$P((X = x) \cap (Y = y)) = P(X = x)P(Y = y)$

 \Leftrightarrow and P(X = x, Y = y) = P(X = x)P(Y = y)

 $P_{X,y}(x,y) = P_X(x)P_Y(y)$