$$= P\left(\frac{n+1}{\sigma^{2}}\right)^{2} < \chi^{2}_{\alpha/2, n-1}, \quad \chi^{2}_{1-\alpha/2, n-1} < \frac{n+1}{\sigma^{2}}\right)^{2}$$

$$= P\left(V < \chi^{2}_{\alpha/2, n-1}, \quad \chi^{2}_{1-\alpha/2, n-1} < V\right)$$

$$= P\left(\chi^{2}_{1-\alpha/2, n-1} < V < \chi^{2}_{\alpha/2, n-1}\right)$$