(check

chain rule

$$\frac{\partial}{\partial y}\left(-\frac{1}{x}\cos xy\right) = -\frac{1}{x}\frac{\partial}{\partial xy}(\cos xy)$$

$$= -\frac{1}{x}(-\sin xy)\frac{\partial}{\partial y}(xy)$$

$$= \sin xy$$