

Then

$$h'(x) = \frac{d}{dx} \ln f(x) = \frac{1}{f(x)} \frac{df}{dx} = \frac{f'(x)}{f(x)}$$

chain rule