$$\Gamma(\alpha+1) = \int_0^\infty \overbrace{x^{-\alpha}}^{u}\overbrace{e^{-x}dx}^{dv}$$

$$= \underset{u}{(-x^{\alpha}}\underset{v}{e^{-x}})\Big|_0^\infty - \int_0^\infty \overbrace{\alpha x^{\alpha-1}}^{du}(-\overbrace{e^{-x}}^{v})dx$$

$$= \alpha \int_0^\infty x^{\alpha-1}e^{-x}dx$$