitter.asteval.symtable['lorenztian'] = lorenztian
```

and this `lorenztian()` function can now be used in constraint expressions.

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